# Towards Stochastic FMI Co-simulations: Implementation of an FMU for a Stochastic Activity Networks Simulator

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#### A naïve question

Can I plug a new simulator into an existing multi-model?

an almost trivial solution.

#### A not-so-naïve question:

Can I 'plug' a nondeterministic/stochastic simulation into a deterministic multi-model?

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yet to be found not-so-trivial solutions (see last slide).

# Stochastic Activity Networks (1)

The *Stochastic Activity Networks* (SAN) are a wide-ranging and complex extension to Petri Nets.

Petri Net = places + marking + transitions + enabling conditions + firing rules.

Stochastic Petri Net = PN + stochastic transition delay.

Stochastic Activity Network = SPN + stochastic transition outcome + user-defined enabling conditions + user-defined firing rules +  $\dots$ 

William H. Sanders and John F. Meyer, "Stochastic Activity Networks: formal definitions and concepts", in Lectures on formal methods and performance analysis: first EEF/Euro summer school on trends in computer science, 2002.

## Stochastic Activity Networks (2)

Activities may be *timed* or *instantaneous* (or *immediate*).

*Enabling conditions*: activities are enabled by user-defined **input predicates** associated with **input gates**.

An input predicate is a Boolean function of the net marking.

*Firing rules*: user defined functions specifying the next marking can be associated with input gates (**input functions**) and **output gates** (**output functions**).

*Stochastic transition outcome*: Alternative results of an activity can be specified as mutually exclusive **cases** associated with the activity.

Each case has a probability defined by a function of the marking (it may be a constant).

# The Möbius tool

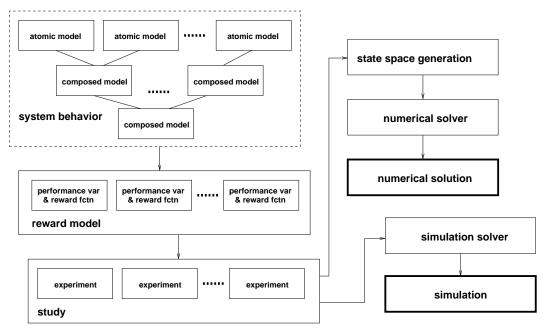
The Möbius environment provides:

- Graphical editor to make (*atomic*) SAN models.
- Hierarchical composition of models.
- Reward models to define and compute *performance variables*, i.e., quantitative properties related to system performance or dependability.
- Numerical solution of Markov chain equations, if certain constraints on the model are satisfied.
- System simulation satisfying user-defined statistical parameters, such as confidence level and confidence interval.

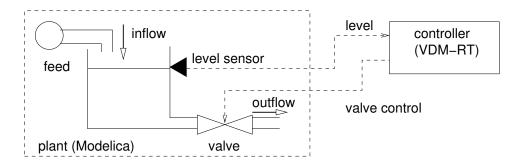
G. Clark *et al.*, "The Möbius modeling tool", in 9th Int. Workshop on Petri Nets and Performance Models, 2001.

The Möbius Manual, Version 2.4 Rev. 1, https://www.mobius.illinois.edu/docs/MobiusManual.pdf

## The Möbius analysis process



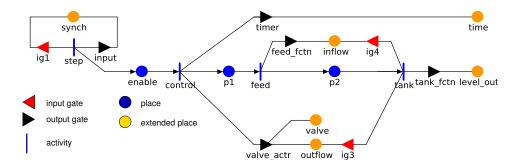
# The INTO-CPS Water Tank Example



constant inflow, outflow depends on current volume

```
valvecontrol = if level >= maxlevel then 1.0 (fully open)
else if level < minlevel then 0.0 (fully closed)
else valvecontrol unchanged;
```

# The SAN Model



Physical behavior:

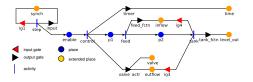
variable feed flow (inflow) valve opens gradually drain flow (outflow) depends on valve area

# The SAN Model: synchronization (1)

```
Input gate ig1 predicate:
synch->Mark() == 1
Output gate input function:
```

```
// wait for input from controller
cin >> x;
```

```
if (x == 1) {
    valve_control.Set(1);
} else if(x == -1) {
    valve_control.Set(-1);
} else if (x == 0) {
    valve_control.Set(0);
}
```



```
synch->Mark() = 0; // reset synch
// implicitly set enable place
```

With the FMI protocol, each simulator executes one simulation step when it receives an *fmi2DoStep* request from the master algorithm. The rate at which the master algorithm issues *fmi2DoStep* requests establishes a common time base for the simulators.

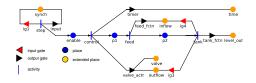
To synchronize the Möbius simulation, time has been simulated explicitly as a variable that, at each step, is incremented by a fixed amount equal to interval between *fmi2DoStep* requests.

# The SAN Model: synchronization (3)

#### Output gate timer function:

```
time->Mark() += dt;
```

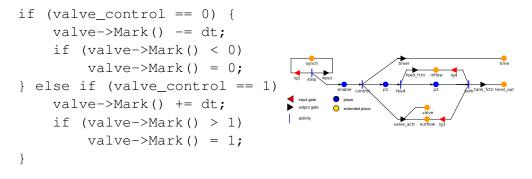
```
if (time->Mark() > maxtime)
    exit(0);
```



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#### The SAN Model: valve actuation

Output gate valve\_actuator function:



outflow->Mark() = C\*valve->Mark();

### The SAN Model: tank behavior

#### Output gate tank\_fctn function:

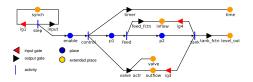
```
double netfl =
    inflow->Mark() - outflow->Mark();
level_out->Mark() =
    level_out->Mark() + netfl*dt;
```

```
if (level_out->Mark() < 0)
    level_out->Mark() = 0;
```

level.Set(level\_out->Mark());

// set synch and enable step
synch->Mark() = 1;

// send level to controller
cout << level\_out->Mark();





# The FMU

Implement fmi2Instantiate:

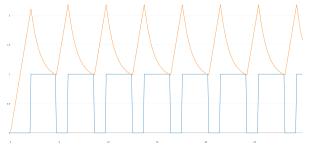
create pipes to redirect stdin and stdout; spawn process running the Möbius-generated executable; connect pipes.

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Implement fmi2DoStep:

send control signal to Möbius process; receive and parse level value from Möbius process; send back level value to COE.

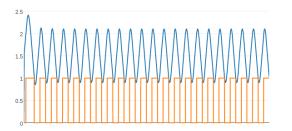
# **Co-simulation**



- (Controller)-cont.valve - (NaterTank) wt.level

#### **INTO-CPS** distribution

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Möbius tool

## Further work

Initial work towards integration of statistical simulation techniques

... but statistics not yet used!

Much work needed to deal with important issues:

- A more modular approach is needed.
  - Reduce to a minimum the changes to fit a self-standing model into an existing multi-model;
  - how much knowledge on the model is needed (white/black/gray box)?
  - Möbius is a rather closed environment.
- A smarter synchronization mechanism is needed if statistical parameters are to be computed.
- A deeper understanding of the interaction between deterministic and non-deterministic models is needed.

Lawrence, D.P.Y., Gomes, C., Denil, J., Vangheluwe, H., Buchs, D.: Coupling Petri nets with deterministic formalisms using co-simulation. In: Proceedings of the Symposium on Theory of Modeling & Simulation. pp. 6:1–6:8. TMS-DEVS '16, Society for Computer Simulation International, San Diego, CA, USA (2016)

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