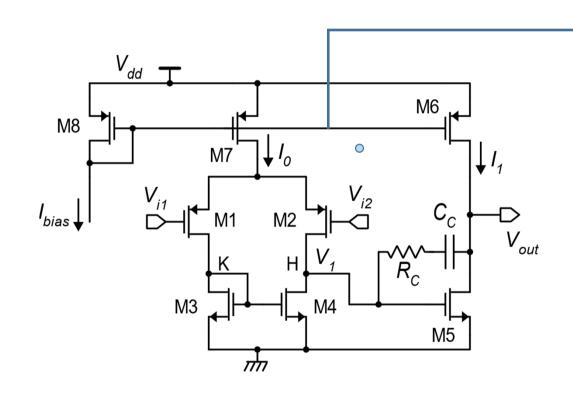
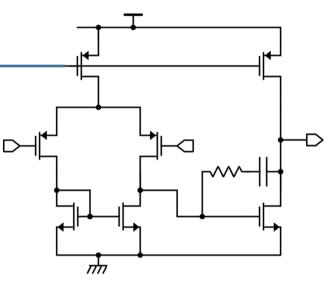


P. Bruschi – Design of Mixed Signal Circuits

Use of a single M8 device to bias multiple op-amp

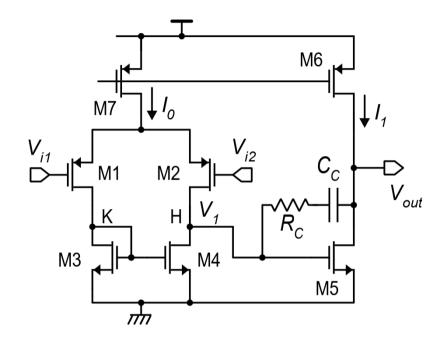




M8 can be shared among different amplifiers and is not part of the opamp architecture

For this reason, we do not consider M8 in the amplifier topology

Degrees Of Freedom (DOFs)



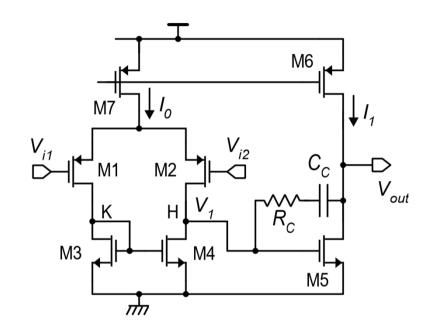
Possible DOFs:

W, L of all devices (14 DOFs) I_0 , I_1 C_C , R_C

First estimate: Total number of DOFS: 18 But ...

- Not all DOFs are independent.
- It is necessary to choose a set of independent DOFs

Constraints



Constraints are relationships among DOFs

Two types of constraints:

• Equality constraints:

$$\exists .g. \quad \frac{I_1}{I_0} = \frac{\beta_6}{\beta_7}$$

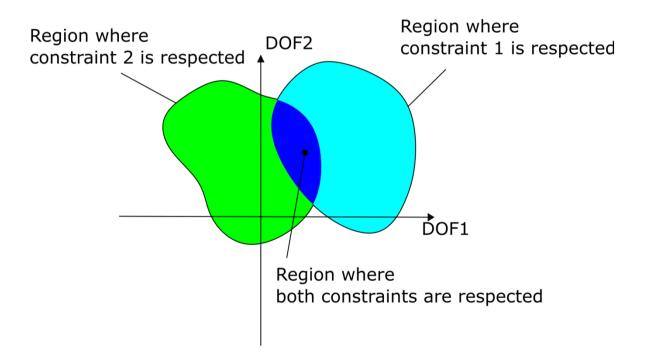
• Inequality constraints:

E.g. $GBW(DOFs) \ge GBW_{\min}$

Constraints

- Every equality constraint reduces the dimension of the DOF space. Equality constraints represent exact conditions that has to be fulfilled in order to guarantee correct operation of the circuit. Some equality constraints derive from simple considerations, such as symmetry: M1=M2, M3=M4. With a few exceptions, equality constraints are specific of the topology and does not depend on the specifications
- Inequality constraints are derived from the circuit specifications. They do not reduce the dimension of the DOF space but select regions of the DOF space where the specs are met.

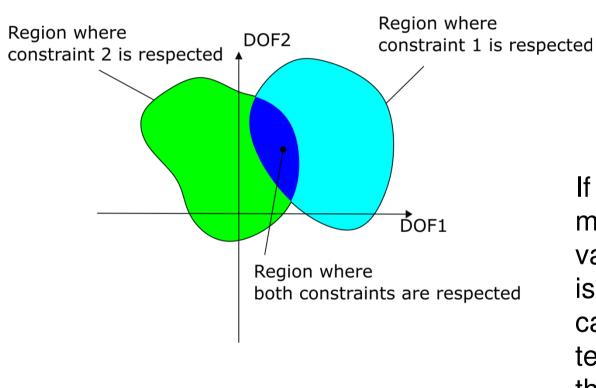
The sizing process: role of multiple inequality constraints A very simple case with only two independent DOFs and two inequality constraints



Combining the various inequality constraints, we find a domain (the intersection of all regions) where all points satisfy all constraints. All points in the domain are valid solutions.

If such region does not exist (null intersection), the sizing problem is: "unfeasible".

The sizing process: automatic algorithms



<u>Computer programs</u> that perform automatic sizing, are not compatible with an infinite number of feasible solutions. To find a single solution, an optimization condition is often added.

If the design is performed manually, any point (set of DOFs values) in the intersection domain is a good solution. Also in this case, optimization or arbitrary techniques can be used to operate the choice Sizing of a new topology: steps

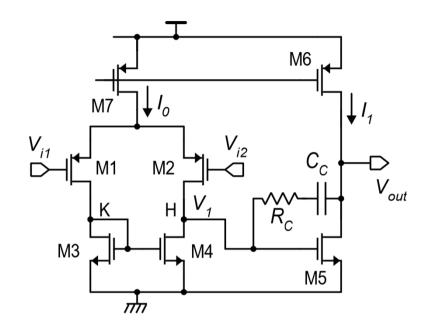
1. Find **equality constraints** to reduce the number of independent DOFs. These constraints will be of two types:

(a) Strictly necessary constraints (if not respected the circuit does not work properly)

(b) Arbitrary constraints: they are added to further reduce the DOF set and simplify the design. These constraints should be motivated.

- 2. Choose a set of DOFs that have the following properties:
 (a) the remaining dependent DOFs can be easily derived from this set;
 (b) the specifications (**inequality constraints**) can be written easily and in a simple form as a function of the selected DOFs
- 3. Write the specifications in terms of the selected DOFs and try to find general design rules.

Equality constraints for the simple 2-stage op-amp



Symmetry (necessary to obtain low offset and low CMRR

N. of equality constraints

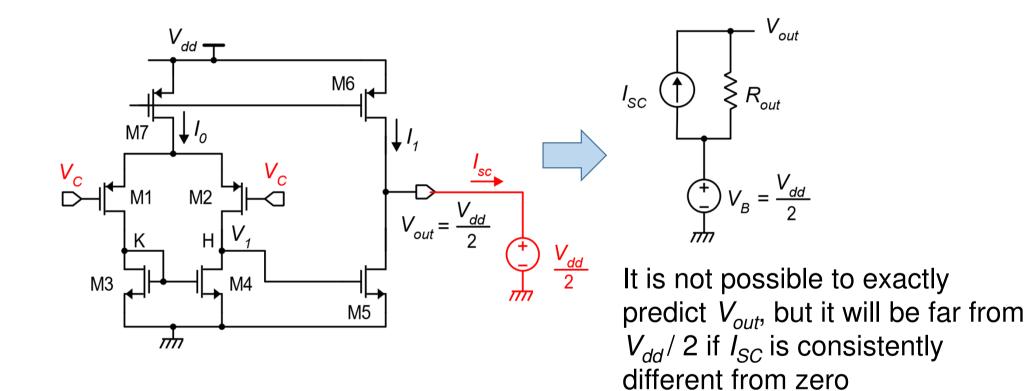
M1=M2
$$(W_1 = W_2, L_1 = L_2)$$
 ----- 2

M3=M4 (
$$W_3 = W_4$$
, $L_3 = L_4$) ----- 2

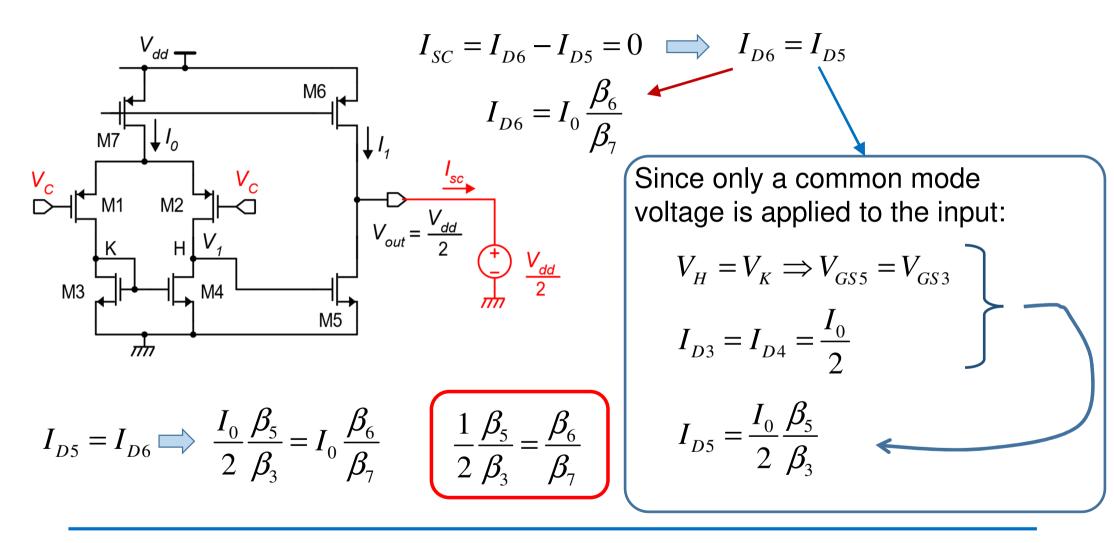
Current ratios

$$\frac{I_1}{I_0} = \frac{\beta_6}{\beta_7} = \frac{W_6 / L_6}{W_7 / L_7} \quad ----- 1$$

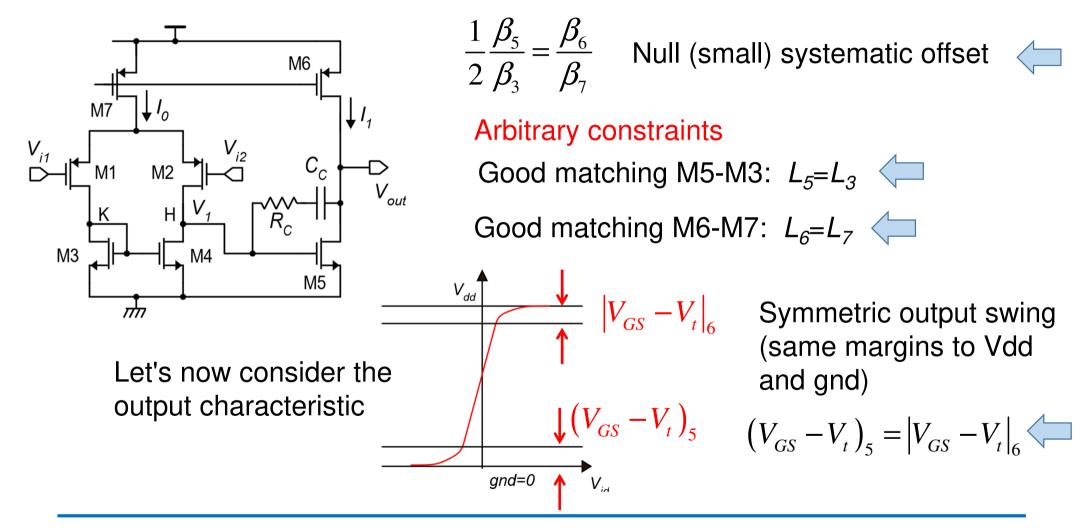
Initial DOF number: 18, Resulting DOFs after reduction: 18-5=13



Necessary constraint: null systematic offset



More constraints



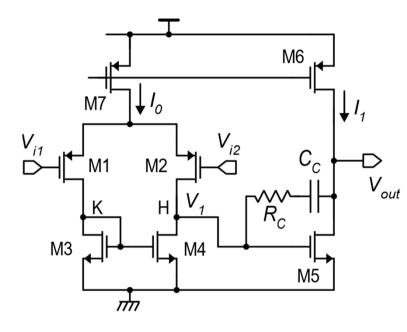
Residual number of DOFs

13 - 4 = 9 Of these residual DOFs we can separate two ones (C_C and R_C) that do not affect the dc performances and the operating point. We will come back to them later. Then we will focus on **7** DOFs (bias current I_0 and device size) that affect the operating point and we will call them "static" DOFs).

We could select 7 DOFs within the original set (16 DOFs, R_c and C_c are not included) and then try to derive the remaining ones using the equations that tie them (equality constraints).

It is more useful to choose a set of DOFs that may not necessarily include the original 18, in a way that the other ones can be easily derived.

Selection of the 7 DOFs



Rationale: the most important MOSFETs of the circuits are M1 (=M2) and M5, since these are the devices that are at the heart of the two stages, where they perform the V-to-I conversion.

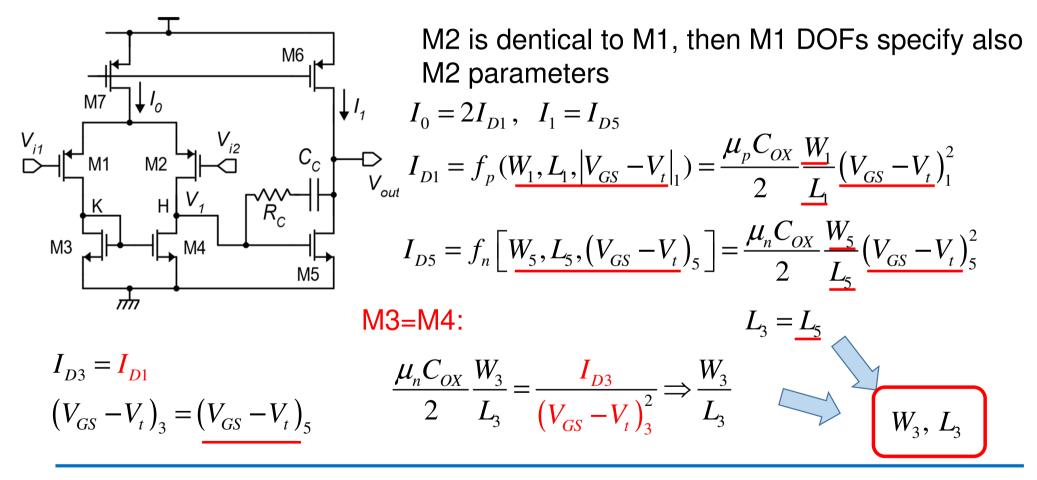
We include all possible DOFs of M1 and M5 into the selected set

M1:
$$W_1$$
, L_1 , $|V_{GS} - V_t|_1$ 6 DOFs
M5: W_5 , L_5 , $(V_{GS} - V_t)_5$

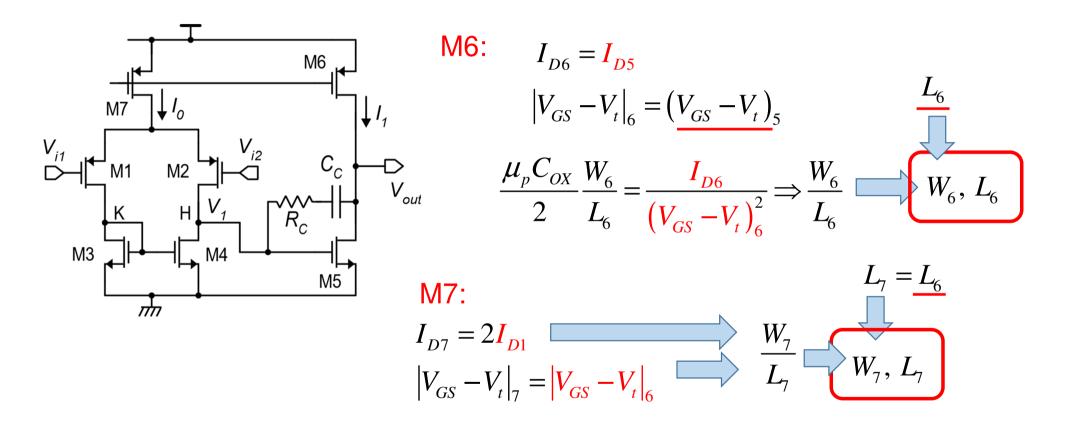
To complete the set, let us include also L_6 into the DOFs

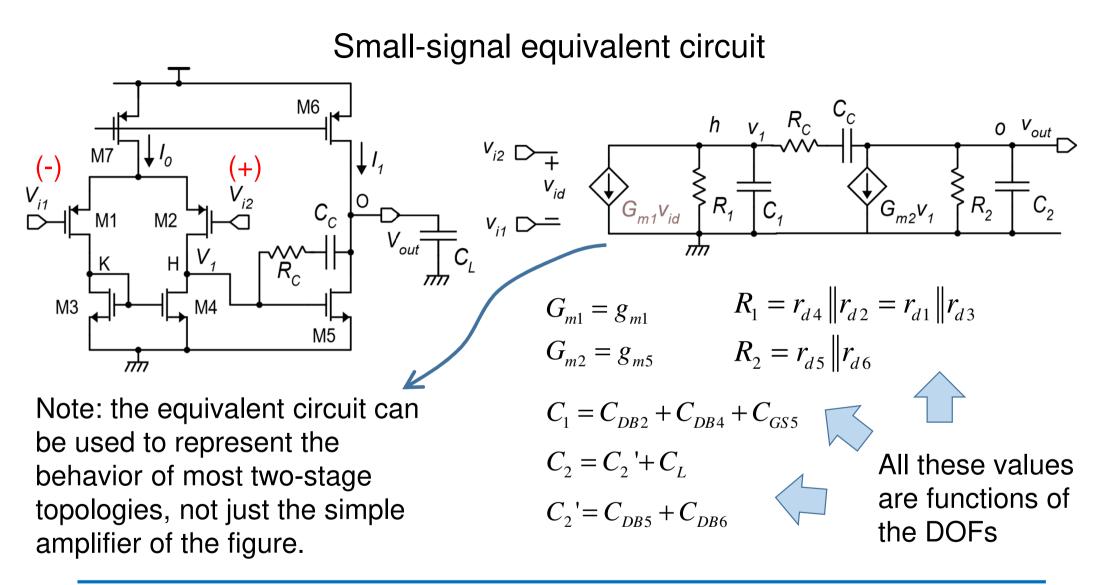
Final set of static DOFs: $\{W_1, L_1, |V_{GS} - V_t|_1, W_5, L_5, (V_{GS} - V_t)_5, L_6\}$

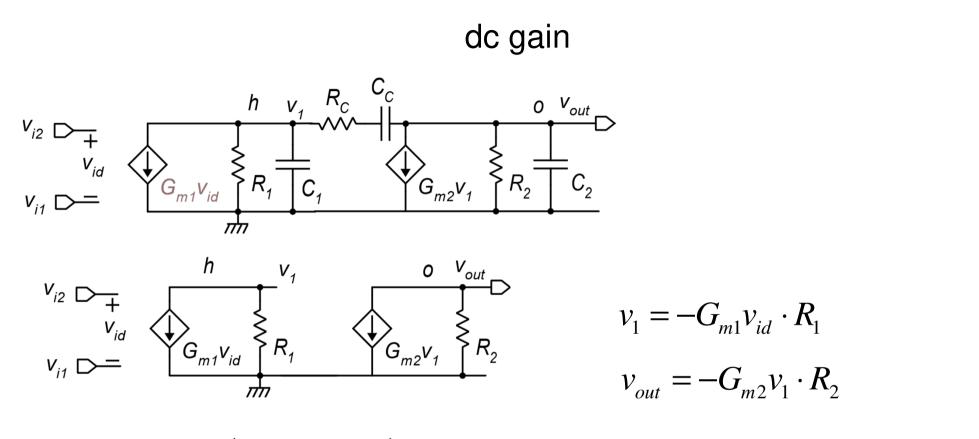
Derivation of all the op-amp parameters from the 7 DOFs All conditions will refer to the operating point ($V_{id}=0$)



Derivation of all the op-amp parameters from the 7 DOFs

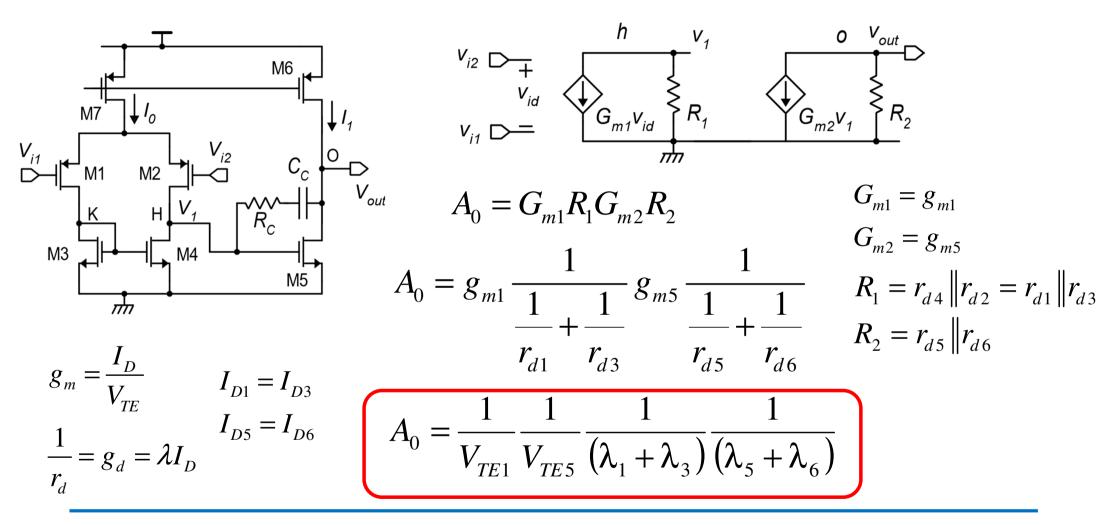






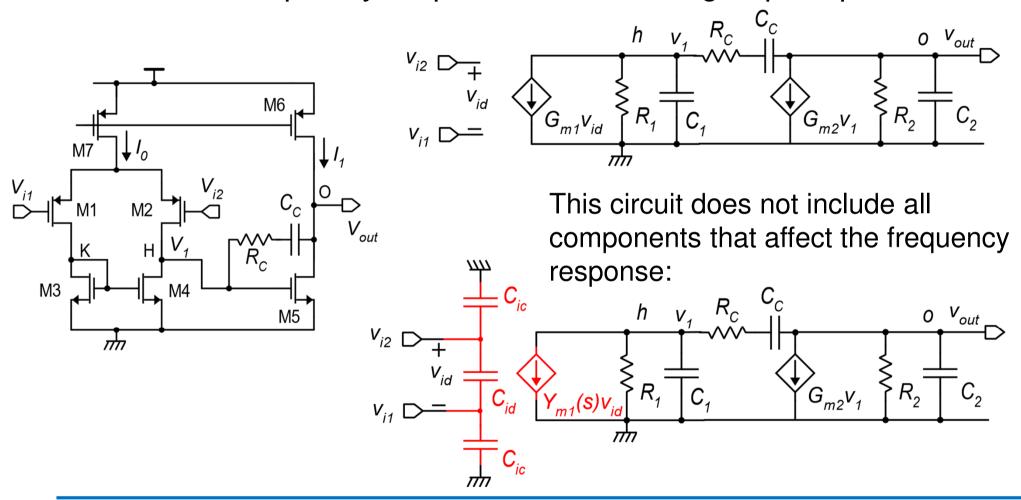
 $v_{out} = -G_{m2} \left(-G_{m1} v_{id} \cdot R_1 \right) R_2 = G_{m1} R_1 G_{m2} R_2 v_{id} \implies A_0 = G_{m1} R_1 G_{m2} R_2$

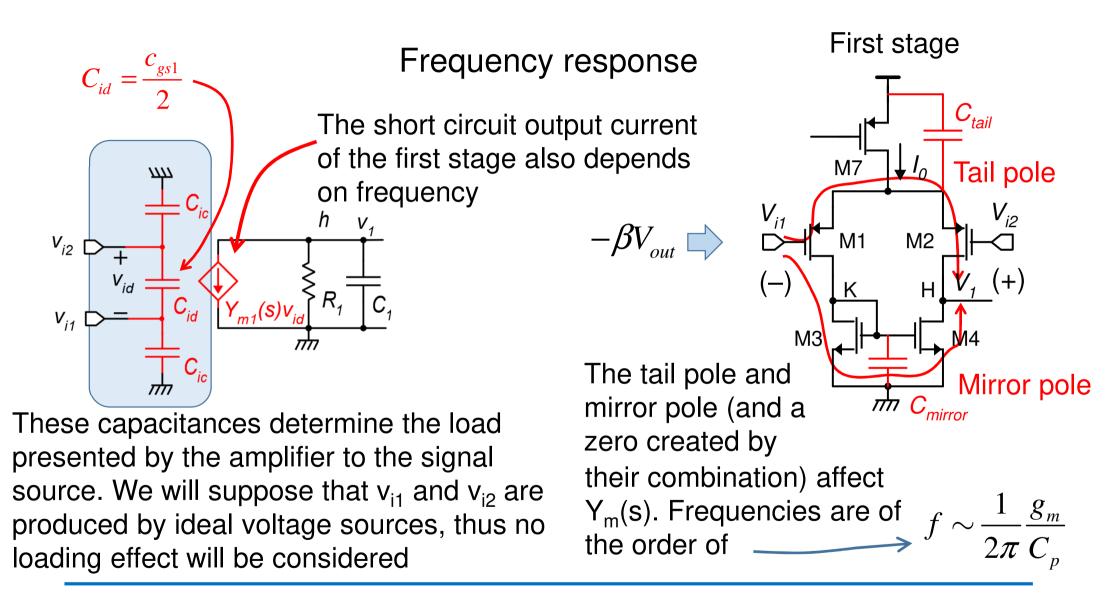
dc gain as a function of the DOFs



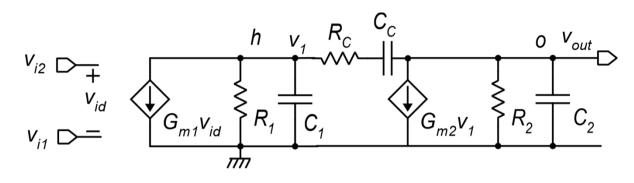
P. Bruschi – Microelectronic System Design

Frequency response of a two-stage op-amp

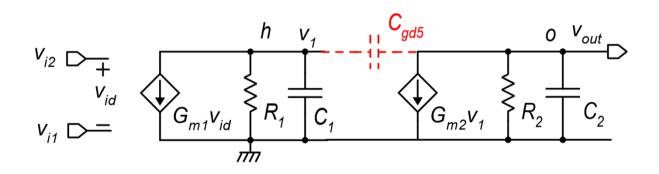




Frequency response, simplified small-signal circuit

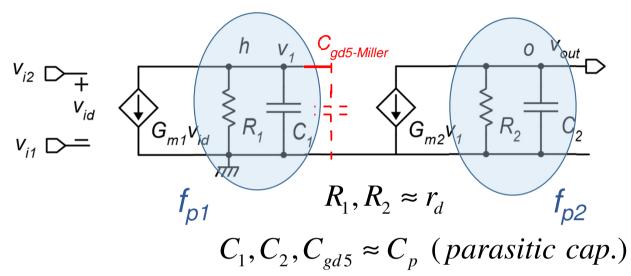


If the compensation group C_C - R_C is not present:



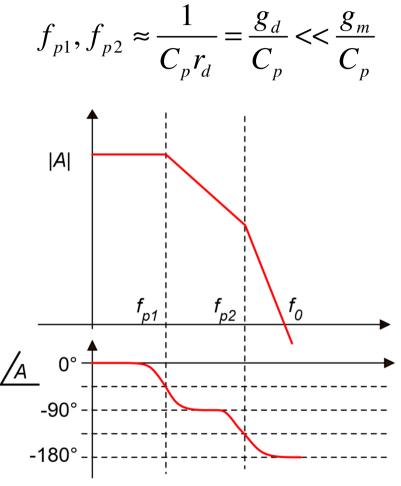
We still have C_{gd5} parasitic capacitance, which is not sufficient to produce the compensation effect

Uncompensated frequency response

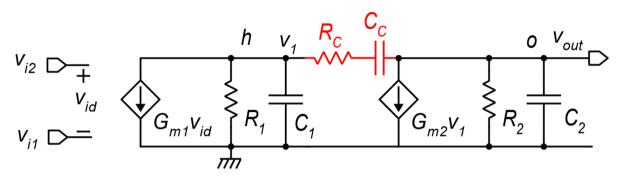


Without compensation, we have two poles at frequencies f_{p1} , f_{p2} , which are of the same order of magnitude and none of them is dominant.

The result is a very small or even negative (= instability) phase margin.



Miller compensation = Pole splitting



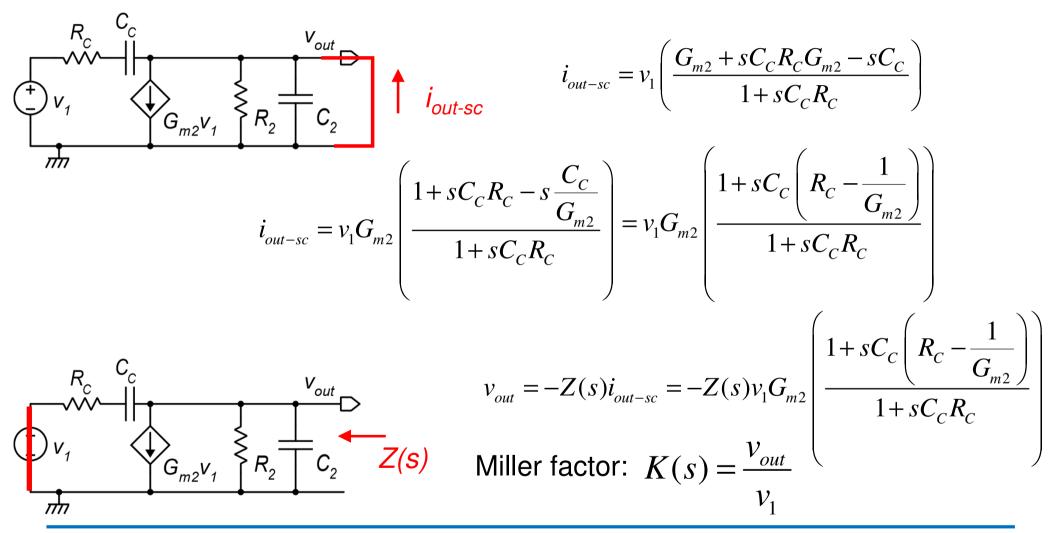
To do this, we need to calculate the Miller factor $K=v_{out}/v_1$. We force voltage v_1 and use the Norton equivalent model of the output port. It is convenient to divide the bridge impedance R_C - C_C into two impedances by means of the Miller theorem

of the output port.

$$i_{out-sc} = G_{m2}v_1 - \frac{v_1}{R_c} + \frac{1}{sC_c} = v_1 \left(G_{m2} - \frac{sC_c}{1 + sC_cR_c} \right)$$

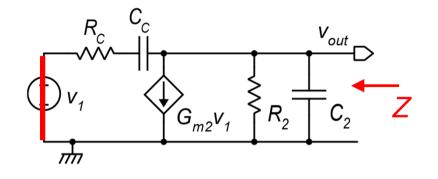
$$\downarrow v_1 \qquad \downarrow G_{m2}v_1 \qquad \downarrow R_2 \qquad \downarrow C_2 \qquad \uparrow i_{out-sc} = v_1 \left(\frac{G_{m2} + sC_cR_cG_{m2} - sC_c}{1 + sC_cR_c} \right)$$

Miller factor

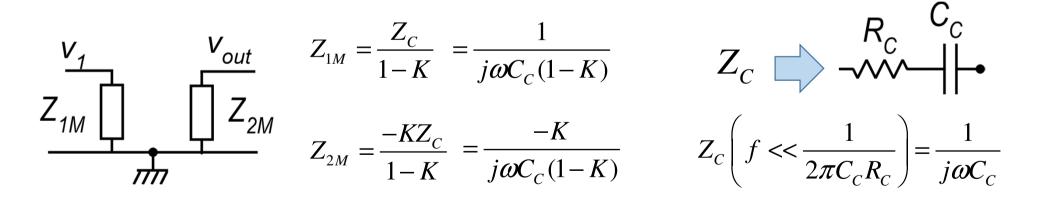


Transformation of the bridge impedance Z_C by the Miller Theorem

$$K = \frac{v_{out}}{v_1} = -ZG_{m2} \left(\frac{1 + sC_C \left(R_C - \frac{1}{G_{m2}} \right)}{1 + sC_C R_C} \right)$$

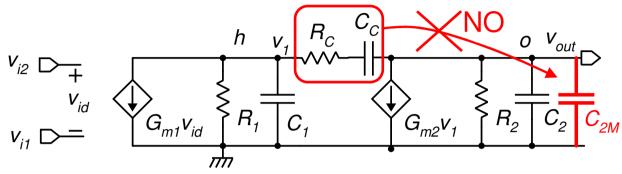


The low frequency limit of the K factor: $Z(f \rightarrow 0) = R_2$ $K(f \rightarrow 0) = -G_m, R_2$



Miller transformations: shifting the input pole to very low frequencies

Second effect of Pole Splitting: shifting the output pole to high frequencies



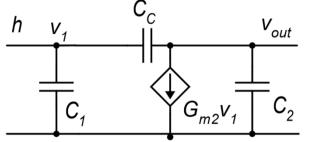
 ωC_{γ}

We cannot use the Miller theorem again, because the resulting pole would fall at frequencies where K is very different from **K(0)**.

At frequencies such that:

$$<< R_2$$
, $\frac{1}{\omega C_1} << R_1$ and still: $\frac{1}{\omega C_C} >> R_C$

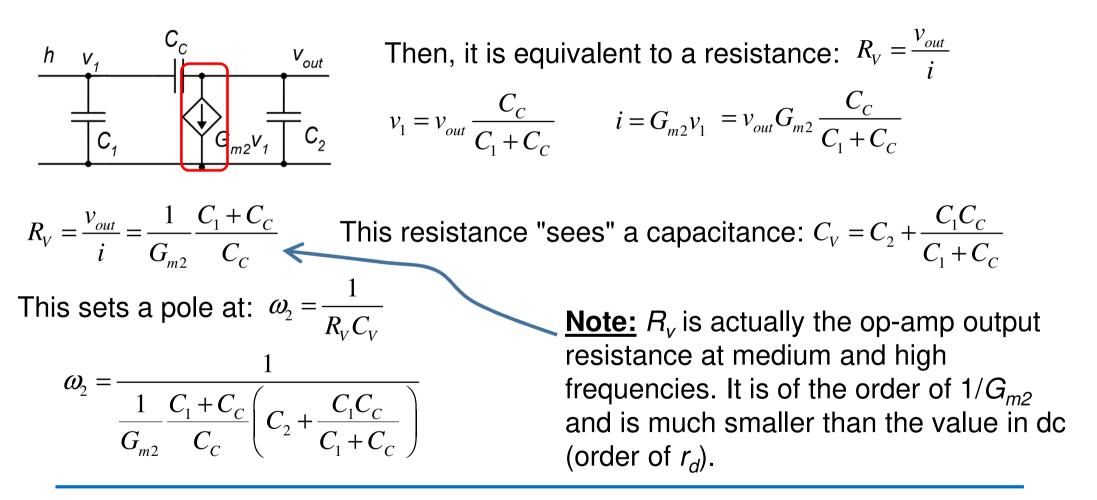
The equivalent circuit reduces to:



Current source $G_{m2}v_1$ is controlled by the voltage across it:

$$v_1 = v_{out} \frac{C_C}{C_1 + C_C}$$

Second effect of Miller Compensation: shifting the output pole to high frequencies



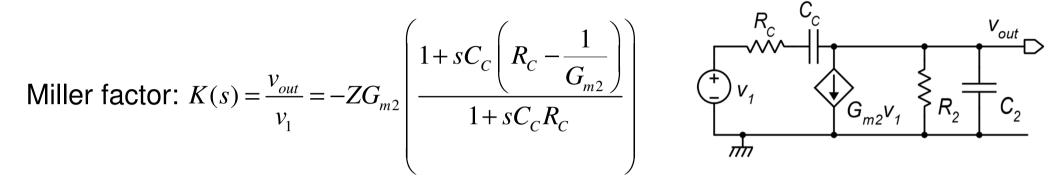
Second effect of Miller Compensation: shifting the output pole to high frequencies

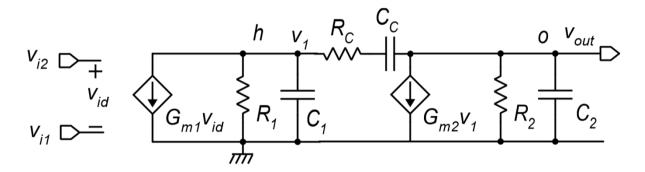
$$\omega_{2} = \frac{1}{R_{v}C_{v}} = \frac{1}{\frac{1}{G_{m2}} \frac{C_{1} + C_{c}}{C_{c}} \left(C_{2} + \frac{C_{1}C_{c}}{C_{1} + C_{c}}\right)} = \frac{G_{m2}}{\frac{C_{1}C_{2} + C_{c}C_{2} + C_{1}C_{c}}{C_{c}}}$$

$$\omega_{2} = \frac{G_{m2}}{\left(\frac{C_{1}C_{2}}{C_{c}} + C_{2} + C_{1}\right)} = \frac{G_{m2}}{(C_{1} + C_{2})\left(1 + \frac{1}{C_{c}} \cdot \frac{C_{1}C_{2}}{C_{1} + C_{2}}\right)} \qquad C_{s} = \frac{C_{1}C_{2}}{C_{1} + C_{2}} \qquad \text{Series of } C_{1}$$

$$\omega_{2} = \frac{G_{m2}}{(C_{1} + C_{2})\left(1 + \frac{C_{s}}{C_{c}}\right)}$$

Miller Factor and overall transfer function



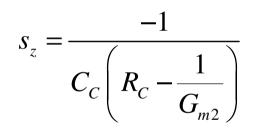


Factorizing A:
$$A = \frac{v_{out}}{v_{id}} = \frac{v_1}{v_{id}} \frac{v_{out}}{v_1} = \frac{v_1}{v_{id}} K(s)$$

The zero introduced by $R_C - C_C$

$$K(s) = \frac{v_{out}}{v_1} = -ZG_{m2} \left(\frac{1 + sC_C \left(R_C - \frac{1}{G_{m2}} \right)}{1 + sC_C R_C} \right)$$

There is a zero in K(s):

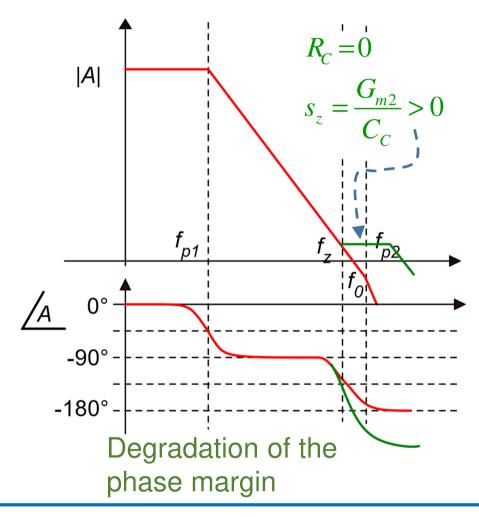


$$A = \frac{v_{out}}{v_{id}} = \frac{v_1}{v_{id}} \frac{v_{out}}{v_1} = \frac{v_1}{v_{id}} K(s)$$

If $R_C = 0$ $s_z = \frac{-1}{C_C \left(\frac{-1}{G_{m2}}\right)} = \frac{G_{m2}}{C_C} > 0$

This zero occurs also in the overall transferfunction of the amplifier (A). It cannot be cancelled by an equal zero, since an unstable pole (>0) would be required

Effects of the zero in the transfer function

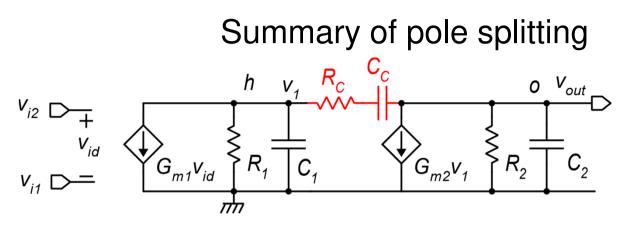


Thanks to R_c:

$$s_{z} = \frac{-1}{C_{C} \left(R_{C} - \frac{1}{G_{m2}} \right)}$$
$$R_{C} = \frac{1}{G_{m2}} \quad S_{z} \longrightarrow \infty$$

With this choice for R_C , we can eliminate the zero and cancel its bad effect on the phase delay.

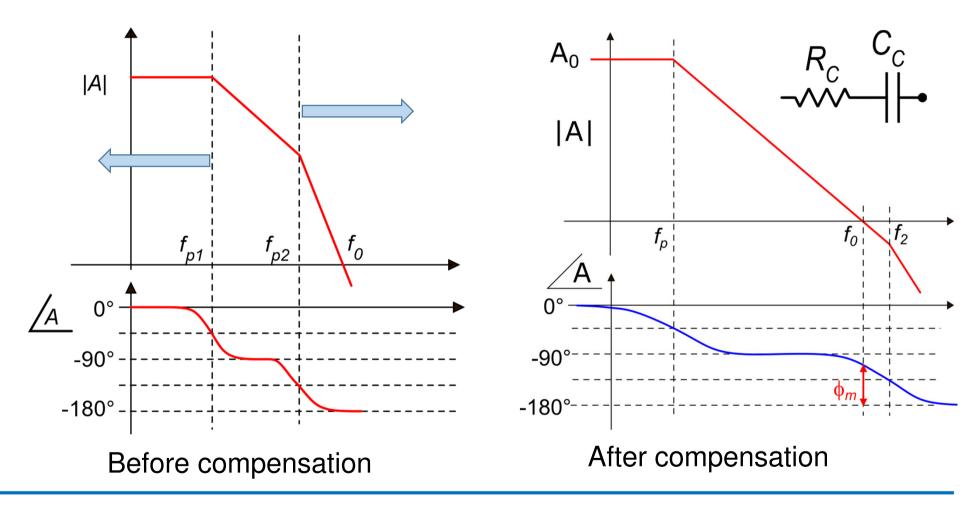
Other possible choices are possible: for $R_c>1/G_{m2}$ it is possible to change the positive zero into a negative one and use it to compensate f_{p2} .



Capacitor C_C introduces a feedback across the second stage that:

- 1. Puts an equivalent large capacitor $(C_C G_{m2} R_2 >> C_1)$ across the output resistance of the first stage (R_1) shifting the first pole back to very low frequencies
- 2. Reduces the output resistance (R_V) at medium/high frequencies from R_2 to a value close to $1/G_{m2}$. This shifts the output pole to much higher frequencies.
- **3.** Resistor R_c is significant only at high frequencies and "shapes" the zero, either cancelling it or turning it into a negative zero

Pole splitting, graphical view



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