# Periodic Steady State (PSS) Analysis

PSS is the equivalent of DC analysis but applied to periodic circuits: finds the periodic steady-state response of a circuit and evalutes the periodic operating point. The steady-state solution is then linearized for time-varying small-signal analysis as Periodic AC (PAC), Periodic Noise (PNOISE)…

Useful to study several number of circuits driven by periodic, large-signal excitations. Some examples:

- RF circuits: oscillators, mixers, PLL...

- Power Electronics circuits: dc-dc converters, rectifiers...

- Analog circuits: switched-capacitor amplifiers, chopper amplifiers…

# Periodic Steady State (PSS) Analysis

Need to find the solution of the following system equations:

$$\begin{cases} \dfrac{d}{dt}q(t,v) + j(t,v) = 0 \\ \quad v(0) - v(T) = 0 \end{cases}$$

q(t,v) represents the charges assembled at the respective nodes, j(t,v) represents the sources and the static part, T is the fundamental period

There are two PSS methods:

1. Harmonic Balance (Agilent ADS): frequency-domain method

2. Shooting Method (Cadence Spectre RF): time-domain method

# Harmonic Balance

- Steady-state solutions are approximated by finite Fourier series
- Frequency-domain linear analysis for the linear elements
- Time-domain analysis for non-linear elements, then transformed in the frequency domain
- Must solve system of K x N equations (K: number of harmonics in the Fourier series, N: number of nodes)

✓ Easily handles frequency-domain models (e.g. S-parameters)

X  Accuracy limited by the number of harmonics

X  Not suitable for simulating strongly nonlinear responses

# Shooting Method

- Try to solve iteratively: $v(0) - v(T) = 0$

- It computes a transient simulation from 0 to T and compares all voltage and currents at the start and end of the shooting interval

- It repeats for a second interval from T to 2T and so on, until it converges (or not…)

- We can adjust the parameter tstab to skip the initial "start-up" behavior

✓ Accuracy not limited by the number of harmonics

✓ Suitable for simulating strongly nonlinear responses

X  Doesn't handle frequency-domain models (e.g. S-parameters)

# PSS Parameters

- <u>PSS fundamental frequency</u>: fundamental frequency of the circuit and of all the periodic input sources. In the case of different frequencies of the periodic input sources, they must be multiple of the fundamental frequency

- <u>Number of harmonics</u>: contributes to the time step of the transient simulations and sets the truncation of the Fourier series representation of the periodic signals

- <u>tstab</u>: initial time for the stabilization of the circuit (can be automatically detected by the simulator)

# Periodic AC (PAC) Analysis

PAC is similar to AC analysis, except that the circuit is linearized around a periodically varying operating point. In this way, it is possible to analyze transfer-functions that include frequency translation.



$$H(j\omega; t) = \sum_{m=-\infty}^{+\infty} H_m(j\omega)e^{jm\omega_c t}$$

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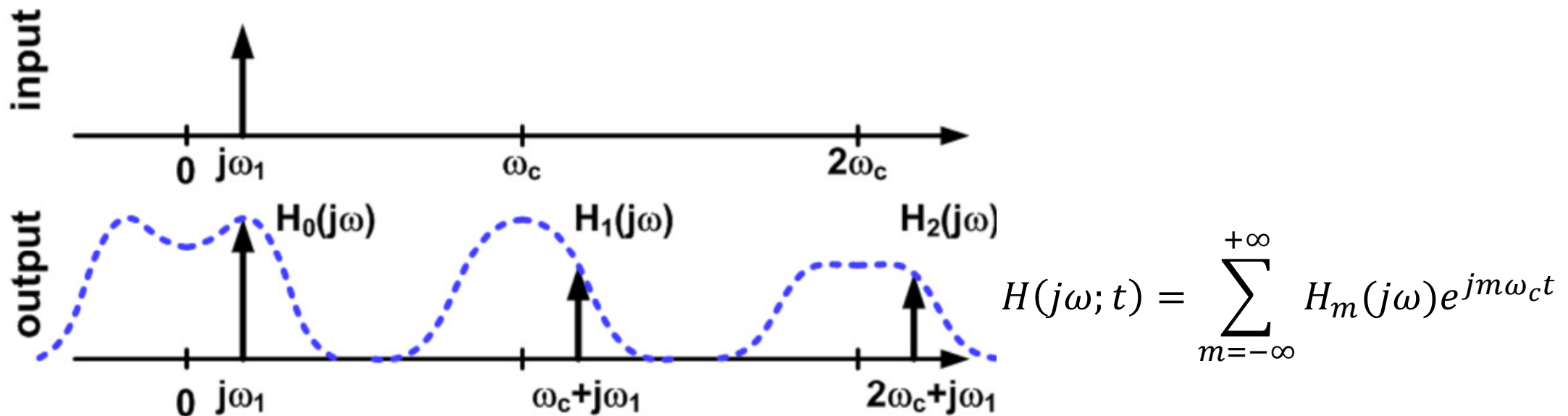
# PAC Parameters

- <u>PSS fundamental frequency</u>: same as indicated in PSS analysis
- <u>Start/stop frequency</u>: frequency range of the input small signal
- <u>Maximum sidebands</u>: number of replicas of the input signal at the output due to frequency translations (e.g. sampling, modulation…)

E.g.:
Sample&Hold
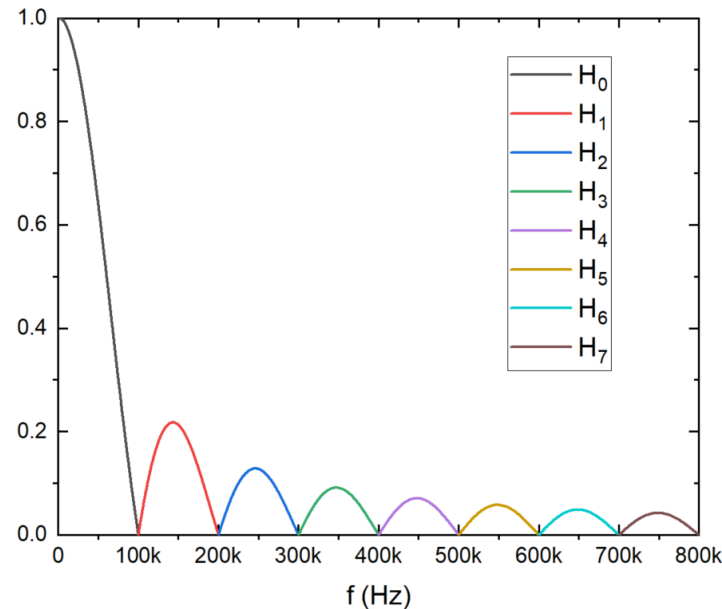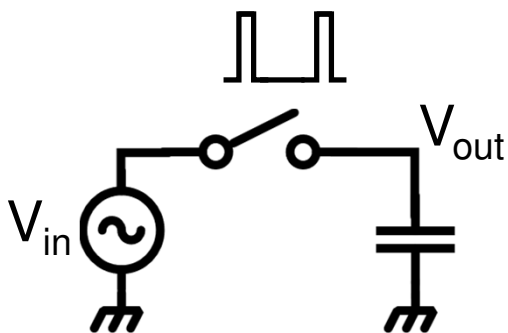


Fundamental Frequency: 100 kHz
Maximum Sideband: 7
Start/Stop Frequency: [1Hz/100kHz]

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# Periodic Noise (PNOISE) Analysis

PNOISE computes the frequency conversion effects as noise foldover, moreover it takes into account the time-varying operating point that acts ad a modulation for bias dependent noise sources. Noise sources can be modeled as periodically time-varying, also called cyclostationary noise.
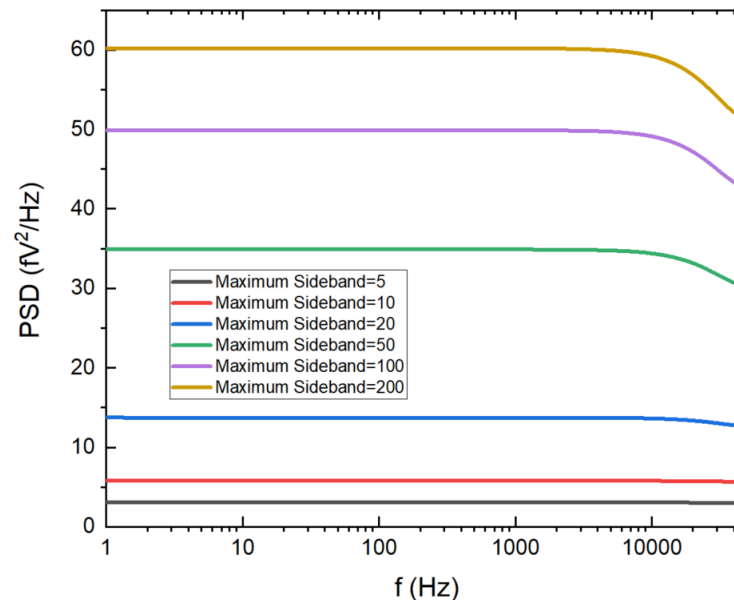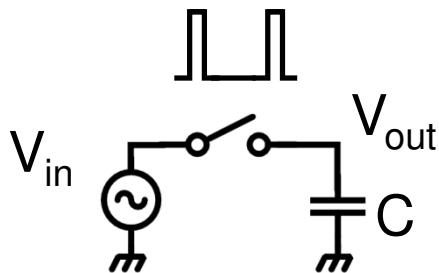
E.g. Modulated noise
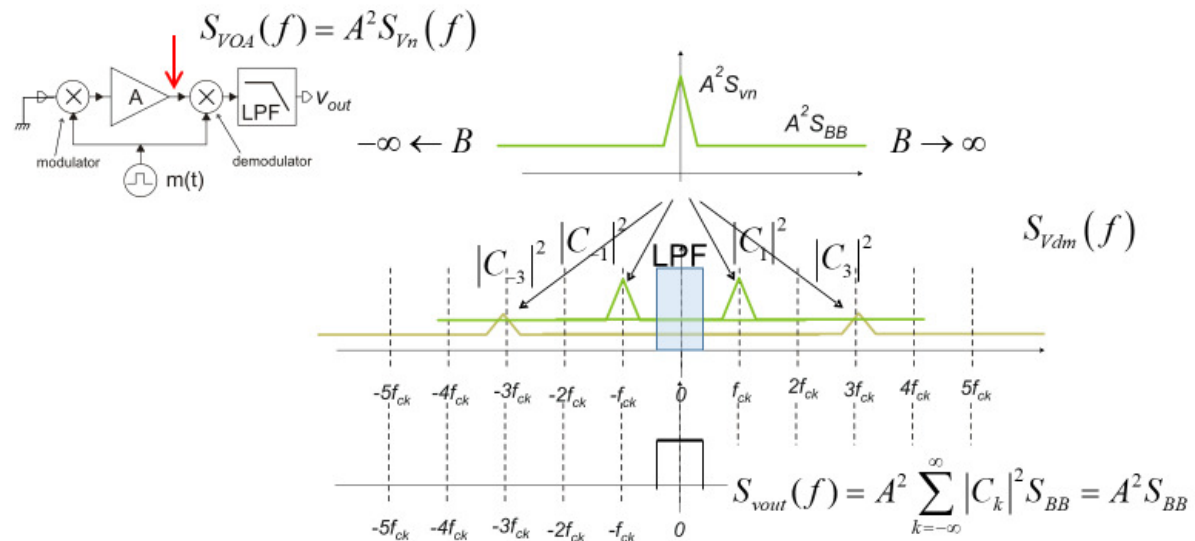
# PNOISE Parameters

- <u>PSS fundamental frequency</u>: same as indicated in PSS analysis
- <u>Start/stop frequency</u>: frequency range of the noise spectral density
- <u>Maximum sidebands</u>: number of noise replica
- <u>Noise type</u>: time average (single-sided spectrum, harmonic referred noise analysis) vs. time domain (strobed noise analysis)

E.g.:
Sample&Hold



Fundamental Frequency: 100 kHz
Start/Stop Frequency: [1Hz/50kHz]
C=1pF