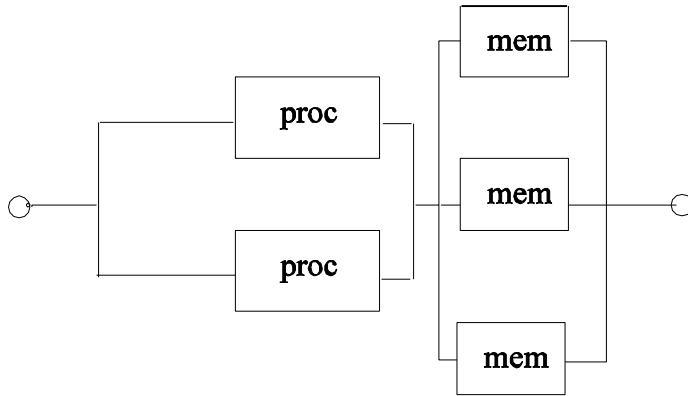


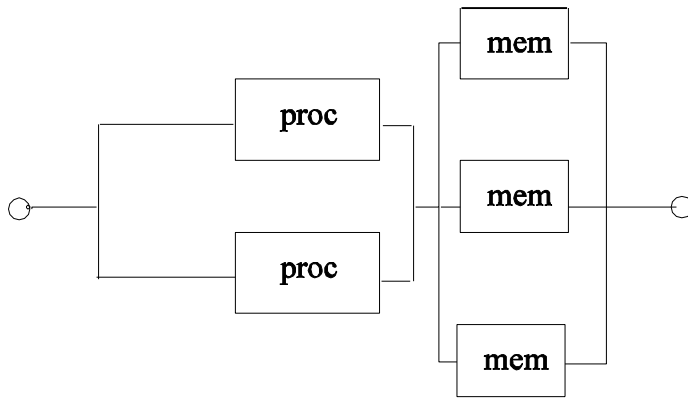
# Example

Multiprocessor system with 2 processors and 3 shared memories system.  
System is operational if at least one processor and one memory are operational.



$\lambda_m$  failure rate for memory  
 $\lambda_p$  failure rate for processor

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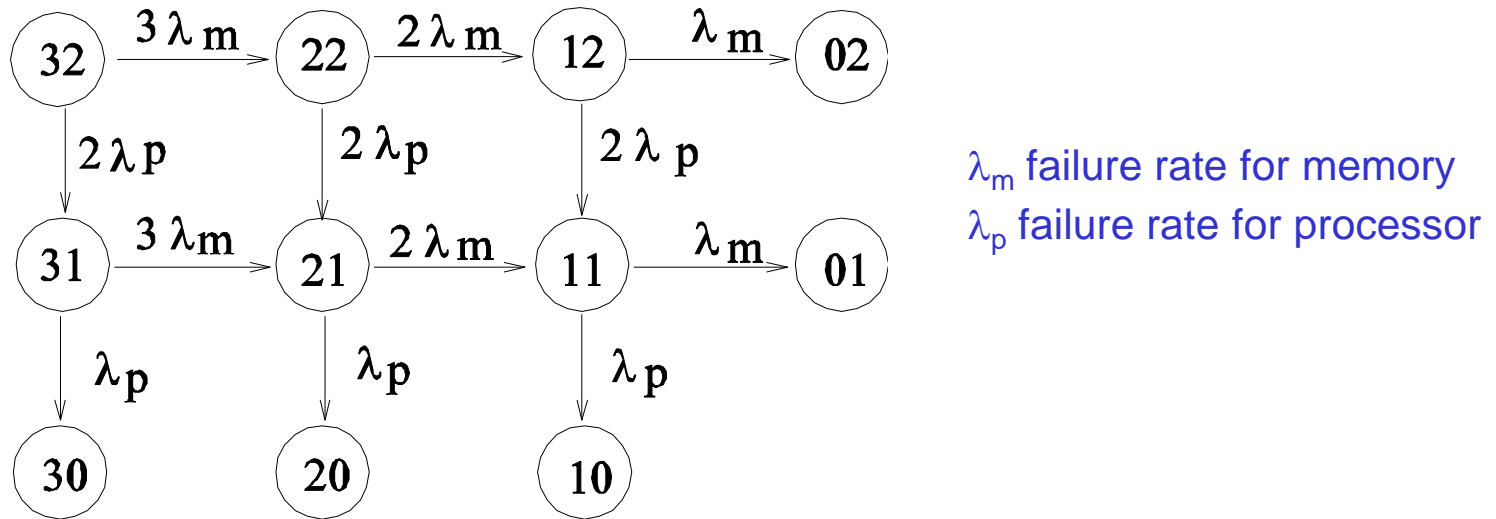
Given a state (i, j):

i is the number of operational memories;

j is the number of operational processors

$$S = \{(3,2), (3,1), (3,0), (2,2), (2,1), (2,0), (1,2), (1,1), (1,0), (0,2), (0,1)\}$$

## Markov chain



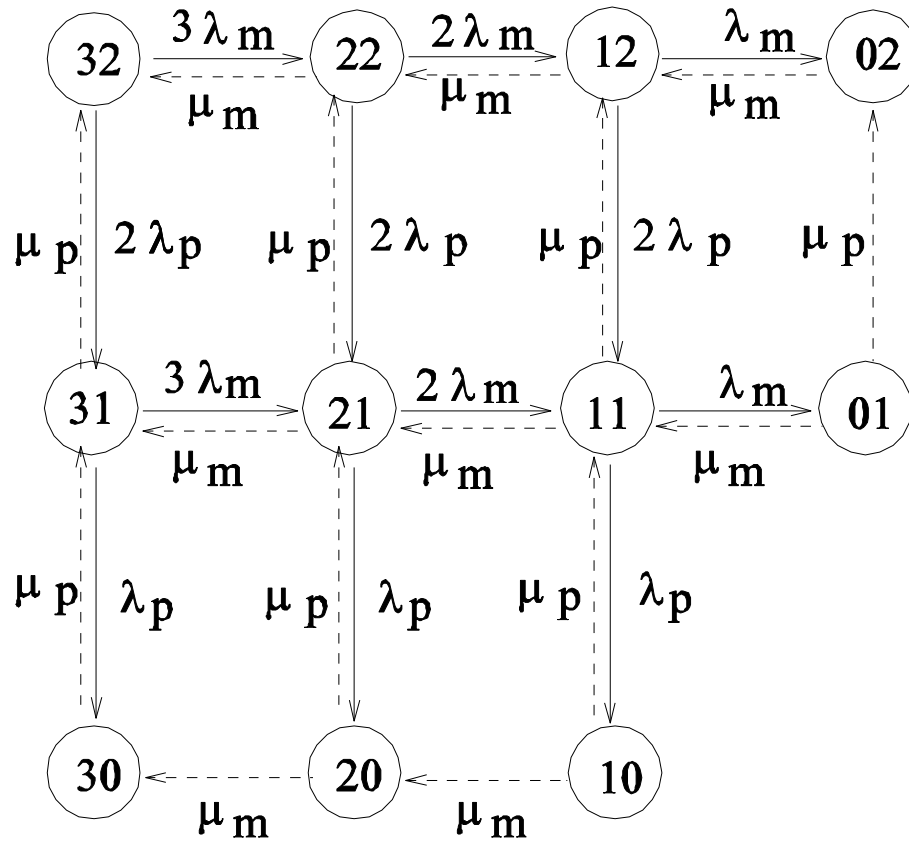
(3, 2)  $\rightarrow$  (2,2) after a memory fault

(3,0), (2,0), (1,0), (0,2), (0,1) are absorbent states

# Availability modeling

- Assume that faulty components are replaced and we evaluate the probability that the system is operational at time  $t$
- Constant repair rate  $\mu$  (number of expected repairs in a unit of time)
- Strategy of repair:  
only one processor or one memory at a time can be substituted

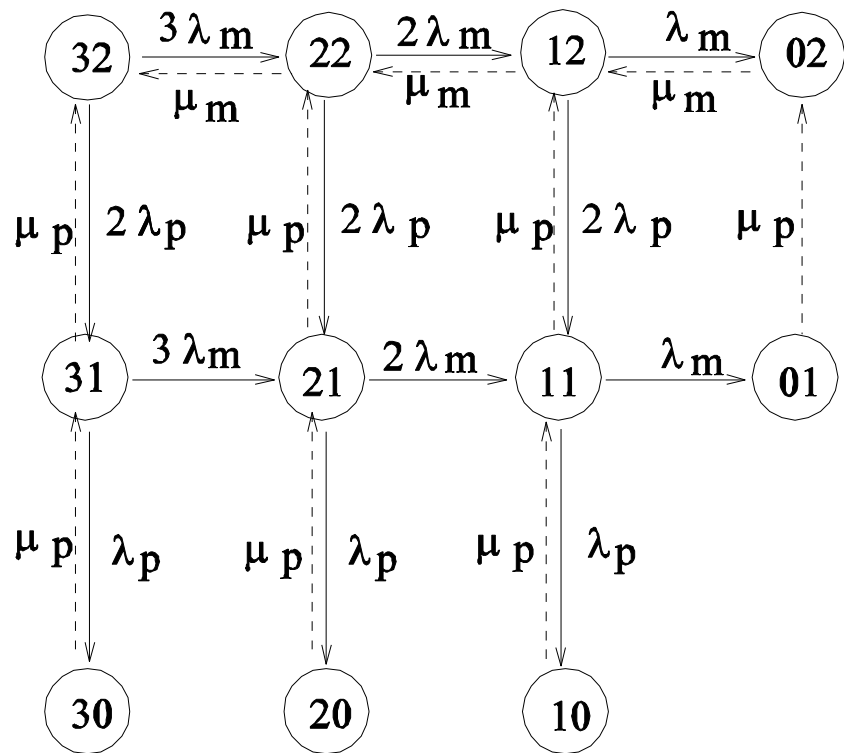
Markov chain modelling the 2 processors and 3 shared memories system with repair.



$\lambda_m$  failure rate for memory  
 $\lambda_p$  failure rate for processor  
 $\mu_m$  repair rate for memory  
 $\mu_p$  repair rate for processor

- Strategy of repair:
  - only one component can be substituted at a time
  - processor higher priority

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  - only one component can be substituted at a time
  - processor higher priority



exclude the lines  $\mu m$   
representing memory repair  
in the case where there has  
been a process failure