

# Möbius Tool

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LAB 03

# Contacts

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# Overview

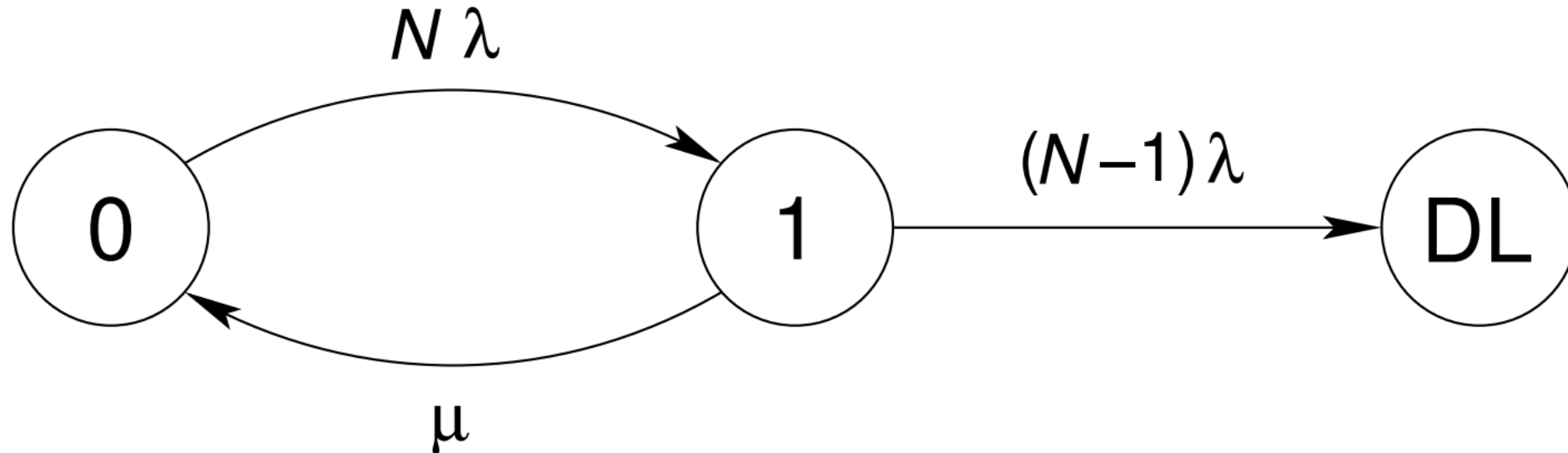
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- Tutorial on RAID5 and RAID51
  - Systems formalization
  - Markov chains
  - Mobius SAN models

# System formalization of RAID5

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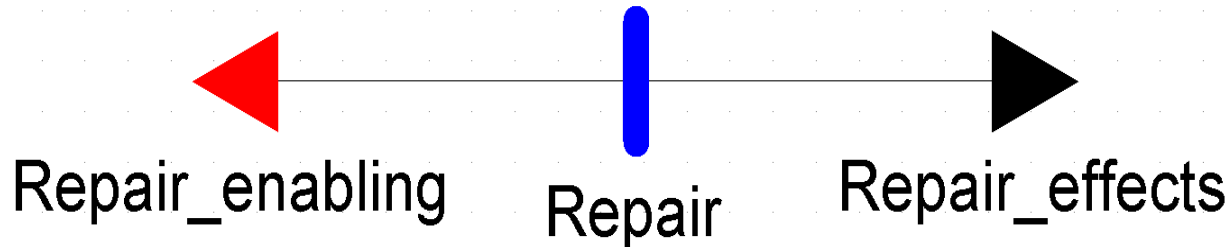
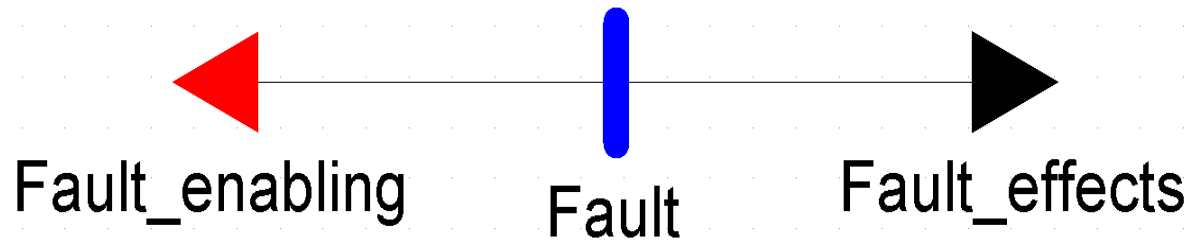
- RAID5 scheme arranges  $N$  disks an array, with one redundant disk, and can tolerate(repair) up to 1 disk failure.
- Assume  $\lambda$  is the failure rate of a disk and  $\mu$  is the repair rate, then the Markov Chain of a RAID5 array is the following, where each state represents the number of failed disks.



# RAID5 in Mobius

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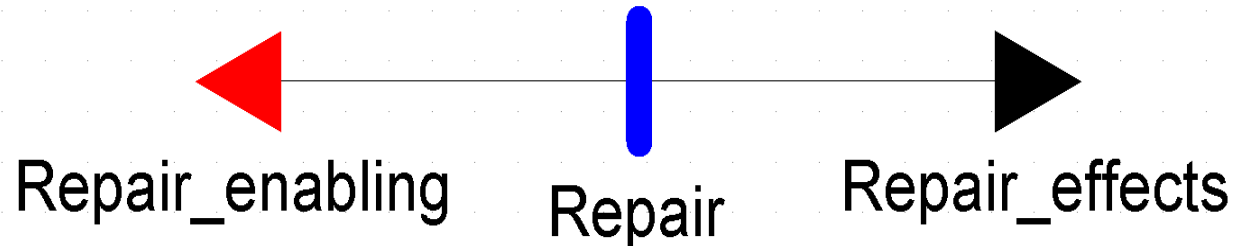
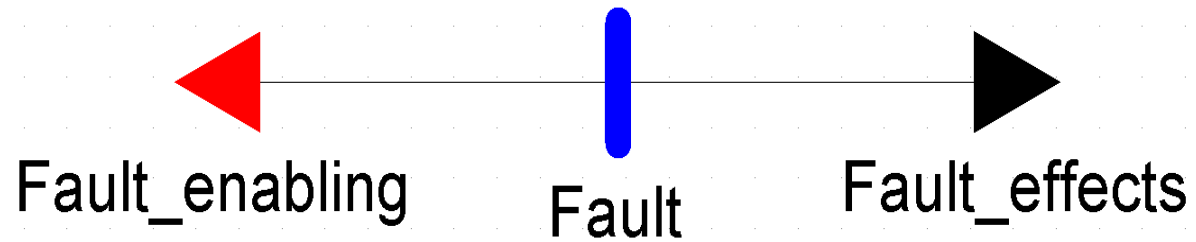
  
Disks



Initial tokens of Disks?  
Fault enabling?  
Fault effect?  
Fault rate?  
Repair enabling?  
Repair effect?  
Repair rate?  
Data loss condition?

# RAID5 in Mobius

  
Disks



Initial tokens of Disks?  $N$

Fault enabling?  $\text{Disks} \rightarrow \text{Mark}() > 0$

Fault effect?  $\text{Disks} \rightarrow \text{Mark}()--;$

Fault rate?  $\text{Disks} \rightarrow \text{Mark}() * \lambda$

Repair enabling?  $\text{Disks} \rightarrow \text{Mark}() == N-1$

Repair effect?  $\text{Disks} \rightarrow \text{Mark}()++;$

Repair rate?  $\mu$

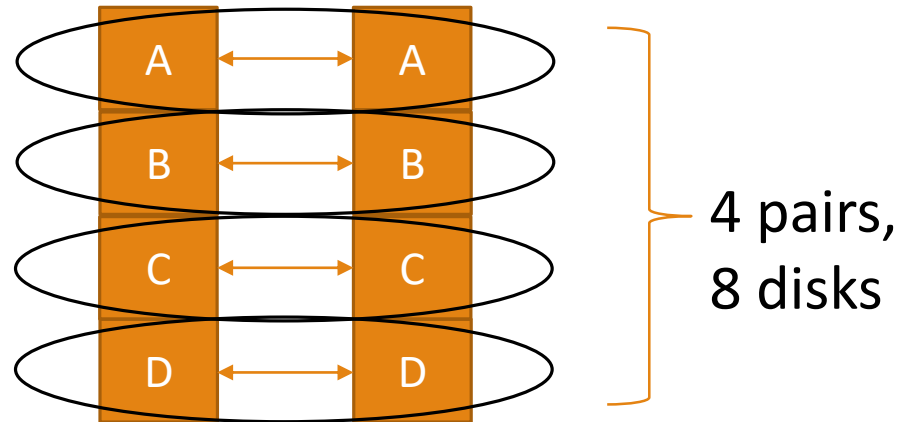
Data loss condition?

$\text{Disks} \rightarrow \text{Mark}() < N-1$

# System Formalization of RAID51

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- RAID51 is a RAID5 array with mirroring.
- The contents of a failed disk is recovered first by its mirror,
  - and if it is not possible, it is recovered through the corresponding RAID5 array.
- The configuration comprises  $D$  pairs of disks, where each pair contains 2 disks with identical content



# Markov Chain of RAID51

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$D, 0, 0$

$D$  is the size of an array.

$\lambda$  and  $\mu$  failure and repair rates of a disk.

Each state is represented by a triplete(  $x, y, z$ ) where:

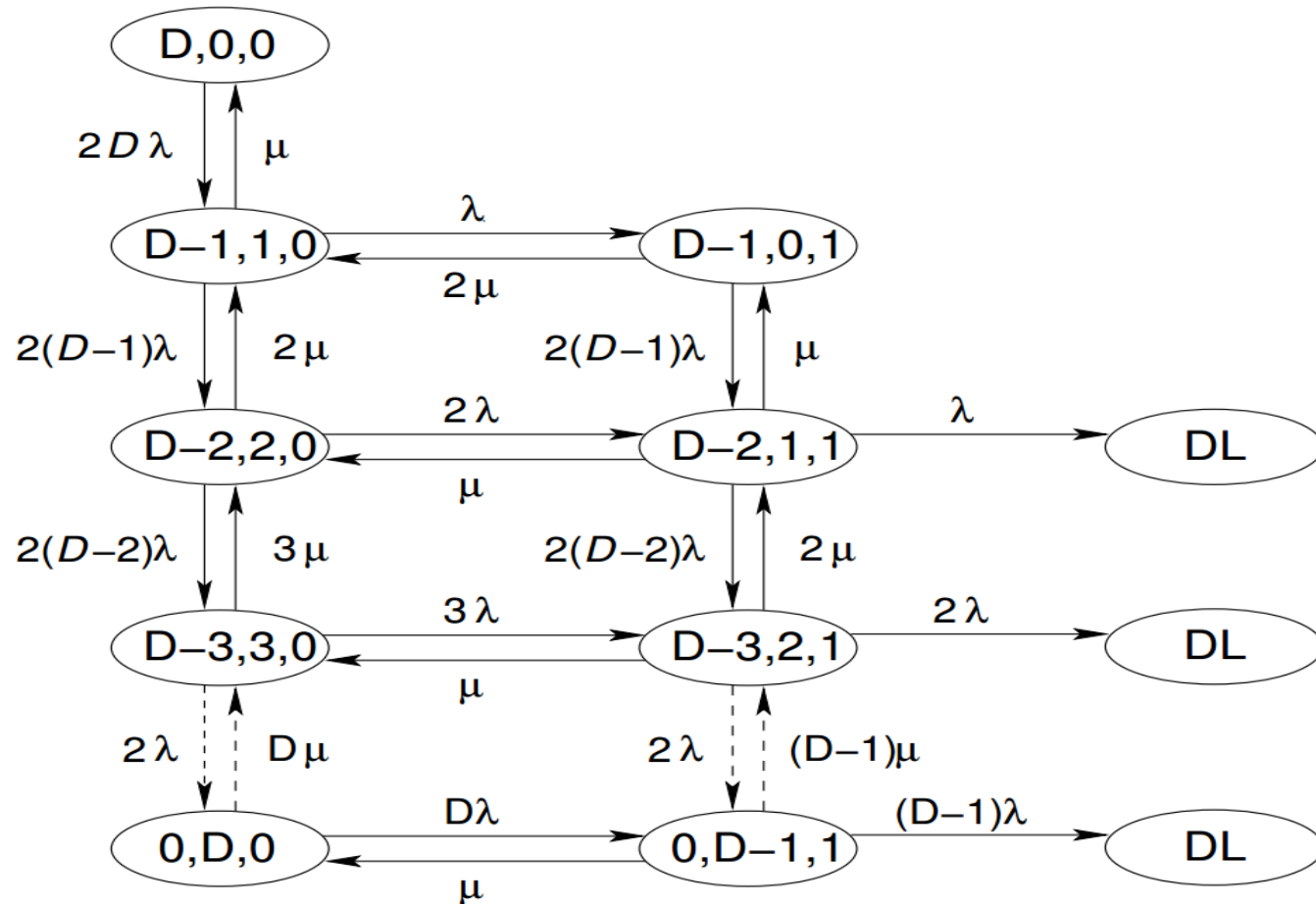
$x$  represents the number of pairs with both disks working.

$y$  represents the number of pairs with one disk working.

$z$  represents the number of pairs with both disks failed.



# Markov Chain of RAID51



$D$  is the size of an array.

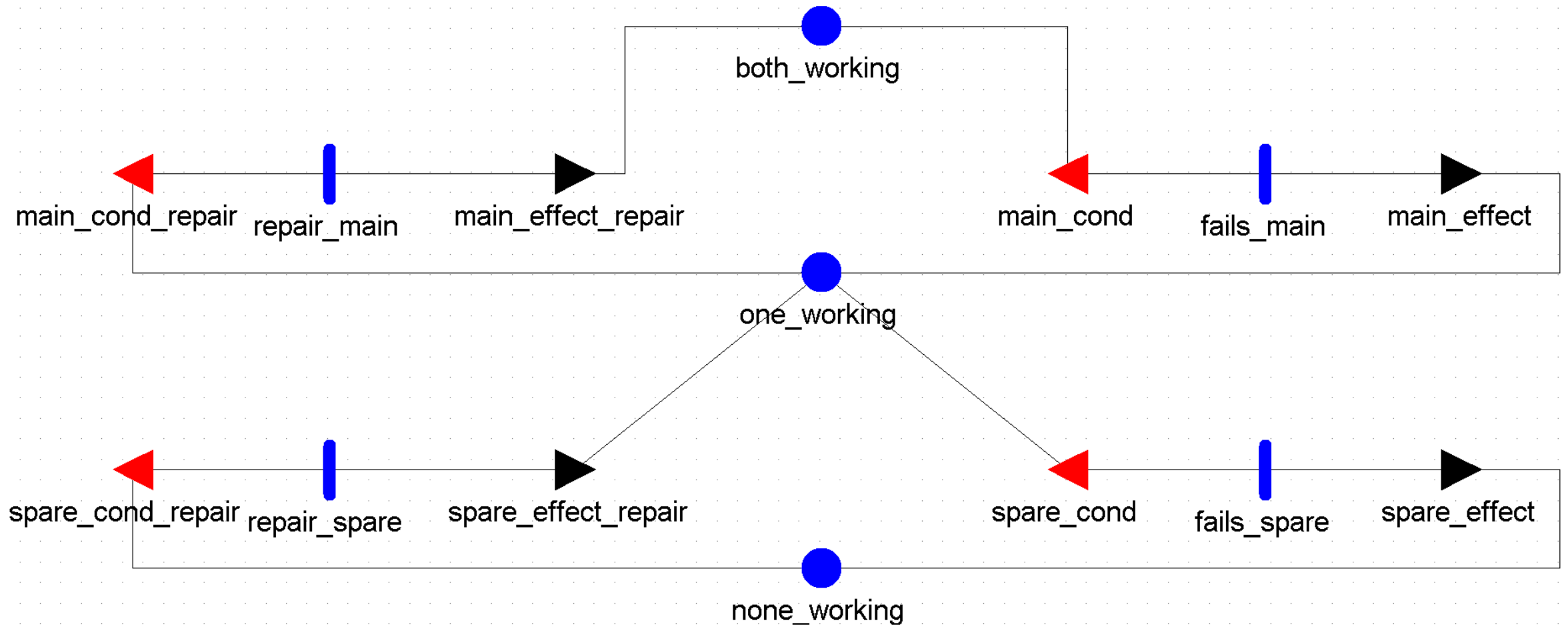
Each state is represented by a triplet  $(x, y, z)$  where:

$x$  represents the number of pairs with both disks working.

$y$  represents the number of pairs with one disk working.

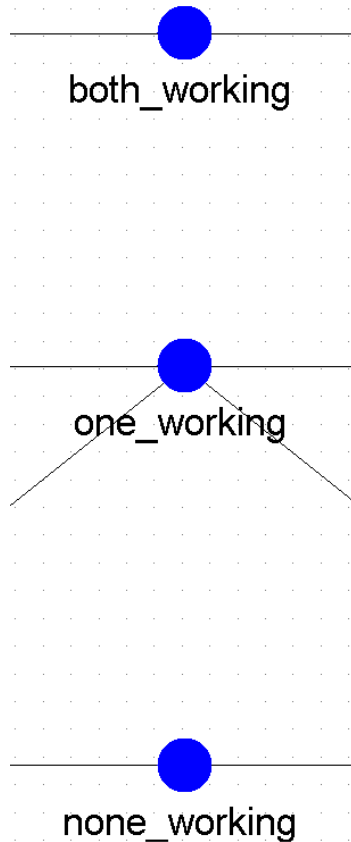
$z$  represents the number of pairs with both disks failed.

# RAID51 in Mobius



# Places of RAID51 model

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Place that represents the number of pairs with both disks working (  $x$  ).

Initial number of tokens?

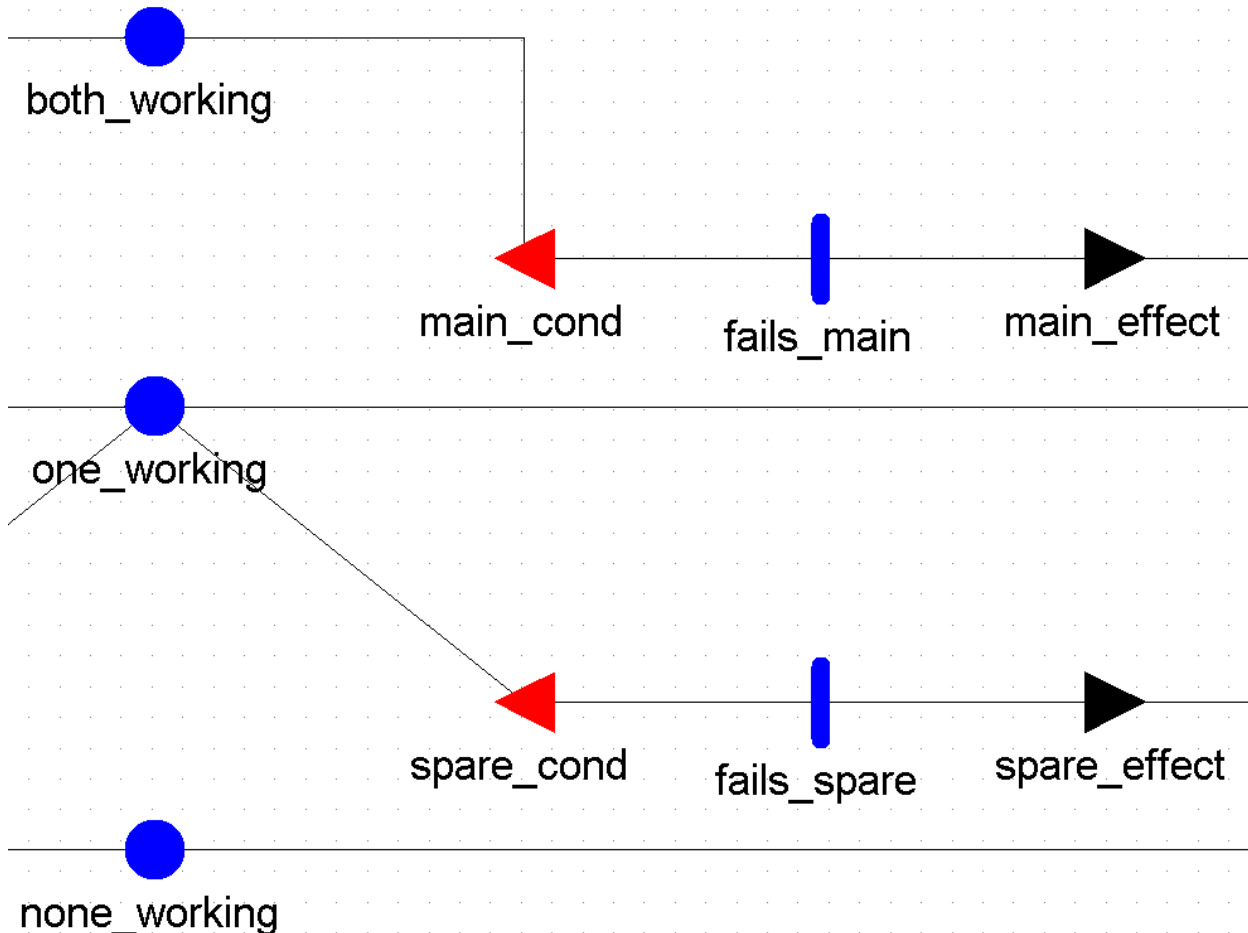
Place that represents the number of pairs with one disk working (  $y$  ).

Initial number of tokens?

Place that represents the number of pairs with no disk working (  $z$  ).

Initial number of tokens?

# Transitions 1/2



**Fails\_main** represents the failure of a disk which is within a pair of **both working** disks

**Enabling condition?**

**Effect?**

**Rate?**

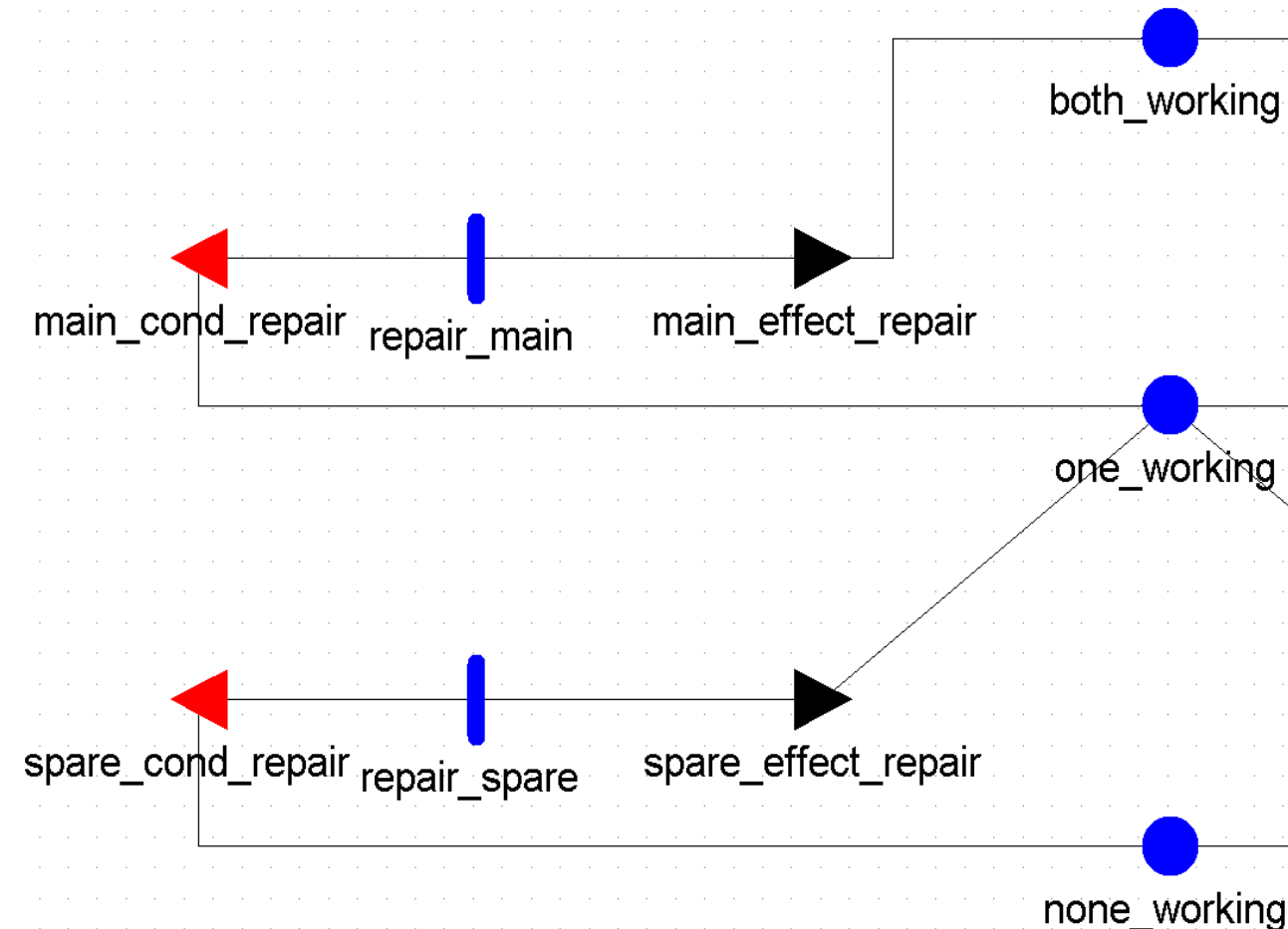
**Fails\_spare** represents the failure of a disk which is within a pair of **one working** disks

**Enabling condition?**

**Effect?**

**Rate?**

# Transition 2/2



**repair\_main** represents the repair of a disk which is within a pair of **one working** disks

**Enabling condition?**

**Effect?**

**Rate?**

**repair\_spare** represents the repair of a disk which is within a pair of **none working** disks

**Enabling condition?**

**Effect?**

**Rate?**

# References

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<https://pdfs.semanticscholar.org/f2f1/b23e010de35e2537abab741fb8f9417a0827.pdf>

[https://www.mobius.illinois.edu/wiki/index.php/Möbius\\_Documentation](https://www.mobius.illinois.edu/wiki/index.php/Möbius_Documentation)

Thanks to prof. Andrea Domenici for previous version of the slides.