# Floating Point Formats for Machine Learning 

IEEE Working Group P3109 interim report on 8-bit binary floating-point formats.

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Send questions and comments to the P3109 Secretary < jeffrey.sarnoff@ieee.org>.

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## Table of Contents

1. Introduction .....  3
2. Typographical conventions and notation .....  3
3. Values .....  4
4. Subnormals .....  5
5. Not a number ( NaN ) .....  5
6. Zero .....  6
7. Infinities ..... 6
8. Classification Operators ..... 7
9. Comparison Operators .....  7
10. Extremal Values ..... 9
Appendix A: Numerical Examples ..... 10
Appendix B: Value Tables ..... 11
Value table: binary8p3 ..... 12
Value table: binary8p4 ..... 13
Value table: binary8p5 ..... 14

## 1. Introduction

This document represents the results of discussions and decisions made by IEEE working group P3109, "Standard for Arithmetic Formats for Machine Learning". The Project Authorization Request (PAR) for P3109 defines the scope, need, and stakeholders as follows:

Scope of proposed standard: This standard defines a binary arithmetic and data format for machine learning-optimized domains. It also specifies the default handling of exceptions occurring in this arithmetic. This standard provides a consistent and flexible arithmetic framework optimized for Machine Learning Systems (MLS) in hardware and/or software implementations to minimize the work required to make MLS interoperable with each other as well as other dependent systems. This standard is aligned with the IEEE Std 754-2019 for Floating-Point Arithmetic.

Need for the Project: Machine Learning Systems have different arithmetic requirements from most other domains. Precisions tend to be lower, and accuracy is measured in dimensions other than just numerical (e.g. inference accuracy). Furthermore, Machine Learning Systems often are integrated into mission-critical and safety-critical systems. With no standards specifically addressing these needs, Machine Learning Systems are built with inconsistent expectations and assumptions that hinder the compatibility and reuse of machine learning hardware, software, and training data.

Stakeholders for the Standard: System developers, vendors, and users of machine learning applications across many industries and interests including but not limited to compute, storage, medical, telecommunications, e-commerce, fleet-management, automotive, robotics, and security.

The scope of this interim release is interchange formats only. The working group continues to deliberate on the specification of operations.

## 2. Typographical conventions and notation

## Bold text describes the decisions and specifications of this document.

Non-bold text is non-normative background material, typically providing rationale and arguments representing the discussions of the WG leading to a decision and specification.

This document specifies 8-bit floating-point interchange formats (binary formats) and associated operations. Binary formats are parameterized by their width, the number of bits spanned in memory (here, 8 ); and their precision ( $p$ ), the number of bits spanned by the true significand (one more than the number of explicit "mantissa" bits).

The formats defined herein shall be referred to as "binary8" formats, and further parametrized by precision $p$ yielding names "binary8pp".

For example, "binary8p3" is a format with 3 bits of precision, hence a 2-bit mantissa and a 5-bit exponent field.

## 3. Values

This section describes the set of values that a binary8 format shall represent. The universe of values in existing floating point usage encompasses some finite real numerical values, the nonfinite numerical values positive and negative infinity ( $-\operatorname{Inf}, \quad+\operatorname{Inf}$ ), the non-numeric not-a-number values ( $N a N, N a N_{1}, \ldots$ ), and negative zero ( -0 ). The value set for each binary 8 format specifies the set of values that are available in that format.

Each binary format shall be associated with a unique encoding. An 8-bit binary encoding is a mapping from 8-bit strings to values. Some of these mappings are included as an Appendix.

The four special values ( $0,+\operatorname{lnf},-\operatorname{lnf}, \mathrm{NaN}$ ) have encodings that are shared by all binary8 formats.
Table 1 - Encoding Special Values

| Value | Hexadecimal Encoding | Bit Sequence |
| :--- | :---: | :---: |
| Zero | $0 \times 00$ | 00000000 |
| Positive Infinity (+Inf) | $0 \times 7 F$ | 01111111 |
| Negative Infinity (-Inf) | $0 \times F F$ | 11111111 |
| Not a Number (NaN) | $0 \times 80$ | 10000000 |

The set of finite floating-point numbers representable with a binary format is determined by two parameters:

- $\quad p=$ the number of digits in the significand (precision)
- emax = the maximum exponent

IEEE-754 2019 includes the radix $b$ and emin in the list of format parameters. This document covers binary (radix 2) formats only. The parameter emin is determinable from other parameters, so is not a format-defining parameter.

The range of finite values represented by a given binary8 format is defined by the parameter emax. In IEEE-754, emax was consistently chosen across formats to be $2^{w-1}-1$, where $w$ is the exponent field width in bits. P3109 formats shall follow this convention. This choice has the following consequences:

- The binary8pp value sets are subsets of the IEEE-754 binary16 value set for $p>2$.
- The finite values are symmetrically distributed about 1: there are 63 encodings in the range $(0,1)$, and 63 encodings in the range $[1, \infty)$.

Table 2 - Parameters for Binary Formats*

| Parameter | binary8pp | binary8p5 | binary8p4 | binary8p3 | binary16 | binary32 | binary64 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $k$, storage width in bits | $\mathbf{8}$ | $\mathbf{8}$ | $\mathbf{8}$ | $\mathbf{8}$ | $\mathbf{1 6}$ | $\mathbf{3 2}$ | $\mathbf{6 4}$ |
| $p$, precision in bits | $\boldsymbol{p}$ | $\mathbf{5}$ | $\mathbf{4}$ | $\mathbf{3}$ | $\mathbf{1 1}$ | $\mathbf{2 4}$ | $\mathbf{5 3}$ |
| emax, max exponent | $\mathbf{2}^{8-\boldsymbol{p + 1}} \mathbf{- 1}$ | $\mathbf{3}$ | $\mathbf{7}$ | $\mathbf{1 5}$ | $\mathbf{1 5}$ | $\mathbf{1 2 7}$ | $\mathbf{1 0 2 3}$ |
|  |  |  |  |  |  |  |  |
| $w$, exponent field width | $8-p$ | 3 | 4 | 5 | 5 | 8 | 11 |
| bias, $E-e$ | $e m a x+1$ | 4 | 8 | 16 | 15 | 127 | 1023 |
| sign bit | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| $t$, significand field width | $p-1$ | 4 | 3 | 2 | 10 | 23 | 52 |

* Adapted from table 3.5 of IEEE-754 (2019), and extended to include proposed binary8 formats.


## 4. Subnormals

## Binary8 value sets shall include subnormals.

The IEEE-754 value sets include subnormals. A value with trailing significand field $m$ and exponent $e$ is interpreted as $1 . m \times 2^{e-b}$ except when all bits of the exponent bitfield are 0 , in which case, the value is $0 . m \times 2^{e-b+1}$.

When training models, it is common to represent near-zero values for gradients. Subnormal numbers induce equal quantization steps around zero; this expands the reach of binary8 trainable models. In statistical applications, the subnormal range is useful for uniform-like distributions, being uniform around zero. This also supports working with Gaussian-like distributions where numbers around zero are more probable.

## 5. Not a number (NaN)

## Binary8 value sets shall include exactly one NaN, which shall not signal.

Other floating point formats define several NaN values, denoted ( $\mathrm{NaN}, \mathrm{NaN}_{1}, \ldots$ ). NaNs are returned from operations with results outside the set of values. For example, $\operatorname{DIV}(0,0)$, or $\operatorname{ADD}(\operatorname{Inf},-\operatorname{Inf})$. Multiple NaN encodings are used in other formats to allow different exceptional conditions to be distinguished.

In the context of machine learning systems, uses of NaN include:

- Debugging of code running on the accelerator. In AI accelerators, exceptions may be difficult or expensive to convey back to user code, so it is common practice to allow NaN values to propagate through calculations in order to indicate that an error has occurred.
- Usage as a "notable value" indicator. In some datasets, for example tabular data, values may be missing. It is useful to use a value outside of the normal numeric range to indicate the position of these values. Particularly where memory usage is a concern, as may be expected in float8 applications, the use of a separate "mask" array, or a list of indices, imposes an extra memory overhead. In some cases, an Inf can be used as a missing value, but given the restricted range of float8, it is likely that infinity shall be used as a separate indicator of "larger/smaller than +/- MaxFloat".
- The use of multiple NaN payloads is not unknown in statistical code (e.g. the R system has NaN and N/A), but it is not widely used, and in the context of float8, multiple NaNs imposes either additional hardware complexity (using only a subset of the significand range), or a large reduction in encoding space (e.g. 8 codes for E5, 16 codes for E4, 32 codes for E3).


## 6. Zero

## Binary8 formats shall have exactly one zero. This zero value is non-negative.

The inclusion of negative zero would incur the cost of an additional code point. Given the decision to encode only a single NaN , placing that NaN at the negative zero code point enables the strictly positive and strictly negative number ranges to be symmetric.

A key rationale for inclusion of - 0 in IEEE- 754 was the consistent implementation of branch cuts in the atan 2 function [Kahan 1987]. Although the atan function is common in deep learning, it is used as an activation function, rather than a trigonometric operation, and the atan2 function is not known in deep learning applications. Furthermore, it is not expected that this standard shall define either atan or atan2.

A secondary rationale for inclusion of -0 is the hardware simplification offered by its presence in the implementation of sign/magnitude arithmetic. However, the existence of in-market implementations is evidence that the small hardware simplification has not been sufficient to balance the loss of one code point.

It might be considered that the use of integer comparisons in sorting would argue against the placing of NaN at the negative zero code point. For example, the JAX machine learning framework is known to sort using integer comparison [link]. However such sorting still requires $O(n)$ preprocessing and postprocessing steps to enable the use of twos-complement integer comparison, and already has special treatment of NaN and -0 , so eliminating -0 and placing NaN in the -0 position imposes negligible additional burden. As an aside, it is noted that sorting using comparison operations, as typically defined, is undefined in presence of NaN , however the existing practice is to sort NaN (e.g. using totalOrder) to the end of the array, and this remains permitted, at no additional cost.

## 7. Infinities

## Binary8 formats shall include positive and negative infinities.

This decision causes a reduction in dynamic range ( 252 values rather than 254 ), but offers improved numerical robustness in important machine learning use cases. Two generic classes of such usage are:

- mask values, for example, in Transformer models in machine learning, [ref].
- representation of overflow.

As illustrated in Appendix A, both usages are facilitated by the presence of infinity.

## 8. Classification Operators

Conforming implementations shall provide these classification predicates and the classifier function. The classification predicates and the classifier function shall not signal exceptions.

| predicate | Definition | predicate | definition |
| :--- | :--- | :--- | :--- |
| isZero | Iff $x$ is 0 | isNaN | Iff $x$ is NaN |
| isInfinite | iff $x$ is infinite | isFinite | Iff $x$ is zero, subnormal or normal |
| isNormal | Iff $x$ is normal | isSubnormal | Iff $x$ is subnormal |
| isSignMinus | Iff $x$ has a negative sign $^{1}$ |  |  |
| isCanonical | True $^{2}$ | isSignaling | False $^{3}$ |

Table 3: Classification Predicates
${ }^{1}$ isSignMinus( NaN ) is True: all binary8 formats encode NaN as $0 \times 80$ (0b10000000).
${ }^{2}$ There are no non-canonical binary8 interchange formats.
${ }^{3}$ All binary 8 formats have one NaN ; it does not signal.

The Classifier function
enum class $(x)$
NaN
Zero
positiveInfinity
positiveNormal
positiveSubnormal
negativeInfinity
negativeNormal
negativeSubnormal
end

## 9. Comparison Operators

## Conforming implementations shall provide these comparison operators and the total $\operatorname{Order}(x, y)$ function.

Comparison operators are two argument predicates and their negations that return \{ True, False \}. Comparisons shall not raise exceptions. Comparisons are either ordered or unordered. A comparison is unordered iff either argument is NaN . All other comparisons are ordered.

For $\{=,>, \geq,<, \leq, \lessgtr\}$, if any argument is NaN the result is False.
For $\{\neq, \ngtr, \not \geq, \not \subset, \nsubseteq, \nsubseteq\}$, if any argument is NaN the result is True.
Otherwise, the result of a comparison shall match the mathematical result.

## Table 4: Comparison Predicates and Negations

| math symbol | predicate true relations | math symbol | negation <br> true relations |
| :---: | :---: | :---: | :---: |
| $=$ | CompareEqual equal | \#, NOT = | CompareNotEqual less than, greater than, unordered |
| > | CompareGreater greater than | $\ngtr$, NOT > | CompareNotGreater less than, equal, unordered |
| $\geq$ | CompareGreaterEqual equal, greater than | $\geq$, NOT $\geq$ | CompareLessUnordered less than, unordered |
| < | CompareLess less than | *, NOT < | CompareNotLess greater than, equal, unordered |
| $\leq$ | CompareLessEqual less than, equal | \$, NOT $\leq$ | CompareGreaterUnordered greater than, unordered |
| $\leqslant$ | CompareOrdered less than, equal, greater than | \$, NOT $\$$ | CompareUnordered unordered |

## The totalOrder predicate

total $\operatorname{Order}(x, y)$ provides a total ordering over each binary8 format's value set. It shall not raise any exceptions. totalOrder $(x, y)$ shall return $\{$ True, False $\}$ in accord with the logic given below.

```
boolean totalOrder( }x,y
    if ! ( isNaN(x) || isNaN(y) )
            return compareLessEqual( }x,y\mathrm{ )
    else
            return (! isNaN(x)) || isNaN(y)|| true
        end
end
```

Logical operations used within totalOrder()
! is the logical negation operator: !true == false, !false == true.
|| is the short-circuiting, left-associative logical OR.

- if $a$ is true, $a \| b$ returns true without evaluating $b$.
- if a evaluates as false, $a|\mid b$ returns the evaluation of $b$.
- a || b || c evaluates as (a || b) || c.


## 10. Extremal Values

It is practical to offer extremal finite values for supported 8-bit binary interchange formats. Following IEEE 754-2019 naming patterns, we adopt: maxNormal(T), minNormal(T), minSubnormal(T) where $T$ is a binary8 format. For example: maxNormal(binary8p4) $==7 / 4^{*}\left(2^{\wedge} 7\right)$, minNormal(binary8p5) $==1 /\left(2^{\wedge} 3\right)$.

|  | maxNormal | minNormal | minSubnormal |
| :--- | :---: | :---: | :---: |
| binary8p3 | $3 / 2^{*}\left(2^{\wedge} 15\right)$ | $1 /\left(2^{\wedge} 15\right)$ | $1 /\left(2^{\wedge} 17\right)$ |
| binary8p4 | $7 / 4^{*}\left(2^{\wedge} 7\right)$ | $1 /\left(2^{\wedge} 7\right)$ | $1 /\left(2^{\wedge} 10\right)$ |
| binary8p5 | $15 / 8^{*}\left(2^{\wedge} 3\right)$ | $1 /\left(2^{\wedge} 3\right)$ | $1 /\left(2^{\wedge} 7\right)$ |
| binary8p6 | $31 / 16^{*}\left(2^{\wedge} 1\right)$ | $1 /\left(2^{\wedge} 1\right)$ | $1 /\left(2^{\wedge} 6\right)$ |

Table 5: Extremal Values

## Appendix A: Numerical Examples

## Mask Values

A common use for $\infty$ is to create masks, for example, in Transformer models in machine learning, [ref]. These values, assembled in mask matrix $M$ with values $M_{i j} \in\{0,-\infty\}$ are typically be added to computed values $A$, in a computation such as:

$$
\log (\operatorname{sum}(\exp (\tau *(A+M))))
$$

where $\tau$ is a "temperature" or "base" parameter [ref]. This calculation depends on the property that $\exp \left(\tau * A_{i j}-\infty\right)=0$. It is clear that where $M_{i j}$ is a large float (e.g. 480), then $\exp (-480)$ is an extremely small number, clearly much closer to zero than to any other value. However, careful implementations do not execute the calculation as written, and instead fuse the $\log (\operatorname{sum}(\exp (\boldsymbol{v})))$ operation into a single operation $\operatorname{logsumexp}(\boldsymbol{v})$, whose implementation makes use of the identity

$$
\operatorname{logsumexp}(\boldsymbol{v})=\operatorname{logsumexp}(\boldsymbol{v}-\max (\boldsymbol{v}))+\max (\boldsymbol{v})
$$

Without the "sticky" properties of Inf, this would produce incorrect answers. For example, in a format where MaxFloat=224 without Inf, and MaxFloat=240 with Inf:

$$
\operatorname{logsumexp}(\tau *[-224,-\infty]) \rightarrow \operatorname{logsumexp}(\tau *[0,-\infty])
$$

while

$$
\operatorname{logsumexp}(\tau *[-224,-240]) \rightarrow \operatorname{logsumexp}(\tau *[0,-16])
$$

If $\tau=1$ and all calculations are done in 8 -bit floating point, then the answer will be the same, as $\exp (-16)=0$, but if $\tau$ is small, or calculations are done in mixed precision, as is common with 8-bit floating point, the loss of "stickiness" shall silently yield unexpected answers. It is not expected that the full calculation shall be done in 8-bit floating point, but the subtraction of the maximum value (and computation of the maximum) might reasonably be in 8-bit floating point.

## Overflow to Infinity

A second use of infinity is to indicate overflow on conversion to the binary8 type. Existing implementations offer several behaviours on overflow: overflow to infinity, saturation to MaxFloat, and overflow to NaN. The existence of a code point for infinity allows any of these options to be implemented in a given instantiation, while removing the code point removes the possibility of implementing the first.

## Appendix B: Value Tables

Value tables mapping 8-bit strings to value sets are provided in this section.
A typical entry is of the form:

```
HEX BINARY = BINARY_FLOAT = DECIMAL
0x01 0_00000_01 = +0.b0.01^*2^-15 = 7.62939453125e-06
```

Where the fields are interpreted as follows:

| HEX | Hexadecimal encoding of the code point |
| :--- | :--- |
| BINARY | Binary expansion of the code point, with underscores separating sign_exponent_significand |
| BINARY_FLOAT | The precise float value as a binary fraction followed by $2^{\wedge} e$ with decimal exponent $e$ |
| DECIMAL | The decimal expansion of the value |

## Value table: binary8p3

| 0x00 $=0$-00000_00 |  |  |  |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| $\begin{aligned} & 0 \times 02=0 \_00000 \_10 \\ & 0 \times 03=0 \_00000 \_11 \end{aligned}$ |  |  |  |
|  |  |  |  |
| $0 \times 04=0 \_00001 \_00$$0 \times 05=000001$ |  |  |  |
|  |  |  |  |
| $0 \times 05=0 \_00001 \_01$$0 \times 06=0 \_00001 \_10$ |  |  |  |
| $0 \times 07=0 \_00001-11$$0 \times 08=000010-00$ |  |  |  |
|  |  |  |  |
| $0 \times 09=0{ }^{-} 000100^{-} 01$ |  |  |  |
| $\begin{aligned} & 0 \times 0 \mathrm{a}=0 \_00010 \_10 \\ & 0 \times 0 \mathrm{~b}=0 \_00010 \_11 \end{aligned}$ |  |  |  |
|  |  |  |  |
| $0 \times 0 b=0 \_00010 \_11$ |  |  |  |
| $0 \times 0 c=0 \_00011 \_00$ |  |  |  |
| $\begin{aligned} & 0 \times 0 \mathrm{~d}=0 \_00011 \_01 \\ & 0 \times 0 \mathrm{e}=0 \_00011 \_10 \end{aligned}$ |  |  |  |
| 0x0f = 0_00011_ ${ }^{11}$ |  |  |  |
| $\begin{aligned} & 0 \times 10=0 \_00100 \_00 \\ & 0 \times 11=0 \_00100 \_01 \end{aligned}$ |  |  |  |
|  |  |  |  |
| $\begin{aligned} & 0 \times 11=0 \_00100 \_01 \\ & 0 \times 12=0 \_00100 \_10 \end{aligned}$ |  |  |  |
| $\begin{aligned} & 0 \times 12=0 \_00100 \_10 \\ & 0 \times 13=0 \_00100 \_11 \end{aligned}$ |  |  |  |
|  |  |  |  |
| $0 \times 15=0 \_00101 \_01$ |  |  |  |
| $\begin{aligned} & 0 \times 15=0 \_00101 \_01 \\ & 0 \times 16=0 \_00101 \_10 \end{aligned}$ |  |  |  |
|  |  |  |  |
| $0 \times 18 \text { = 0_00110_00 }$ |  |  |  |
| $0 \times 19 \text { = 0_00110_01 }$ |  |  |  |
| $0 \times 1 \mathrm{a}=0 \_00110 \_10$ |  |  |  |
| $0 \times 1 b=0 \_00110 \_11$ |  |  |  |
|  |  |  |  |
| $0 \times 1 d=0 \_00111 \_01$ |  |  |  |
| $0 \times 1 \mathrm{e}=0 \_00111 \_10$ |  |  |  |
| $0 \times 1 f=0 \_00111 \_11$ |  |  |  |
|  |  |  |  |
| $0 \times 21 \text { = 0_01000_01 }$ |  |  |  |
| $0 \times 22=0 \_01000 \_10$ |  |  |  |
|  |  |  |  |
| $\begin{aligned} & 0 \times 23=0 \_01000 \_11 \\ & 0 \times 24=0 \_01001 \_00 \end{aligned}$ |  |  |  |
| $0 \times 24=0 \_01001 \_00$$0 \times 25=0 \_01001 \_01$ |  |  |  |
| $0 \times 25=0 \_01001 \_01$$0 \times 26=0 \_01001 \_10$ |  |  |  |
| $0 \times 26=0 \_01001 \_10$$0 \times 27=0 \_01001 \_11$ |  |  |  |
| $0 \times 27=0 \_01001 \_11$$0 \times 28=0 \_01010 \_00$ |  |  |  |
| $0 \times 28=0 \_01010 \_00$$0 \times 29=0 \_01010 \_01$ |  |  |  |
| $0 \times 29=0 \_01010 \_01$$0 \times 2 a=0 \_01010 \_10$ |  |  |  |
| $0 \times 2 \mathrm{a}=0 \_01010 \_10$$0 \times 2 \mathrm{~b}=0 \_01010 \_11$ |  |  |  |
| $0 \times 2 \mathrm{~b}=0 \_01010 \_11$$0 \times 2 \mathrm{c}=00101100$ |  |  |  |
| $0 \times 2 \mathrm{c}=0 \_01011 \_00$$0 \times 2 \mathrm{~d}=001011{ }^{\text {a }} 01$ |  |  |  |
| $0 \times 2 \mathrm{~d}=0 \_01011 \_01$$0 \times 2 \mathrm{e}=0$-01011_10 |  |  |  |
| $0 \times 2 \mathrm{f}=0 \_01011 \_{ }^{11}$ |  |  |  |
| 0x30 = 0_01100_00 |  |  |  |
| 0x31 = 0_01100_01 |  |  |  |
| 0x32 = 0_01100_10 |  |  |  |
|  |  |  |  |
| 0x34 $=0$ - 01101 _00 |  |  |  |
| $0 \times 34=0 \_01101 \_00$$0 \times 35=0 \_01101 \_01$ |  |  |  |
| 0x36 = 0_01101_10 |  |  |  |
|  |  |  |  |
| 0x37 $=0$ 0_01101_11 |  |  |  |
| 0x39 = 0_01110_01 |  |  |  |
| $0 \times 3 \mathrm{a}=0 \_01110 \_10$ |  |  |  |
| $0 \times 3 \mathrm{~b}=0 \_01110 \_11$ |  |  |  |
|  |  |  |  |
| 0x3c $=0$-01111-00 |  |  |  |
| $0 \times 3 \mathrm{e}=0 \_01111 \_10$ |  |  |  |
|  |  |  |  | $0 \times 02=0^{-} 00000 \_10=+0 \mathrm{~b} 0.10 * 2^{\wedge}-15=1.52588 \mathrm{e}-05$ $0 \times 03=0 \_00000 \_11=+0 b 0.11 * 2^{\wedge}-15=2.28882 e-05$ $0 \times 04=0 \_00001 \_00=+0 b 1.00 * 2^{\wedge}-15=3.05176 \mathrm{e}-05$ $0 \times 05=0 \_00001 \_01=+0 \mathrm{~b} 1.01 * 2^{\wedge}-15=3.8147 \mathrm{e}-05$

$0 \times 06=00000110=+0 \mathrm{~b} 1.10 * 2^{\wedge}-15=4.57764 \mathrm{e}-05$ $0 \times 07=0 \_00001 \_11=+0 b 1.11 * 2^{\wedge}-15=5.34058 \mathrm{e}-05$ $0 \times 08=0 \_00010 \_00=+0 b 1.00 * 2^{\wedge}-14=6.10352 \mathrm{e}-05$ $0 \times 09=0 \_00010 \_01=+0 b 1.01 * 2^{\wedge}-14=7.62939 \mathrm{e}-05$ $0 \times 0 \mathrm{a}=0 \_00010 \_10=+0 \mathrm{~b} 1.10 * 2^{\wedge}-14=9.15527 \mathrm{e}-05$ $0 \times 0 \mathrm{c}=\mathbf{0}^{-} 00011$ - $00=+0 \mathrm{~b} 1.00 * 2^{\wedge}-13=0.00012207$ $0 x 0 \mathrm{~d}=0 \_00011 \_01=+0 b 1.01 * 2^{\wedge}-13=0.000152588$ $0 \times 0 \mathrm{e}=0 \_00011 \_10=+0 \mathrm{~b} 1.10 * 2^{\wedge}-13=0.000183105$ $0 \times 10=0 \_00100 \_00=+0 b 1.00 * 2^{\wedge}-12=0.000244141$ $0 \times 11=0 \_00100 \_01=+0 b 1.01 * 2^{\wedge}-12=0.000305176$ $0 \times 13=0$ _00100_11 $=+0 \mathrm{~b} 1.11 * 2^{\wedge}-12=0.000427246$ $0 \times 14=0 \_00101 \_00=+0 b 1.00 * 2^{\wedge}-11=0.000488281$ $0 \times 15=0 \_00101 \_01=+0 b 1.01 * 2^{\wedge}-11=0.000610352$
$0 \times 16=0 \_00101 \_10=+0 b 1.10 * 2^{\wedge}-11=0.000732422$ $0 \times 17=0 \_00101 \_11=+0 b 1.11 * 2^{\wedge}-11=0.000854492$ $0 \times 18=0 \_00110 \_00=+0 b 1.00 * 2^{\wedge}-10=0.000976562$ $0 \times 19=0 \_00110 \_01=+0 b 1.01 * 2^{\wedge}-10=0.0012207$
$0 \times 1 a=0 \_00110 \_10=+0 b 1.10 * 2^{\wedge}-10=0.00146484$ $0 \times 1 \mathrm{~b}=0 \_00110 \_11=+0 \mathrm{~b} 1.11 * 2^{\wedge}-10=0.00170898$ $0 \times 1 \mathrm{c}=0 \_00111 \_00=+0 b 1.00 * 2^{\wedge}-9=0.00195312$ $0 \times 1 \mathrm{~d}=0 \_00111 \_01=+0 \mathrm{~b} 1.01 * 2^{\wedge}-9=0.00244141$
$0 \times 1 \mathrm{e}=0 \_00111 \_10=+0 \mathrm{~b} 1.10 * 2^{\wedge}-9=0.00292969$ $0 \times 1 \mathrm{f}=0 \_00111 \_11=+0 \mathrm{~b} 1.11 \star 2^{\wedge}-9=0.00341797$
$0 \times 20=0.01000 \_00=+0 b 1.00 * 2^{\wedge}-8=0.00390625$ $0 \times 21=0 \_01000 \_01=+0 b 1.01 * 2^{\wedge}-8=0.00488281$ $0 \times 23=0-01000-11=+0 b 1.11 * 2^{\wedge}-8=0.0068359$ $0 \times 24=0 \_01001 \_00=+0 b 1.00 * 2^{\wedge}-7=0.0078125$ $0 \times 25=0 \_01001 \_01=+0 b 1.01 * 2^{\wedge}-7=0.00976562$ $0 \times 26=0 \_01001 \_10=+0 b 1.10 * 2^{\wedge}-7=0.0117188$
$0 \times 27=0-0100111=+0 b 1.11 * 2^{\wedge-7}=0.0136719$ $0 \times 27=0 \_01001 \_11=+0 b 1.11 * 2^{\wedge}-7=0.0136719$ $0 \times 28=0 \_01010 \_00=+0 \mathrm{~b} 1.00 * 2^{\wedge}-6=0.015625$
$0 \times 29=0 \_01010 \_01=+0 \mathrm{~b} 1.01 * 2^{\wedge}-6=0.0195312$ $0 \times 2 \mathrm{a}=0_{-}^{-} 01010 \_10=+0 \mathrm{~b} 1.10 * 2^{\wedge}-6=0.0234375$ $0 \times 2 \mathrm{~b}=0 \_01010 \_11=+0 \mathrm{~b} 1.11 * 2^{\wedge}-6=0.0273438$ x2c = 0_01011_00 = +0b1.00*2^-5 = 0.03125 $0 \times 2 d=0 \_01011 \_01=+0 b 1.01 * 2^{\wedge}-5=0.0390625$
$0 \times 2 e=0 \_01011 \_10=+0 b 1.10 * 2^{\wedge}-5=0.046875$ $0 \times 2 \mathrm{f}=0 \_01011 \_11=+0 \mathrm{~b} 1.11 * 2^{\wedge}-5=0.0546875$
$0 \times 30=0 \_01100 \_00=+0 \mathrm{~b} 1.00 * 2 \wedge-4=0.0625$ x31 = 0_01100_01 = +0b1.01*2^-4 = 0.07812 $0 \times 33=0$ _01100_11 $=+0$ b1.11*2^-4 $=0.109375$ $\times 34=00110100=+0 b 1.00 * 2^{\wedge}-3=0.125$ $0 \times 35=0 \_01101 \_01=+0 b 1.01 * 2^{\wedge}-3=0.15625$ $0 \times 37=0_{-01101 \_11}^{-}=+0 b 1.11 * 2^{\wedge}-3=0.21875$ $0 \times 38=0 \_01110 \_00=+0 b 1.00 * 2^{\wedge}-2=0.25$ $0 \times 39=0 \_01110 \_01=+0 b 1.01 * 2^{\wedge}-2=0.312$ $0 \times 3 \mathrm{~b}=0 \_01110-11=+0 \mathrm{~b} 1.11 * 2^{\wedge}-2=0.4375$ $0 \times 3 \mathrm{c}=0 \_01111 \_00=+0 \mathrm{~b} 1.00 * 2^{\wedge}-1=0.5$ $0 \times 3 \mathrm{~d}=0 \_01111 \_01=+0 \mathrm{~b} 1.01 * 2^{\wedge}-1=0.625$ $0 \times 3 f=0 \_01111 \_11=+0 b 1.11 * 2^{\wedge}-1=0.875$
$0 \times 40=0 \_10000 \_00=+0 \mathrm{~b} 1.00 * 2^{\wedge} 0=1$
$0 \times 41=0 \_10000 \_01=+0 \mathrm{bb} 1.01 * 2^{\wedge} 0=1.25$
$0 \times 42=0 \_10000 \_10=+0 b 1.10 * 2^{\wedge} 0=1.5$ $0 \times 42=0 \_10000 \_10=+0 \mathrm{~b} 1.10 * 2 \wedge 0=1.5$ $0 \times 43=0 \_10000 \_11=+0 b 1.11 * 2 \wedge 0=1.75$ $0 \times 44=0 \_10001 \_00=+0 \mathrm{~b} 1.00 * 2 \wedge 1=2$ $0 \times 45=0 \_10001 \_01=+0 \mathrm{~b} 1.01 * 2 \wedge 1=2.5$ $0 \times 46=0 \_10001 \_10=+0 \mathrm{~b} 1.10 * 2 \wedge 1=3$ $0 \times 47=0 \_10001 \_11=+0 \mathrm{~b} 1.11 * 2 \wedge 1=3.5$ $0 \times 48=0 \_10010 \_00=+0 \mathrm{~b} 1.00 * 2 \wedge 2=4$ $0 \times 49=0 \_10010 \_01=+0 \mathrm{~b} 1.01 * 2^{\wedge} 2=5$ $0 \times 4 \mathrm{a}=0 \_10010 \_10=+0 \mathrm{~b} 1.10 * 2 \wedge 2=6$ $0 \times 4 \mathrm{~b}=0 \_10010 \_11=+0 \mathrm{~b} 1.11 * 2 \wedge 2=7$ $0 \times 4 \mathrm{c}=0 \_10011 \_00=+0 \mathrm{~b} 1.00 * 2 \wedge 3=8$ $0 \times 4 \mathrm{~d}=0 \_10011 \_01=+0 b 1.01 * 2 \wedge 3=10$ $0 \times 4 \mathrm{e}=0 \_10011 \_10=+0 \mathrm{~b} 1 \cdot 10 * 2 \wedge 3=12$ $0 \times 4 \mathrm{f}=0 \_10011 \_11=+0 \mathrm{~b} 1.11 * 2 \wedge 3=14$
$0 \times 50=0 \_10100 \_00=+0 b 1.00 * 2 \wedge 4=16$ $0 \times 51=0 \_10100 \_01=+0 b 1.01 * 2 \wedge 4=20$ $0 \times 52=0 \_10100 \_10=+0 b 1 \cdot 10 * 2 \wedge 4=24$ $0 \times 53=0 \_10100 \_11=+0 b 1.11 * 2^{\wedge} 4=28$ $0 \times 54=0 \_10101 \_00=+0 b 1.00 * 2 \wedge 5=32$ $0 \times 55=0 \_10101 \_01=+0 b 1.01 * 2^{\wedge} 5=40$ $0 \times 56=0 \_10101 \_10=+0 b 1 \cdot 10 * 2^{\wedge} 5=48$ $0 \times 57=0 \_10101 \_11=+0 b 1.11 * 2 \wedge 5=56$ $0 \times 58=0 \_10110 \_00=+0 b 1.00 * 2 \wedge 6=64$ $0 \times 59=0 \_10110 \_01=+0 b 1.01 * 2 \wedge 6=80$ $0 \times 5 \mathrm{a}=0 \_10110 \_10=+0 \mathrm{~b} 1.10 * 2 \wedge 6=96$ $0 \times 5 \mathrm{~b}=0 \_10110 \_11=+0 \mathrm{~b} 1.11 * 2 \wedge 6=112$ $0 \times 5 \mathrm{c}=0$ _10111_00 = +0b1.00*2^7 $=128$ $0 \times 5 \mathrm{~d}=0 \_10111 \_01=+0 \mathrm{~b} 1.01 * 2^{\wedge} 7=160$ $0 \times 5 \mathrm{e}=0 \_10111 \_10=+0 \mathrm{~b} 1.10 * 2 \wedge 7=192$ $0 \times 5 \mathrm{f}=0 \_10111 \_11=+0 \mathrm{~b} 1.11 * 2 \wedge 7=224$
$0 \times 60=0 \_11000 \_00=+0 b 1.00 * 2 \wedge 8=256$ $0 \times 61=0 \_11000 \_01=+0 \mathrm{~b} 1.01 * 2 \wedge 8=320$ $0 \times 62=0 \_11000 \_10=+0 \mathrm{~b} 1 \cdot 10 * 2 \wedge 8=384$ $0 \times 63=0 \_11000 \_11=+0 \mathrm{~b} 1.11 * 2 \wedge 8=448$ $0 \times 64=0 \_11001 \_00=+0 b 1.00 * 2 \wedge 9=512$ $0 \times 65=0 \_11001 \_01=+0 b 1.01 * 2 \wedge 9=640$ $0 \times 66=0 \_11001 \_10=+0 \mathrm{~b} 1 \cdot 10 * 2 \wedge 9=768$ $0 \times 67=0 \_11001 \_11=+0 b 1.11 * 2 \wedge 9=896$ $0 \times 68=0 \_11010 \_00=+0 b 1.00 * 2 \wedge 10=1024$ $0 \times 69=0 \_11010 \_01=+0 b 1.01 * 2^{\wedge} 10=1280$ $0 \times 6 \mathrm{a}=0 \_11010 \_10=+0 \mathrm{~b} 1 \cdot 10 * 2 \wedge 10=1536$ $0 \mathrm{x} 6 \mathrm{~b}=0 \_11010 \_11=+0 \mathrm{~b} 1.11 * 2 \wedge 10=1792$ $0 \times 6 \mathrm{c}=0$ _ $11011 \_00=+0 \mathrm{~b} 1.00 * 2 \wedge 11=2048$ $0 \times 6 \mathrm{~d}=0 \_11011 \_01=+0 \mathrm{~b} 1.01 * 2^{\wedge} 11=2560$ $0 \times 6 \mathrm{e}=0 \_11011 \_10=+0 \mathrm{~b} 1.10 * 2^{\wedge} 11=3072$ $0 \times 6 \mathrm{f}=0 \_11011 \_11=+0 \mathrm{~b} 1.11 * 2^{\wedge} 11=3584$
$0 \times 70=0 \quad 1110000=+0 b 1.00 * 2^{\wedge} 12=4096$ $0 \times 71=0 \_11100 \_01=+0 b 1.01 * 2^{\wedge} 12=5120$ $0 \times 72=0 \_11100 \_10=+0 b 1.10 * 2^{\wedge} 12=6144$ $0 \times 73=0 \_11100 \_11=+0 b 1.11 * 2 \wedge 12=7168$ $0 \times 74=0 \_11101 \_00=+0 \mathrm{~b} 1.00 * 2 \wedge 13=8192$ $0 \times 75=0 \_11101 \_01=+0 b 1.01 * 2^{\wedge} 13=10240$ $0 \times 76=0 \_11101 \_10=+0$ b1.10*2^13 $=12288$ $0 \times 77=0 \_11101 \_11=+0 b 1.11 * 2^{\wedge} 13=14336$ $0 \times 78=0 \_11110 \_00=+0 b 1.00 * 2^{\wedge} 14=16384$ $0 \times 79=0 \_11110 \_01=+0 b 1.01 * 2^{\wedge} 14=20480$ $0 \times 7 \mathrm{a}=0 \_11110 \_10=+0 \mathrm{~b} 1.10 * 2 \wedge 14=24576$ $0 \times 7 \mathrm{~b}=0$ _ $11110 \_11=+0 \mathrm{~b} 1.11 * 2^{\wedge} 14=28672$ $0 \times 7 \mathrm{c}=0 \_11111 \_00=+0 \mathrm{~b} 1.00 * 2 \wedge 15=32768$ $0 \times 7 \mathrm{~d}=0 \_11111 \_01=+0 \mathrm{~b} 1.01 * 2^{\wedge} 15=40960$ $0 x 7 \mathrm{e}=0$ _11111_10 $=+0 \mathrm{~b} 1.10 *$ 2^ $^{\wedge} 15=49152$ $0 \times 7 \mathrm{f}=0 \_11111 \_11=+\mathrm{Inf}$

$0 \mathrm{xc} 0=1 \_10000 \_00=-0 \mathrm{~b} 1.00 * 2^{\wedge} 0=-1$
$0 \times \mathrm{xc} 1=1 \_10000 \_01=-0 \mathrm{~b} 1.01 * 2^{\wedge} 0=-1.25$
$0 x c 2=1 \_10000 \_10=-0 b 1.10 * 2 \wedge 0=-1.5$
$0 \mathrm{xc} 3=1 \_10000 \_11=-0 \mathrm{~b} 1.11 * 2 \wedge 0=-1.75$
$0 \mathrm{xc} 4=1 \_10001 \_00=-0 \mathrm{~b} 1.00 * 2^{\wedge} 1=-2$
$0 \mathrm{xc} 5=1 \_10001 \_01=-0 \mathrm{~b} 1.01 * 2 \wedge 1=-2.5$
$0 \mathrm{xc} 6=1 \_10001 \_10=-0 \mathrm{~b} 1.10 * 2 \wedge 1=-3$
$0 \mathrm{xc} 7=1 \_10001 \_11=-0 \mathrm{~b} 1.11 * 2^{\wedge} 1=-3.5$
$0 \mathrm{xc} 8=1 \_10010 \_00=-0 \mathrm{~b} 1.00 * 2 \wedge 2=-4$
$0 x c 9=1 \_10010 \_01=-0 b 1.01 * 2 \wedge 2=-5$
$0 x c a=1 \_10010 \_10=-0 b 1 \cdot 10 * 2^{\wedge} 2=-6$
$0 x \mathrm{cb}=1 \_10010 \_11=-0 b 1.11 * 2 \wedge 2=-7$
$0 \mathrm{xcc}=1 \_10011 \_00=-0 \mathrm{~b} 1.00 * 2 \wedge 3=-8$
$0 \mathrm{xcd}=1 \_10011 \_01=-0 \mathrm{~b} 1.01 * 2^{\wedge} 3=-10$
$0 x c e=1 \_10011 \_10=-0 b 1 \cdot 10 * 2 \wedge 3=-12$
$0 x c f=1 \_10011 \_11=-0 b 1.11 * 2 \wedge 3=-14$
$0 \times d 0=1 \_10100 \_00=-0 b 1.00 * 2 \wedge 4=-16$
$0 \times \mathrm{d} 1=1 \_10100 \_01=-0 \mathrm{~b} 1.01 * 2^{\wedge} 4=-20$
$0 x d 2=1 \_10100 \_10=-0 b 1 \cdot 10 * 2 \wedge 4=-24$
$0 \times d 3=1 \_10100 \_11=-0 b 1.11 * 2 \wedge 4=-28$
$0 \times \mathrm{xd} 4=1 \_10101 \_00=-0 \mathrm{~b} 1.00 * 2^{\wedge} 5=-32$
$0 \times \mathrm{xd} 5=1 \_10101 \_01=-0 \mathrm{~b} 1.01 * 2^{\wedge} 5=-40$
$0 x d 6=1_{-} 10101 \_10=-0 b 1 \cdot 10 * 2^{\wedge} 5=-48$
$0 \times d 7=1 \_10101 \_11=-0 b 1 \cdot 11 * 2^{\wedge} 5=-56$
$0 x d 8=1 \_10110 \_00=-0 \mathrm{~b} 1.00 * 2 \wedge 6=-64$
$0 x d 9=1 \_10110 \_01=-0 b 1.01 * 2^{\wedge} 6=-80$
$0 x d a=1 \_10110 \_10=-0 b 1 \cdot 10 * 2 \wedge 6=-96$ $0 \mathrm{xdb}=1 \_10110 \_11=-0 \mathrm{~b} 1.11 * 2^{\wedge} 6=-112$ $0 x d c=1 \_10111 \_00=-0 b 1.00 * 2^{\wedge} 7=-128$ $0 x d d=1 \_10111 \_01=-0 b 1.01 * 2^{\wedge} 7=-160$ $0 x d e=1 \_10111 \_10=-0 b 1 \cdot 10 * 2^{\wedge} 7=-192$ $0 x d f=1 \_10111 \_11=-0 b 1.11 * 2^{\wedge} 7=-224$
$0 x e 0=1 \_11000 \_00=-0 b 1.00 * 2 \wedge 8=-256$ $0 x e 1=1 \_11000 \_01=-0 b 1.01 * 2^{\wedge} 8=-320$ $0 x e 2=1 \_11000 \_10=-0 b 1 \cdot 10 * 2 \wedge 8=-384$ $0 x e 3=1 \_11000 \_11=-0 b 1.11 * 2^{\wedge} 8=-448$ $0 x e 4=1 \_11001 \_00=-0 b 1.00 * 2 \wedge 9=-512$ $0 x e 5=1 \_11001 \_01=-0 b 1.01 * 2^{\wedge} 9=-640$ $0 x e 6=1 \_11001 \_10=-0 b 1.10 * 2 \wedge 9=-768$ $0 x e 7=1 \_11001 \_11=-0 b 1.11 * 2^{\wedge} 9=-896$ $0 x \mathrm{xe} 8=1 \_11010 \_00=-0 \mathrm{~b} 1.00 * 2^{\wedge} 10=-1024$ $0 \times \mathrm{xe} 9=1 \_11010 \_01=-0 \mathrm{~b} 1.01 * 2 \wedge 10=-1280$ $0 x e a=1 \_11010 \_10=-0 b 1 \cdot 10 * 2^{\wedge} 10=-1536$ 0 xeb $=1 \_11010 \_11=-0 b 1.11 * 2^{\wedge} 10=-1792$ $0 \mathrm{xec}=1 \_11011 \_00=-0 \mathrm{~b} 1.00 * 2 \wedge 11=-2048$ $0 \times \mathrm{xed}=1 \_11011 \_01=-0 \mathrm{~b} 1.01 * 2^{\wedge} 11=-2560$ 0 xee $=1 \_11011 \_10=-0 b 1 \cdot 10 * 2^{\wedge} 11=-3072$ 0 xef $=1 \_11011 \_11=-0 b 1 \cdot 11 * 2^{\wedge} 11=-3584$
$0 x f 0=1 \_11100 \_00=-0 b 1.00 * 2^{\wedge} 12=-4096$ $0 \times f 1=1 \_11100 \_01=-0 b 1.01 * 2^{\wedge} 12=-5120$ $0 x f 2=1 \_11100 \_10=-0 b 1 \cdot 10 * 2^{\wedge} 12=-6144$ $0 \times f 3=1 \_11100 \_11=-0 b 1.11 * 2^{\wedge} 12=-7168$ $0 \times f 4=1 \_11101 \_00=-0 b 1.00 * 2 \wedge 13=-8192$ $0 \times f 5=1 \_11101 \_01=-0 b 1.01 * 2 \wedge 13=-10240$ $0 \times f 6=1 \_11101 \_10=-0 b 1.10 * 2^{\wedge} 13=-12288$ $0 \times f 7=1 \_11101 \_11=-0 b 1.11 * 2^{\wedge} 13=-14336$ $0 \times f 8=1 \_11110 \_00=-0 \mathrm{~b} 1.00 * 2 \wedge 14=-16384$ $0 \times f 9=1 \_11110 \_01=-0 b 1.01 * 2 \wedge 14=-20480$ $0 \times \mathrm{xfa}=1 \_11110 \_10=-0 \mathrm{~b} 1.10 *$ 2^ $^{\wedge} 14=-24576$ $0 \times \mathrm{fb}=1_{-11110 \_11}=-0 \mathrm{~b} 1.11 *$ 2^14 $^{\wedge}=-28672$ $0 \times f \mathrm{c}=1 \_11111 \_00=-0 \mathrm{~b} 1.00 * 2^{\wedge} 15=-32768$ $0 \times f d=1 \_11111 \_01=-0 \mathrm{~b} 1.01 * 2^{\wedge} 15=-40960$ $0 \times f e=1 \_11111 \_10=-0 b 1 \cdot 10 * 2^{\wedge} 15=-49152$ $0 \times \mathrm{xff}=1 \_11111 \_11=-\operatorname{Inf}$

## Value table: binary8p4

| $0 \times 00=0.0000 \_000=+0 \mathrm{bO} 0.000 * 2^{\wedge}-7$ | $0 \times 40=0 \_1000 \_000=+0 b 1.000 * 2^{\wedge} 0=1$ | 0x80 $=1 \_0000$ _000 $=$ NaN | $0 \times 00=1 \_1000 \_000=-0 b 1.000 * 2 \wedge 00-1$ |
| :---: | :---: | :---: | :---: |
| 0x01 = 0_0000_001 $=+0 \mathrm{~b} 0.001 * 2^{\wedge}-7=0.000976562$ | $0 \times 41=0 \_1000 \_001=+0 \mathrm{bl} 1.001 * 2 \wedge 0=1.125$ | $0 \times 81=1 \_0000 \_001=-0 b 0.001 * 2 \wedge-7=-0.000976562$ | $0 \mathrm{xc} 1=1 \_1000 \_001=-0 \mathrm{bl} 1.001 * 2 \wedge 0=-1.125$ |
| $0 \times 02=0 \_0000 \_010=+$ bbo. $010 * 2 \wedge-7=0.00195312$ | $0 \times 42=0 \_1000 \_010=+0 \mathrm{bl}$. $010 * 2 \wedge 0=1.25$ | $0 \times 82=1 \_0000 \_010=-0 \mathrm{bb} .010 * 2 \wedge-7=-0.00195312$ | $0 \mathrm{xc} 2=1 \_1000 \_010=-0 \mathrm{~b} 1.010 \times 2 \wedge 0=-1.25$ |
| $0 \times 03=0 \_0000 \_011=+0 \mathrm{bo} 0011 * 2^{\wedge}-7=0.00292969$ | $0 \times 43=0{ }^{1000 \_011}=+0 \mathrm{bl} 1.011 * 2 \wedge 0=1.375$ | $0 \times 83=1 \_0000 \_011=-0 \mathrm{bo} 0.011 * 2^{\wedge}-7=-0.00292969$ | $0 \mathrm{xc} 3=111000 \_011=-0 \mathrm{bl} 1.011 * 2 \wedge 0=-1.375$ |
| 0x04 $=0$ _0000_100 $=+0 \mathrm{bo} .100 * 2^{\wedge}-7=0.00390625$ | $0 \times 44=0 \_1000 \_100=+0 b 1.100 * 2 \wedge 0=1.5$ | $0 \times 84=1 \_0000 \_100=-0 \mathrm{bo.100*2} \mathrm{\wedge}-7=-0.00390625$ | 0xc4 $=1$ 1 ${ }^{1000}{ }^{100}=-0 \mathrm{bl} 1.100 * 2 \wedge 0=-1.5$ |
| Ox05 = 0_0000_101 = +0bo.101*2^-7 = 0.00488281 | $0 \times 45=0{ }^{1000 \_101}=+0 \mathrm{bl} 1.101 * 2 \wedge 0=1.625$ | 0x85 = 1_0000_101 = -0bo.101*2^-7 =-0.00488281 | 0xc5 = 1_1000_101 $=-0 \mathrm{bl} 1.101 * 2^{\wedge} 0=-1.625$ |
| $0 \times 06=0 \_0000 \_110=+0 \mathrm{bO} .110 * 2 \wedge-7=0.00585938$ | 0x46 $=0$ _ 1000 _ $110=+0 \mathrm{bl} 1110 * 2 \wedge 00=1.75$ | $0 \times 86=1 \_0000 \_110=-0 \mathrm{bo} 0.110 * 2^{\wedge}-7=-0.00585938$ | $0 \mathrm{xc} 6=1 \_1000 \_110=-0 \mathrm{bl} 1.110 * 2 \wedge 0=-1.75$ |
| $0 \times 07=0 \_0000 \_111=+0 \mathrm{bo} .111 * 2 \wedge-7=0.00683594$ | $0 \times 47=0 \_1000 \_111=+0 b 1.111 * 2 \wedge 0=1.875$ | $0 \times 87=1 \_0000 \_111=-0 \mathrm{bb} .111 * 2^{\wedge}-7=-0.00683594$ | Oxc7 $=1 \_1000 \_111=-0 b 1.111 * 2 \wedge 0=-1.875$ |
| 0x08 $=0$ _0001_000 $=+0 b 1.000 * 2^{\wedge}-7=0.0078125$ | 0x48 $=0$ _1001_000 $=+0 \mathrm{bl} 1.000 \times 2 \wedge 1$ | $0 \times 88=1 \_0001 \_000=-0 b 1.000 * 2 \wedge-7=-0.0078125$ | 0xc8 $=1$ 1 1001 -000 $=-0 b 1.000 * 2 \wedge 1=-2$ |
| 0x09 = 0_0001_001 $=+0 \mathrm{bl} 1.001 * 2 \wedge-7=0.00878906$ | $0 \times 49=0 \_1001 \_001=+0 b 1.001 * 2 \wedge 1=2.25$ | 0x89 = 1_0001_001 $=-0 \mathrm{bl} 1.001 * 2^{\wedge}-7=-0.00878906$ | 0xc9 = 1_1001_001 $=-0 \mathrm{bl} .001 * 2 \wedge 1=-2.25$ |
| 0x0a $=0$ _0001_010 $=+0 \mathrm{bl} 1.010 * 2 \wedge-7=0.00976562$ | $0 \times 4 \mathrm{a}=0 \_1001 \_010=+0 \mathrm{bl} .010 * 2 \wedge 1=2.5$ | $0 \times 8 \mathrm{a}=1 \_0001 \_010=-0 \mathrm{bl} 1.010 * 2^{\wedge}-7=-0.00976562$ | Oxca $=1$ 1 ${ }^{1001}$-010 $=-0 \mathrm{bl} 1.010 * 2 \wedge 11=-2.5$ |
| Ox0b $=0$ _0001_011 $=+0 b 1.011 * 2 \wedge-7=0.0107422$ | $0 \times 4 \mathrm{~b}=0$-1001_011 $=+0 \mathrm{bl} 1.011 * 2 \wedge 11=2.75$ | $0 \times 8 \mathrm{~b}=1 \_0001 \_011=-0 \mathrm{bl} .011 * 2 \wedge-7=-0.0107422$ | $0 \mathrm{xcb}=1 \_1001$ - $011=-0 \mathrm{bl} 1.011 * 2 \wedge 1=-2.75$ |
| Ox0c $=0$ _0001_100 $=+0 b 1.100 * 2 \wedge-7=0.0117188$ | 0x4c $=0{ }^{1001}{ }^{100}=+0 b 1.100 * 2 \wedge 1$ | $0 \times 8 \mathrm{c}=1$ 1_0001_100 $=-0 \mathrm{bl} 1.100 * 2 \wedge-7=-0.0117188$ |  |
| Ox0d $=0 \_0001$ _101 $=+0 \mathrm{b1.101*2} \mathrm{\wedge-7}=0.0126953$ | x4d $=0$ _1001_101 $=+0{ }^{\text {d }} 1.101 * 2 \wedge 1=3.25$ | $0 \times 8 \mathrm{~d}=1$-0001_101 $=-0 \mathrm{bl} 1.101 * 2 \wedge-7=-0.0126953$ | Oxcd $=1$ 1 1001 _101 $=-0 \mathrm{bb1.101*2} \mathrm{\wedge 1}=-3.25$ |
| Ox0e $=0 \_0001 \_110=+0 b 1.110 * 2 \wedge-7=0.0136719$ | $0 \times 4 \mathrm{e}=0 \_1001 \_110=+0 \mathrm{bl} 1.110 * 2 \wedge 1=3.5$ | $0 \times 8 \mathrm{e}=1 \_0001 \_110=-0 \mathrm{bl} 1.110 * 2^{\wedge}-7=-0.0136719$ |  |
| Ox0f $=0 \_0001 \_111=+0 b 1.111 * 2^{\wedge}-7=0.0146484$ | $0 \times 4 \mathrm{f}=0{ }^{1001 \_111}=+0 \mathrm{~b} 1.111 * 2 \wedge 1=3.75$ | $0 \times 8 \mathrm{f}=1 \_0001 \_111=-0 \mathrm{bl} 1111 * 2^{\wedge}-7=-0.0146484$ | $0 \mathrm{xcf}=1 \_1001 \_111=-0 \mathrm{bl} 1.111 * \wedge^{\wedge} 1=-3.75$ |
| $0 \times 10=0 \_0010 \_000=+0 \mathrm{bl} 1.000 * 2^{\wedge}-6=0.015625$ | *50 $=0$ _ ${ }^{1010 \_000}=+0 \mathrm{bl} 1.000 \times 2 \wedge 2$ | $0 \times 90=1 \_0010 \_000=-0 b 1.000 * 2^{\wedge}-6=-0.015625$ | $0 \times \mathrm{xdO}=1 \_1010 \_000=-0 \mathrm{bl} 1.000 \times 2 \wedge 2=-4$ |
| $0 \times 11=0 \_0010 \_001=+0 b 1.001 * 2^{\wedge}-6=0.0175781$ | $0 \times 51=0 \_1010 \_001=+0 \mathrm{bl} 1.001 * 2 \wedge 2=4.5$ | $0 \times 91=1 \_0010 \_001=-0 b 1.001 * 2 \wedge-6=-0.0175781$ | $0 \mathrm{xd1}=1 \_{ }^{1010}$ _001 $=-0 \mathrm{bl} 1.001 * 2 \wedge 2=-4.5$ |
| $0 \times 12=0 \_0010 \_010=+0 b 1.010 * 2 \wedge-6=0.0195312$ | 52 $=0$ _1010_010 $=+0 \mathrm{bl} 1.010 * 2 \wedge 2$ | $0 \times 92=1 \_0010 \_010=-0 b 1.010 * 2 \wedge-6=-0.0195312$ | $0 \times \mathrm{xd2}=1 \_1010 \_010=-0 b 1.010 \times 2 \wedge 2=-5$ |
| $0 \times 13=0 \_0010 \_011=+0 b 1.011 * 2^{\wedge}-6=0.0214844$ | $0 \times 53=0 \_1010 \_011=+0 \mathrm{bl} 1.011 * 2 \wedge 2=5.5$ | $0 \times 93=1 \_0010 \_011=-0 b 1.011 * 2 \wedge-6=-0.0214844$ | $0 \mathrm{xd3}=1 \_{ }^{1010}{ }^{0} 011=-0 \mathrm{bl} 1.011 * 2 \wedge 2=-5.5$ |
| $0 \times 14=0 \_0010{ }^{100}=+0 b 1.100 * 2^{\wedge}-6=0.0234375$ | $0 \times 54=0{ }^{1010 \_100}=+0 \mathrm{bl} 1.100 * 2^{\wedge} 2$ | $0 \times 94=1 \_0010 \_100=-0 b 1.100 * 2 \wedge-6=-0.0234375$ |  |
| $0 \times 15=0 \_0010$ _101 $=+0$ b1.101*2^-6 $=0.0253906$ | $5=0{ }^{1010}{ }^{101}=+0 \mathrm{bl} 1.101 * 2 \wedge 2=6.5$ | $0 \times 95=1 \_0010{ }^{101}=-0 \mathrm{bl} 1.101 * 2^{\wedge}-6=-0.0253906$ | Oxd5 $=1 \_1010{ }_{-} 101=-0 \mathrm{bb} 1.101 * 2 \wedge 2=-6.5$ |
| $0 \times 16=0 \_0010{ }^{110}=+0 b 1.110 * 2^{\wedge}-6=0.0273438$ | $0 \times 56=0{ }^{1010 \_110}=+0$ b1.110*2^2 | $0 \times 96=1 \_0010{ }^{110}=-0 \mathrm{bl} 1.110 * 2 \wedge-6=-0.0273438$ | $0 \times \mathrm{d} 6=1{ }^{1010} \mathbf{l}^{110}=-0 \mathrm{bl} 1.110 \times 2 \wedge 2=-7$ |
| $0 \times 17=0 \_0010{ }^{111}=+0 b 1.111 * 2 \wedge-6=0.0292969$ | $0 \times 57=0 \_1010 \_111=+0 \mathrm{bl} 1.111 * 2 \wedge 2=7.5$ | $0 \times 97=1 \_0010 \_111=-0 b 1.111 * 2 \wedge-6=-0.0292969$ | $0 \mathrm{xd7}=1$ 1010_111 $=-0 \mathrm{bl} 1111 * 2 \wedge 2=-7.5$ |
| $0 \times 18=0 \_0011 \_000=+0 b 1.000 * 2^{\wedge}-5=0.03125$ | $0 \times 58=0{ }^{1011}$ - $000=+0 \mathrm{bl} 1.000 * 2^{\wedge} 3=8$ | 0x98 = 1_0011_000 $=-0 \mathrm{bl} 1.000 * 2^{\wedge}-5=-0.03125$ | $0 \times \mathrm{xd8}=1 \_1011 \_000=-0 \mathrm{bl} 1.000 \times 2 \wedge 3=-8$ |
| $0 \times 19=0 \_0011 \_001=+0 b 1.001 * 2^{\wedge}-5=0.0351562$ | 0x59 = 0_1011 ${ }^{\text {a }} 001=+0 \mathrm{bl}$. 001 * | $0 \times 99=1 \_0011$ _001 $=-0 \mathrm{bl} 1.001 * 2 \wedge-5=-0.0351562$ | $0 \times \mathrm{xd} 9=1 \_1011$-001 $=-0 \mathrm{bl} 1.001 \times 2 \wedge 3=-9$ |
| $0 \times 1 \mathrm{la}=0 \_0011 \_010=+0 b 1.010 * 2 \wedge-5=0.0390625$ | $0 \times 5 \mathrm{a}=0 \_1011 \_010=+0 \mathrm{bl} 1.010 \times 2 \wedge 3=10$ | $0 \times 9 \mathrm{a}=1 \_0011$-010 $=-0 \mathrm{bl} 1.010 * 2 \wedge-5=-0.0390625$ | 0xda $=1 \_1011 \_010=-0 b 1.010 * 2 \wedge 3=-10$ |
| $0 \times 1 \mathrm{~b}=0 \_0011 \_011=+0 b 1.011 * 2 \wedge-5=0.0429688$ | $0 \times 5 \mathrm{~b}=0{ }^{1011} \mathbf{0}^{011}=+0 \mathrm{~b} 1.011 * 2 \wedge 3=11$ | 0x9b $=1$ 1_0011_011 $=-0 \mathrm{bl} 1.011 * 2 \wedge-5=-0.0429688$ | $0 \mathrm{xdb}=1 \_1011 \_011=-0 \mathrm{bl} .011 * 2 \wedge 3=-11$ |
| Ox1c $=0 \_0011 \_100=+0 \mathrm{bb} 1.100 * 2^{\wedge}-5=0.046875$ | $0 \times 5 \mathrm{c}=0 \_1011 \_100=+0 \mathrm{bl} 100 \times 2 \wedge 3=12$ | 0x9c $=1 \_0011$ - $100=-0 b 1.100 * 2 \wedge-5=-0.046875$ | Oxdc = 1_1011_100 = -0b1.100*2^3 $=-12$ |
| 0x1d $=0$ _0011_101 $=+0 b 1.101 * 2 \wedge-5=0.0507812$ | $0 \times 5 \mathrm{~d}=0{ }^{1011} \mathbf{l}^{101}=+0 \mathrm{bl} 101 * \wedge^{\wedge} 3=13$ | $0 \times 9 \mathrm{~d}=1 \_0011{ }^{101}=-0 \mathrm{bl} 1.101 * 2^{\wedge}-5=-0.0507812$ | Oxdd $=1 \_1011$ - $101=-0 b 1.101 * 2 \wedge 3=-13$ |
| 0x1e $=0 \_0011 \_110=+0 b 1.110 * 2 \wedge-5=0.0546875$ | $0 \times 5 \mathrm{e}=0{ }^{1011 \_110}=+0 \mathrm{~b} 1.110{ }^{2}$ ^3 $=14$ | $0 \times 9 \mathrm{e}=1 \_0011$ 110 $=-0 \mathrm{bl} 1.110 * 2 \wedge-5=-0.0546875$ | 0xde $=1 \_1011 \_110=-0 b 1.110 * 2 \wedge 3=-14$ |
| $0 \times 1 \mathrm{f}=0 \_0011 \_111=+0 b 1.111 * 2 \wedge-5=0.0585938$ | $0 \times 5 \mathrm{f}=0{ }^{1011} \mathbf{l}^{111}=+0 \mathrm{b1} .111 * 2 \wedge 3$ | $0 \times 9 \mathrm{f}=1 \_0011 \_111=-0 \mathrm{bl} 1111 * 2 \wedge-5=-0.0585938$ | Oxdf = 1_1011_111 = -0b1.111*2^3 = -15 |
| $0 \times 20=0 \_0100 \_000=+0 b 1.000 * 2^{\wedge}-4=0.0625$ | $60=0 \_1100 \_000=+0 b 1.000 * 2 \wedge 4=16$ | 0xa0 $=1 \_0100 \_000=-0 b 1.000 * 2^{\wedge}-4=-0.0625$ | Oxee $=1 \_1100 \_000=-0 b 1.000 * 2 \wedge 4=-16$ |
| $0 \times 21=0 \_0100 \_001=+0 b 1.001 * 2^{\wedge}-4=0.0703125$ | $0 \times 61=0 \_1100 \_001=+0 b 1.001 * 2 \wedge 4=18$ | $0 \times \mathrm{a} 1=1 \_0100 \_001=-0 b 1.001 * 2^{\wedge}-4=-0.0703125$ | $0 \mathrm{xe} 1=1 \_1100 \_001=-0 \mathrm{bl} 1.001 * 2 \wedge 4=-18$ |
| $0 \times 22=0 \_0100 \_010=+0 \mathrm{~b} 1.010 * 2^{\wedge}-4=0.078125$ | $0 \times 62=0 \_1100 \_010=+0 b 1.010 \times 2 \wedge 4=20$ | 0xa2 $=1 \_0100 \_010=-0 b 1.010 * 2 \wedge-4=-0.078125$ | $0 \mathrm{xe2}=1 \_1100 \_010=-0 \mathrm{bl} 1.010 * 2 \wedge 4=-20$ |
| $0 \times 23=0 \_0100 \_011=+0 b 1.011 * 2 \wedge-4=0.0859375$ | $0 \times 63=0 \_1100 \_011=+0 b 1.011 * 2 \wedge 4=22$ | $0 \times$ a3 $=1 \_0100 \_011=-0 b 1.011 * 2^{\wedge}-4=-0.0859375$ | 0xe3 $=1 \_1100 \_011=-0 b 1.011 * 2 \wedge 4=-22$ |
| $0 \times 24=0 \_0100 \_100=+0 \mathrm{bl} 1.100 * 2^{\wedge}-4=0.09375$ | $0 \times 64=0 \_1100 \_100=+0 b 1.100 * 2 \wedge 4=24$ | $0 \times \mathrm{xa} 4=1 \_0100 \_100=-0 \mathrm{bl} 1.100 * 2 \wedge-4=-0.09375$ | $0 \mathrm{xe} 4=1 \_1100 \_100=-0 \mathrm{bl} \cdot 100 * 2 \wedge 4=-24$ |
| 0x25 $=0$ _0100_101 $=+0 \mathrm{~b} 1.101 * 2^{\wedge}-4=0.101562$ | 0_1100_101 = +0b1.101*2^4 $=26$ | 0xa5 $=1$-0100_101 $=-0 \mathrm{bl} 1.101 * 2 \wedge-4=-0.101562$ | 0xe5 = 1_1100_101 = -0b1.101*2^4 $=-26$ |
| $0 \times 26=0 \_0100 \_110=+0 \mathrm{bb} 1.110 * 2 \wedge-4=0.109375$ | $\times 66=0 \_1100 \_110=+0 b 1.110 * 2$ | 0xa6 $=1$ _ 0100 _ $110=-0 b 1.110 * 2 \wedge-4=-0.109375$ | 0xe6 $=1 \_1100 \_110=-0 b 1.110 * 2^{\wedge} 4=-28$ |
| $0 \times 27=0 \_0100 \_111=+0 b 1.111 * 2^{\wedge}-4=0.117188$ | $0 \times 67=0 \_1100 \_111=+0 b 1.111 * 2 \wedge 4=30$ | 0xa7 $=1$ _0100_111 $=-0 \mathrm{bl} 1111 * 2 \wedge-4=-0.117188$ | $0 \mathrm{xe7}=1 \_1100 \_111=-0 \mathrm{bl} 1111 * 2 \wedge 4=-30$ |
| $0 \times 28=0 \_0101 \_000=+0 b_{1} .000 * 2^{\wedge}-3=0.125$ | $0 \times 68=0 \_1101 \_000=+0 b 1.000 * 2 \wedge 5=32$ | 0xa8 $=1 \_0101 \_000=-0 b 1.000 * 2 \wedge-3=-0.125$ | 0xe8 $=1 \_1101 \_000=-0 b 1.000 * 2^{\wedge} 5=-32$ |
| $0 \times 29=0 \_0101 \_001=+0 \mathrm{bl} 1.001 * 2 \wedge-3=0.140625$ | 0x69 = 0_1101_001 = +0b1.001*2^ | 0xa9 = 1_0101_001 = -0b1.001*2^-3 $=-0.140625$ | 0xe9 = 1_1101_001 $=-0 \mathrm{bl} 1.001 * 2 \wedge 5=-36$ |
| $0 \times 2 \mathrm{a}=0$-0101_010 $=+0 \mathrm{bl} 1.010 * 2 \wedge-3=0.15625$ | 0x6a $=0 \_1101 \_010=+0 b 1.010 \times 2 \wedge 5=40$ | (xaa $=1 \_0101 \_010=-0 b 1.010 * 2 \wedge-3=-0.15625$ | Oxea $=1 \_1101 \_010=-0 b 1.010 * 2 \wedge 5=-40$ |
| $0 \times 2 \mathrm{~b}=0 \_0101 \_011=+0 \mathrm{~b} 1.011 * 2^{\wedge}-3=0.171875$ | $0 \times 6 \mathrm{~b}=0 \_1101 \_011=+0 \mathrm{bl} .011 * 2 \wedge 5=44$ | $0 \mathrm{xab}=1 \_0101 \_011=-0 \mathrm{bl} 1.011 * 2 \wedge-3=-0.171875$ | $0 \mathrm{xeb}=1 \_1101 \_011=-0 \mathrm{bl} .011 * 2 \wedge 5=-44$ |
| 0x2c $=0$ _0101_100 $=+0$ b1.100*2^-3 $=0.1875$ | $0 \times 6 \mathrm{c}=0$-1101_100 $=+0 \mathrm{bl} 1.100 * 2$ | Oxac $=1 \_0101$ - $100=-0 b 1.100 * 2 \wedge-3=-0.1875$ | Oxec $=1 \_1101 \_100=-0 b 1.100 * 2^{\wedge} 5=-48$ |
| 0x2d $=0$ _0101_101 $=+0 \mathrm{bl} 1.101 * 2^{\wedge}-3=0.203125$ | 0x6d = 0_1101_101 = +0b1.101*2 | 0xad $=1$-0101_101 $=-0 \mathrm{bl} 1.101 * 2$ ^-3 $=-0.203125$ | 0xed = 1_1101_101 $=-0 \mathrm{bl} 1.101 * 2 \wedge 5=-52$ |
| $0 \times 2 \mathrm{e}=0 \_0101 \_110=+0 \mathrm{bl} 1.110 * 2 \wedge-3=0.21875$ | $0 \times 6 \mathrm{e}=0 \_1101 \_110=+0 \mathrm{bl} 1110 \times 2 \wedge 5=56$ | Oxae $=1 \_0101 \_110=-0 b 1.110 * 2 \wedge-3=-0.21875$ | Oxee $=1 \_1101 \_110=-0 b 1.110 * 2 \wedge 5=-56$ |
| $0 \times 2 \mathrm{f}=0 \_0101 \_111=+0 \mathrm{~b} 1.111 * 2^{\wedge}-3=0.234375$ | $0 \times 6 \mathrm{f}=0{ }^{1101 \_} \mathbf{l}^{111}=+0 \mathrm{bl} 1111 \times 2 \wedge 5=60$ | Oxaf $=1 \_0101 \_111=-0 b 1.111 * 2 \wedge-3=-0.234375$ | Oxef $=1 \_1101 \_111=-0 b 1.111 * 2 \wedge 5=-60$ |
| $0 \times 30=0 \_0110 \_000=+0 b 1.000 * 2^{\wedge}-2=0.25$ | 0x70 $=0$ _1110_000 $=+0 \mathrm{bl} 1.000 \times 2 \wedge 6=64$ | $0 \times x \mathrm{~b} 0=1 \_0110 \_000=-0 b 1.000 * 2^{\wedge}-2=-0.25$ | Oxf0 $=1 \_1110 \_000=-0 b 1.000 * 2 \wedge 6=-64$ |
| $0 \times 31=0 \_0110 \_001=+0 b 1.001 * 2^{\wedge}-2=0.28125$ | $0 \times 71=0 \_1110 \_001=+0 b 1.001 * 2 \wedge 6=72$ | $0 \times \mathrm{xb1}=1$ _0110_001 $=-0 \mathrm{bl} 1.001 * 2 \wedge-2=-0.28125$ | Oxf1 $=1 \_1110 \_001=-0 b 1.001 * 2 \wedge 6=-72$ |
| $0 \times 32=0 \_0110 \_010=+0 b 1.010 * 2 \wedge-2=0.3125$ | 0_1110_010 = +0b1.010*2^6 | Oxb2 $=1$ _0110_010 $=-0 \mathrm{bl} 1.010 \times \wedge^{\wedge}-2=-0.3125$ | Oxf2 $=1 \_1110 \_010=-0 b 1.010 * 2 \wedge 6=-80$ |
| $0 \times 33=0 \_0110 \_011=+0 b 1.011 * 2 \wedge-2=0.34375$ | $0 \times 73=0 \_1110 \_011=+0 b 1.011 * 2 \wedge 6=88$ | 0xb3 $=1 \_0110 \_011=-0 \mathrm{bl} 1.011 * 2 \wedge-2=-0.34375$ | $0 \mathrm{Off3}=1 \_1110 \_011=-0 \mathrm{bl} .011 * 2 \wedge 6=-88$ |
| 0x34 $=000110 \_100=+0 b 1.100 * 2 \wedge-2=0.375$ | $0 \times 74=0 \_1110 \_100=+0 b 1.100 * 2 \wedge 6=96$ | $0 \mathrm{xb4}=1 \_0110 \_100=-0 \mathrm{bb} 1.100 * 2 \wedge-2=-0.375$ | $0 \times \mathrm{xf4}=1 \_1110 \_100=-0 \mathrm{bl} 1.100 * 2^{\wedge} 6=-96$ |
| $0 \times 35=0 \_0110 \_101=+0 b 1.101 * 2 \wedge-2=0.40625$ | $0 \times 75=0 \_1110 \_^{101}=+0 \mathrm{bl} 1.101 * 2 \wedge 6=104$ | Oxb5 $=1$ _0110_101 $=-0 \mathrm{bl} 1.101 * 2 \wedge-2=-0.40625$ | Oxf5 $=$ 1_1110_101 $=-0 \mathrm{bb} 1.101 * 2 \wedge 6=-104$ |
| $0 \times 36=0 \_0110{ }^{110}=+0 b 1.110 * 2 \wedge-2=0.4375$ | +0b1. | 0xb6 $=1$ _0110_110 $=-0 b 1.110 * 2^{\wedge}-2=-0.4375$ | $0 \times \mathrm{xf6}=1$ 1 ${ }^{1110} \mathbf{-}^{110}=-0 \mathrm{bl} 1110 * 2 \wedge 6=-112$ |
| $0 \times 37=0 \_0110 \_111=+0 \mathrm{~b} 1.111 * 2^{\wedge}-2=0.46875$ | $0 \times 77=0 \_1110 \_111=+0 b 1.111 * 2 \wedge 6=120$ | Oxb7 = 1_0110_111 $=-0 \mathrm{bl} 1.111 * 2 \wedge-2=-0.46875$ | $0 \times \mathrm{ff7}=1$ - ${ }^{1110} \mathrm{C}^{111}=-0 \mathrm{bl} 1.111 * 2 \wedge 6=-120$ |
| $0 \times 38=0 \_0111 \_000=+0 \mathrm{bl} 1.000 * 2 \wedge-1=0.5$ | $0 \times 78=0 \_1111 \_000=+0 b 1.000 * 2 \wedge 7=128$ | 0xb8 $=1 \_0111$ _000 $=-0 \mathrm{bl} 1.000 \times 2 \wedge-1=-0.5$ |  |
| $0 \times 39=0 \_0111 \_001=+0 b 1.001 * 2 \wedge-1=0.5625$ | $0 \times 79=0 \_1111 \mathbf{C l}^{001}=+0 b 1.001 * 2 \wedge 7=$ | Oxb9 $=1 \_0111 \_001=-0 b 1.001 * 2^{\wedge}-1=-0.5625$ | 0xf9 = 1_ ${ }^{1111}$-001 $=-0 \mathrm{bl} 1.001 * 2 \wedge 7=-144$ |
| 0x3a $=0 \_0111 \_010=+0 b_{1} .010 * 2^{\wedge}-1=0.625$ | $0 \times 7 \mathrm{a}=0 \_1111 \_010=+0 \mathrm{bl}$. $010 * 2 \wedge 7=160$ | 0xba $=1 \_0111 \_010=-0 b 1.010 * 2 \wedge-1=-0.625$ | $0 \times \mathrm{xfa}=1 \_{ }^{1111} \mathrm{C}^{010}=-0 \mathrm{bl} 1.010 \times 2 \wedge 7=-160$ |
| $0 \times 3 \mathrm{~b}=0 \_0111 \_011=+0 b 1.011 * 2^{\wedge}-1=0.6875$ | $0 \mathrm{x} 7 \mathrm{~b}=0 \_1111 \_011=+0 \mathrm{bl} .011 * 2 \wedge 7=176$ | Oxbb $=1 \_0111 \_011=-0 b 1.011 * 2^{\wedge}-1=-0.6875$ | $0 \times \mathrm{fb}=1 \_{ }^{1111} \mathrm{C}^{011}=-0 \mathrm{bl} 1.011 * 2 \wedge 7=-176$ |
| $0 \times 3 \mathrm{c}=0$-0111_100 $=+0 \mathrm{~b} 1.100 * 2^{\wedge}-1=0.75$ | $0 \mathrm{x} 7 \mathrm{c}=0 \_1111 \mathrm{l} 100=+0 \mathrm{bl} 1.100 * 2^{\wedge} 7=192$ | $\mathrm{oxbc}=1 \_0111 \_100=-0 \mathrm{bl} 1.100 * 2^{\wedge}-1=-0.75$ | $0 \times \mathrm{xfc}=$ 1- $^{1111} \mathrm{l}^{100}=-0 \mathrm{bb} 1.100 * 2 \wedge 7=-192$ |
|  | 0_1111_101 $=+0 \mathrm{bl} 1.101 \times \wedge^{\wedge} 7=208$ | Oxbd $=1 \_0111101=-0 b 1.101 * 2^{\wedge}-1=-0.8125$ | $0 \times \mathrm{fd}=$ 1_ $^{1111} \mathrm{l}^{101}=-0 \mathrm{bl} 1.101 * 2^{\wedge} 7=-208$ |
| $0 \times 3 \mathrm{e}=0 \_0111 \mathrm{l}^{110}=+0 \mathrm{bl} 1.110 * 2^{\wedge}-1=0.875$ | $0 \times 7 \mathrm{l}=0{ }^{1111}{ }^{110}=+0 \mathrm{bl} 1.110 * 2 \wedge 7=224$ | Oxbe $=1 \_0111 \_110=-0 \mathrm{bl} 1.110 * 2^{\wedge}-1=-0.875$ | $0 \times \mathrm{xfe}=1_{-}^{1111} \mathrm{l}^{110}=-0 \mathrm{bl} 1.110 * 2 \wedge 7=-224$ |
| $0 \times 3 \mathrm{f}=0 \_0111 \_111=+0 b 1.111 * 2^{\wedge}-1=0.9375$ | $0 \times 7 \mathrm{f}=0 \_1111{ }^{111}=+$ Inf | $0 \times \mathrm{xbf}=1 \_0111 \_111=-0 \mathrm{bl} 1111 * 2^{\wedge}-1=-0.9375$ | $0 \times \mathrm{fff}=1 \_1111{ }^{111}=-\mathrm{Inf}$ |

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## Value table: binary8p5



$\times 41=0^{-} 100 \_0001=+0 b 1.0001 * 2^{\wedge} 0=1.0625$
$0 \times 42=0 \_100 \_0010=+0 b 1.0010 * 2 \wedge 0=1.125$
x43 $=0 \_100 \_0011=+0 b 1.0011 * 2 \wedge 0=1.1875$
$0 \times 44=0 \_100 \_0100=+0 b 1.0100 * 2^{\wedge} 0=1.25$
$0 \times 45=0 \_100 \_0101=+0 \mathrm{~b} 1.0101 * 2 \wedge 0=1.3125$
$0 \times 46=0 \_100 \_0110=+0 \mathrm{~b} 1.0110 * 2 \wedge 0=1.375$
$0 \times 47=0 \_100 \_0111=+0 b 1.0111 * 2^{\wedge} 0=1.4375$
$0 \times 48=0 \_100 \_1000=+0 \mathrm{~b} 1.1000 * 2 \wedge 0=1.5$
$0 \times 49=0^{-} 100 \_1001=+0 \mathrm{~b} 1.1001 * 2^{\wedge} 0=1.5625$
$0 \times 4 \mathrm{a}=0 \_100 \_1010=+0 \mathrm{~b} 1.1010 * 2 \wedge 0=1.625$
$0 \times 4 b=01001011=+0 b 1.1011 * 2^{\wedge} 0=1.6875$
$0 \times 4 \mathrm{c}=0 \_100 \_1100=+0 \mathrm{~b} 1.1100 * 2^{\wedge} 0=1.75$
$0 \times 4 \mathrm{~d}=0 \_100 \_1101=+0 \mathrm{~b} 1.1101 * 2^{\wedge} 0=1.8125$
$0 \times 4 \mathrm{e}=0 \_100 \_1110=+0 \mathrm{~b} 1.1110 * 2 \wedge 0=1.875$
$0 \times 50=0 \_101 \_0000=+0 b 1.0000 * 2 \wedge 1=2$
$0 \times 51=0_{-}^{-} 101 \_0001=+0 b 1.0001 * 2^{\wedge} 1=2.125$
$0 \times 52=0 \_101 \_0010=+0$ b1. $0010 * 2 \wedge 1=2.25$
$0 \times 53=0 \_101 \_0011=+0 b 1.0011 * 2^{\wedge} 1=2.375$
$0 \times 54=0 \_101 \_0100=+0 \mathrm{~b} 1.0100 * 2 \wedge 1=2.5$
$0 \times 55=0 \_101 \_0101=+0$ b1 $1.0101 * 2^{\wedge} 1=2.625$
$0 \times 56=0 \_101 \_0110=+0$ b1 $.0110 * 2 \wedge 1=2.75$
$\mathbf{x} 57=0 \_101 \_0111=+0 b 1.0111 * 2 \wedge 1=2.875$
$0 \times 58=0 \_101 \_1000=+0 \mathrm{~b} 1.1000 * 2 \wedge 1=3$
$0 \times 59=0 \_101 \_1001=+$ bb1.1001*2^1 $=3.125$
$0 \times 5 \mathrm{a}=0 \_101 \_1010=+0 \mathrm{~b} 1.1010 * 2 \wedge 1=3.25$
$0 \times 5 \mathrm{~b}=0 \_101 \_1011=+0 \mathrm{~b} 1.1011 * 2 \wedge 1=3.375$
$0 \times 5 \mathrm{c}=0 \_101 \_1100=+0 \mathrm{~b} 1.1100 * 2 \wedge 1=3.5$
$0 \times 5 \mathrm{~d}=0_{-101 \_1101}^{-1}=+0 \mathrm{~b} 1.1101 * 2^{\wedge} 1=3.625$
$0 \times 5 \mathrm{e}=0 \_101 \_1110=+0 \mathrm{~b} 1.1110 * 2 \wedge 1=3.75$
$0 \times 5 f=0 \_101 \_1111=+0 b 1.1111 * 2 \wedge 1=3.875$
$0 \times 60=0 \_110 \_0000=+0 b 1.0000 * 2 \wedge 2=4$
$0 \times 61=0 \_110 \_0001=+0 b 1.0001 * 2^{\wedge} 2=4.25$
$0 \times 62=0 \_110 \_0010=+0 \mathrm{~b} 1.0010 * 2 \wedge 2=4.5$
$0 \times 63=0 \_110 \_0011=+0 \mathrm{~b} 1.0011 * 2^{\wedge} 2=4.75$
$0 \times 64=0 \_110 \_0100=+0 b 1.0100 * 2 \wedge 2=5$
$0 \times 65=0 \_110 \_0101=+0 \mathrm{~b} 1.0101 * 2^{\wedge} 2=5.25$
$0 \times 66=0 \_110 \_0110=+0 \mathrm{~b} 1.0110 * 2 \wedge 2=5.5$
$0 \times 67=0 \_110 \_0111=+0 \mathrm{~b} 1.0111 * 2^{\wedge} 2=5.75$
$0 \times 68=0 \_110 \_1000=+0 \mathrm{~b} 1.1000 * 2 \wedge 2=6$
$0 \times 69=0 \_110 \_1001=+0 b 1.1001 * 2^{\wedge} 2=6.25$
$0 \times 6 \mathrm{a}=0_{-}^{-110 \_} 1010=+0 \mathrm{~b} 1.1010 * 2 \wedge 2=6.5$
$0 \mathrm{x} 6 \mathrm{~b}=0 \_110 \_1011=+0 \mathrm{~b} 1.1011 * 2 \wedge 2=6.75$
$0 \times 6 \mathrm{c}=0 \_110 \_1100=+0 \mathrm{~b} 1.1100 * 2 \wedge 2=7$
$0 \times 6 \mathrm{~d}=\mathbf{0}_{-110 \_1101}=+0 \mathrm{~b} 1.1101 * 2 \wedge 2=7.25$
$0 \times 6 \mathrm{e}=0 \_110 \_1110=+0 \mathrm{~b} 1.1110 * 2 \wedge 2=7.5$
$0 \times 70=0 \_111 \_0000=+0 b 1.0000 * 2 \wedge 3=8$
$0 \times 71=0 \_111 \_0001=+0 \mathrm{~b} 1.0001 * 2^{\wedge} 3=8.5$
$0 \times 72=00^{-111}-0010=+0 b 1.0010 * 2^{\wedge} 3=9$
$0 \times 73=0 \_111 \_0011=+0 \mathrm{~b} 1.0011 * 2 \wedge 3=9.5$
$0 \times 74=0 \_111 \_0100=+0 b 1.0100 * 2 \wedge 3=10$
$0 \times 75=0 \_111 \_0101=+0 b 1.0101 * 2 \wedge 3=10.5$
$0 \times 76=0 \_111 \_0110=+0$ b1.0110*2^3 $=11$
$0 \times 77=0 \_111 \_0111=+0 \mathrm{~b} 1.0111 * 2^{\wedge} 3=11.5$
$0 \times 78=0 \_111 \_1000=+0$ b $1.1000 * 2^{\wedge} 3=12$
$0 \times 79=0 \_111 \_1001=+0$ b1.1001*2^3 $=12.5$
$0 \times 7 \mathrm{a}=0 \_111 \_1010=+0 b 1.1010 * 2^{\wedge} 3=13$
$0 \times 7 \mathrm{~b}=0 \_111 \_1011=+0 \mathrm{~b} 1.1011 * 2^{\wedge} 3=13.5$
x7c $=0 \_111 \_1100=+0 \mathrm{~b} 1.1100 * 2 \wedge 3=14$
$0 \times 7 \mathrm{~d}=0 \_111 \_1101=+0 \mathrm{~b} 1.1101 * 2^{\wedge} 3=14.5$
$0 \times 7 \mathrm{e}=0 \_111 \_1110=+0 \mathrm{~b} 1.1110 * 2^{\wedge} 3=15$
$0 \times 7 \mathrm{f}=0 \_111 \_1111=+$ Inf
$0 \times 80=1 \_0000000=\mathrm{NaN}$
$0 \times 80=1 \_000 \_0000=\mathrm{NaN}$
$0 \times 81=1 \_000 \_0001=-0 \mathrm{bb} 0.0001 * 2^{\wedge}-3=-0.0078125$
$0 \times 82=1 \_000 \_0010=-0 \mathrm{bo} .0010 * 2^{\wedge}-3=-0.015625$
$0 \times 82=1 \_000 \_0010=-0 \mathrm{~b} 0.0010 * 2^{\wedge}-3=-0.015625$
$0 \times 83=100000011=-0 \mathrm{~b} 0.0011 * 2^{\wedge}-3=-0.0234375$ $0 \times 84=10000100=-0 \mathrm{~b} 0.0100 * 2^{\wedge}-3=-0.03125$ $0 \times 85=1 \_000 \_0101=-0 b 0.0101 * 2^{\wedge}-3=-0.0390625$ $0 \times 86=1 \_000 \_0110=-0 b 0.0110 * 2^{\wedge}-3=-0.046875$ $0 \times 87=1 \_000 \_0111=-0 b 0.0111 * 2^{\wedge}-3=-0.0546875$ $0 \times 88=1 \_000 \_1000=-0 b 0.1000 * 2^{\wedge}-3=-0.0625$ $0 \times 89=1$ _ 000 _ $1001=-0 b 0.1001 * 2^{\wedge}-3=-0.0703125$ $0 \times 8 \mathrm{a}=1 \_000 \_1010=-0 \mathrm{~b} 0.1010 * 2^{\wedge}-3=-0.078125$ $0 \times 8 \mathrm{~b}=1 \_000 \_1011=-0 b 0.1011 * 2^{\wedge}-3=-0.0859375$ $0 \times 8 \mathrm{c}=1$ _-000_1100 $=-0 \mathrm{~b} 0.1100 * 2^{\wedge}-3=-0.09375$ $0 \times 8 \mathrm{~d}=1$ _ $000 \_1101=-0 b 0.1101 * 2^{\wedge}-3=-0.101562$ $0 \times 8 \mathrm{e}=\mathbf{1}_{-} 000$ _-1110 $=-0 b 0.1110 * 2^{\wedge}-3=-0.109375$
$0 \times 8 f=1 \_000 \_1111=-0 b 0.1111 * 2^{\wedge}-3=-0.117188$
$0 \times 90=1 \_001 \_0000=-0 b 1.0000 \star 2^{\wedge}-3=-0.125 \quad 0 \times \mathrm{xd} 0=1 \_101 \_0000=-0 \mathrm{~b} 1.0000 * 2 \wedge 1=-2$
$0 \times 91=1 \_001 \_0001=-0 b 1.0001 * 2^{\wedge}-3=-0.132812$
$0 \times 92=1 \_001 \_0010=-0 b 1.0010 * 2^{\wedge}-3=-0.140625$
$0 \times 93=1 \_001 \_0011=-0 b 1.0011 * 2^{\wedge}-3=-0.148438$
$0 \times 94=1 \_001 \_0100=-0 b 1.0100 * 2^{\wedge}-3=-0.15625$
$0 \times 94=1 \_001 \_0100=-0 b 1.0100 * 2^{\wedge}-3=-0.15625$
$0 \times 95=1 \_001 \_0101=-0 b 1.0101 * 2^{\wedge}-3=-0.164062$
$0 \times 96=1 \_001 \_0110=-0 b 1.0110 * 2^{\wedge}-3=-0.171875$
$0 \times 97=1 \_001 \_0111=-0 b 1.0111 * 2^{\wedge}-3=-0.179688$
$0 \times 98=1$ 001 $1000=-0 b 1.1000 * 2^{\wedge}-3=-0.1875$
$\left\lvert\, \begin{aligned} & 0 \times 98=1 \_001 \_1000=-0 b 1.1000 * 2^{\wedge}-3=-0.1875 \\ & 0 \times 99=1 \_001 \_1001=-0 b 1.1001 * 2^{\wedge}-3=-0.195312\end{aligned}\right.$
$0 \times 9 \mathrm{a}=1 \_001 \_1010=-0 b 1.1010 * 2^{\wedge}-3=-0.203125$
$0 \times 9 b=10011011=-0 b 1.1011 * 2^{\wedge}-3=-0.210938$
$0 \times 9 \mathrm{c}=1 \_001 \_1100=-0 \mathrm{~b} 1.1100 * 2^{\wedge}-3=-0.21875$
$0 \times 9 \mathrm{c}=1 \_001 \_1100=-0 \mathrm{~b} 1.1100^{\wedge} 2^{\wedge}-3=-0.21875$
$0 \times 9 \mathrm{~d}=1 \_001 \_1101=-0 b 1.1101 * 2^{\wedge}-3=-0.226562$
$0 \times 9 \mathrm{e}=$ 1_-001_1 $^{-} 1110=-0 \mathrm{~b} 1.1110 * 2^{\wedge}-3=-0.234375$
$0 \times 9 f=1$ _-001_-1111 $=-0 b 1.1111 * 2^{\wedge}-3=-0.242188$
$0 \times \mathrm{xaO}=1 \_010 \_0000=-0 \mathrm{~b} 1.0000 * 2^{\wedge}-2=-0.25$
$0 \times a 1=1 \_010 \_0001=-0 b 1.0001 * 2^{\wedge}-2=-0.265625$
$0 \times a 2=1 \_010 \_0010=-0 b 1.0010 * 2^{\wedge}-2=-0.28125$
$0 \times a 3=1 \_010 \_0011=-0 b 1.0011 * 2^{\wedge}-2=-0.296875$
$0 \times \mathrm{xa} 4=10100100=-0 \mathrm{~b} 1.0100 * 2^{\wedge}-2=-0.3125$
$0 \times a 5=1 \_010 \_0101=-0 b 1.0101 * 2^{\wedge}-2=-0.328125$
$0 \times a 6=1 \_010 \_0110=-0 b 1.0110 * 2^{\wedge}-2=-0.34375$
$0 \times \mathrm{xa7}=1 \_010 \_0111=-0 \mathrm{~b} 1.0111 * 2^{\wedge}-2=-0.359375$
$0 \times x$ 8 $=1 \_010 \_1000=-0 b 1.1000 * 2^{\wedge}-2=-0.375$
$0 \times \mathrm{xa9}=1$ _010_1001 $=-0 \mathrm{~b} 1.1001 * 2^{\wedge}-2=-0.390625$
$0 \times \mathrm{xaa}=1$ _010_1010 $=-0 \mathrm{~b} 1.1010 * 2^{\wedge}-2=-0.40625$
$0_{x a b}=1 \_010 \_1011=-0 b 1.1011 * 2^{\wedge}-2=-0.421875$
$0 \times \mathrm{xac}=1 \_010 \_1100=-0 \mathrm{~b} 1.1100 * 2^{\wedge}-2=-0.4375$
$0 \times \mathrm{xad}=1 \_010 \_1101=-0 \mathrm{~b} 1.1101 * 2^{\wedge}-2=-0.453125$
0 xae $=1$ _010_1110 $=-0 b 1.1110 * 2^{\wedge}-2=-0.46875$
0 xaf $=$ 1_010_- $1111=-0 b 1.1111 * 2^{\wedge}-2=-0.484375$
$0 \times \mathrm{xb} 0=1 \_011 \_0000=-0 \mathrm{~b} 1.0000 * 2^{\wedge}-1=-0.5$
$0 \times \mathrm{xb} 1=1 \_011 \_0001=-0 b 1.0001 * 2^{\wedge}-1=-0.53125$
$0 \times \mathrm{xb} 1=1 \_011 \_0001=-0 \mathrm{~b} 1.0001 * 2^{\wedge}-1=-0.53125$
$0 \times \mathrm{xb} 2=1 \_011 \_0010=-0 \mathrm{~b} 1.0010 * 2^{\wedge}-1=-0.5625$
$0 \times b 2=1 \_011 \_0010=-0 b 1.0010 * 2^{\wedge}-1=-0.5625$
$0 \times \mathrm{xb} 3=1 \_011 \_0011=-0 \mathrm{~b} 1.0011 * 2^{\wedge}-1=-0.59375$
$0 \times b 3=1 \_011 \_0011=-0 b 1.0011 * 2^{\wedge}-1=-0.5937$
$0 \times b 4=10110100=-0 b 1.0100 * 2^{\wedge}-1=-0.625$
$0 \times \mathrm{xb5}=1$ _011_0101 $=-0 \mathrm{~b} 1.0101 * 2^{\wedge}-1=-0.65625$
$0 \times b 5=1 \_011 \_0101=-0 b 1.0101 * 2^{\wedge}-1=-0.65625$
$0 \times b 6=1 \_011 \_0110=-0 b 1.0110 * 2^{\wedge}-1=-0.6875$
$0 \times \mathrm{xb} 6=1 \_011 \_0110=-0 \mathrm{~b} 1.0110 * 2^{\wedge}-1=-0.6875$
$0 \times \mathrm{xb} 7=1 \_011 \_0111=-0 \mathrm{~b} 1.0111 * 2^{\wedge}-1=-0.71875$
$0 \times \mathrm{xb} 7=1 \_011 \_0111=-0 \mathrm{~b} 1.0111 * 2^{\wedge}-1=-0.7187$
$0 \times \mathrm{b} 9=1 \_011 \_1001=-0 \mathrm{~b} 1.1001 * 2^{\wedge}-1=-0.78125$
$0 \times \mathrm{xba}=$ 1_011_ $^{-} 010=-0 \mathrm{~b} 1.1010 *$ 2^ $^{\wedge}-1=-0.8125$
$0 \times \mathrm{xbb}=1 \_011 \_1011=-0 b 1.1011 * 2^{\wedge}-1=-0.84375$
$0 \times \mathrm{xbc}=10111100=-0 \mathrm{~b} 1.1100 * 2^{\wedge}-1=-0.875$
$0 \times \mathrm{xbd}=1$ _011_1101 $=-0 \mathrm{~b} 1.1101 * 2^{\wedge}-1=-0.90625$
$0 x b d=1 \_011 \_1101=-0 b 1.1101 * 2^{\wedge}-1=-0.90625$
$0 x b e=1 \_011 \_1110=-0 b 1.1110 * 2^{\wedge}-1=-0.9375$
$0 \times \mathrm{xbe}=1 \_011 \_1110=-0 \mathrm{~b} 1.1110 * 2^{\wedge}-1=-0.9375$
$0 \mathrm{xbf}=1 \_011 \_1111=-0 \mathrm{~b} 1.1111 * 2^{\wedge}-1=-0.96875$
$0 \times \mathrm{xc} 0=1 \_100 \_0000=-0 \mathrm{~b} 1.0000 * 2^{\wedge} 0=-1$
$0 \mathrm{xc} 1=1 \_100 \_0001=-0 \mathrm{~b} 1.0001 * 2^{\wedge} 0=-1.0625$ $0 \times \mathrm{xc} 1=1-100 \_0001=-0 \mathrm{~b} 1.0001 * 2 \wedge 0=-1.0625$
$0 \mathrm{xc} 2=11000010=-0 \mathrm{~b} 1.0010 * 2 \wedge 0=-1.125$ $0 \times \mathrm{xc} 2=1 \_100 \_0010=-0 \mathrm{~b} 1.0010 * 2^{\wedge} 0=-1.125$
$0 \mathrm{xc} 3=11000011=-0 \mathrm{~b} 1.0011 * 2^{\wedge} 0=-1.1875$ xc3 $=1 \_100 \_0011=-0 b 1.0011 * 2^{\wedge} 0=-1.1875$
$0 \mathrm{xc} 4=1 \_100 \_0100=-0 \mathrm{~b} 1.0100 * 2^{\wedge} 0=-1.25$
$0 x c 4=1 \_100 \_0100=-0 b 1.0100 * 2^{\wedge} 0=-1.25$
$0 x c 5=1 \_100 \_0101=-0 b 1.0101 * 2^{\wedge} 0=-1.3125$
$0 x c 6=1 \_100 \_0110=-0 b 1.0110 * 2^{\wedge} 0=-1.375$
$0 \times \mathrm{c} 6=1 \_100 \_0110=-0 \mathrm{~b} 1.0110 * 2 \wedge 0=-1.375$
$0 \times \mathrm{xc} 7=1 \_100 \_0111=-0 \mathrm{~b} 1.0111 * 2 \wedge 0=-1.4375$
$0 \times \mathrm{xc} 7=1 \_100 \_0111=-0 \mathrm{~b} 1.0111 * 2^{\wedge} 0=-1.43$
$0 \times \mathrm{xc} 8=1 \_100 \_1000=-0 \mathrm{~b} 1.1000 * 2^{\wedge} 0=-1.5$
$0 \times \mathrm{xc} 9=1 \_100 \_1001=-0 \mathrm{~b} 1.1001 \star 2 \wedge 0=-1.5625$
$\begin{aligned} 0 \times 1 \_ & =1 \_100 \_1010=-0 b 1.1010 * 2^{\wedge} 0=-1.625\end{aligned}$
$0 \times \mathrm{ca}=1 \_100 \_1010=-0 \mathrm{~b} 1.1010 * 2^{\wedge} 0=-1.625$
$0 \times \mathrm{cb}=1 \_100 \_1011=-0 \mathrm{~b} 1.1011 * 2^{\wedge} 0=-1.6875$
$0 \times \mathrm{xcc}=1 \_100 \_1100=-0 \mathrm{~b} 1.1100 * 2^{\wedge} 0=-1.75$

$0 \mathrm{xcd}=1 \_100 \_1101=-0 \mathrm{~b} 1.1101 * 2^{\wedge} 0=-1.8125$
$0 \mathrm{xce}=1 \_100 \_1110=-0 \mathrm{~b} 1.1110 * 2^{\wedge} 0=-1.875$
$0 x c e=1 \_100 \_1110=-0 b 1.1110 * 2^{\wedge} 0=-1.875$
$0 x c f=11001111=-0 b 1.1111 * 2^{\wedge} 0=-1.937$
$0 \times \mathrm{xd0}=11010000=-0 \mathrm{~b} 1.0000 * 2 \wedge 1=-2$
$0 \times \mathrm{xd0}=1 \_101 \_0000=-0 \mathrm{~b} 1.0000 * 2^{\wedge} 1=-2$
$0 \times \mathrm{xd} 1=1 \_{ }^{101 \_} \mathbf{-} 0001=-0 \mathrm{~b} 1.0001 * 2 \wedge 1=-2.125$
$\left\{\begin{array}{l}0 x d 1=1 \_101 \_0001=-0 b 1.0001 * 2 \wedge 1=-2.125 \\ 0 \times d 2=1 \_101 \_0010=-0 b 1.0010 * 2 \wedge 1=-2.25 \\ 0 x d 3=1 \_101 \_0011=-0 b 1.0011 * 2 \wedge 1=-2.375\end{array}\right.$
$0 \times \mathrm{xd} 3=1 \_101 \_0011=-0 \mathrm{~b} 1.0011 * 2^{\wedge} 1=-2.375$
$0 x d 3=1 \_101 \_0011=-0 b 1.0011 * 2^{\wedge} 1=-2.375$
$0 x d 4=1 \_101 \_0100=-0 b 1.0100 * 2^{\wedge} 1=-2.5$
$0 \times d 4=1 \_101 \_0100=-0 b 1.0100 * 2^{\wedge} 1=-2.5$
$0 \times d 5=1 \_101 \_0101=-0 b 1.0101 * 2^{\wedge} 1=-2.625$

$0 \times \mathrm{xd7}=1_{-} 101 \_0111=-0 \mathrm{~b} 1.0111 * 2^{\wedge} 1=-2.875$
$0 \times d 7=1 \_1-10110$
$0 \times d 8=1000=-0 b 1.1000 * 2^{\wedge} 1=-3$
$\left\{\begin{array}{l}0 x d 8=1 \_101 \_1000=-0 b 1.1000 * 2^{\wedge} 1=-3 \\ 0 x d 9=1 \_101 \_1001=-0 b 1.1001 * 2^{\wedge} 1=-3.125 \\ 0 x d a=1 \_101 \_1010=-0 b 1.1010 * 2^{\wedge} 1=-3.25\end{array}\right.$
$0 x d a=1 \_101 \_1010=-0 b 1.1010 * 2 \wedge 1=-3.25$
$0 x d b=1 \_101 \_1011=-0 b 1.1011 * 2 \wedge 1=-3.375$
$0 \times \mathrm{db}=1 \_101 \_1011=-0 \mathrm{~b} 1.1011 * 2^{\wedge} 1=-3.375$
$0 \times d c=1 \_101 \_1100=-0 \mathrm{~b} 1.1100 * 2^{\wedge} 1=-3.5$

$0 \times x d e=1 \_101 \_1110=-0 b 1.1110 * 2^{\wedge} 1=-3.75$
$\left\{\begin{array}{l}0 x d e=1 \_101 \_1110=-0 b 1.1110 * 2 \wedge 1=-3.75 \\ 0 x d f=1 \_101 \_1111=-0 b 1.1111 * 2 \wedge 1=-3.875\end{array}\right.$
$0 x d f=1 \_{ }^{101}{ }_{-} 1111=-0 b 1.1111 * 2^{\wedge} 1=-3.875$
$0 \times \mathrm{xe} 0=1 \_110 \_0000=-0 \mathrm{~b} 1.0000 * 2 \wedge 2=-4$
$0 \times 1=1 \_110 \_0001=-0 b 1.0001 * 2 \wedge 2=-4.25$
$0 \mathrm{xe} 1=1 \_110 \_0001=-0 \mathrm{~b} 1.0001 * 2^{\wedge} 2=-4.25$
$0 \mathrm{xe} 2=1 \_110 \_0010=-0 \mathrm{~b} 1.0010 * 2^{\wedge} 2=-4.5$
$0 \mathrm{xe} 2=1 \_110 \_0010=-0 \mathrm{~b} 1.0010 * 2^{\wedge} 2=-4.5$
$0 \mathrm{xe} 3=1 \_110 \_0011=-0 \mathrm{~b} 1.0011 * 2^{\wedge} 2=-4.75$
$0 x$ x $4=1 \_110 \_0100=-0 b 1.0100 * 2 \wedge 2=-5$
$\left\{\begin{array}{l}0 \text { xe4 }=1 \_110 \_0100=-0 \mathrm{~b} 1.0100 * 2 \wedge 2=-5 \\ 0 \times 5=5=1 \_110 \_0101=-0 \mathrm{~b} 1.0101 * 2 \wedge 2=-5.25 \\ 0 \text { xe6 }=110=0110=-0 b 1.0110 * 2 \wedge 2=-5.5\end{array}\right.$
0 ore6 $=1 \_110 \_0110=-0 \mathrm{~b} 1.0110 * 2 \wedge 2=-5.5$
$0 x e 6=1 \_110 \_0110=-0 b 1.0110 * 2^{\wedge} 2=-5.5$
$0 x e 7=1 \_110 \_0111=-0 b 1.0111 * 2^{\wedge} 2=-5.75$
$0 \mathrm{xe} 7=1 \_110 \_0111=-0 \mathrm{~b} 1.0111 * 2^{\wedge} 2=-5.75$
$0 \mathrm{xe} 8=1 \_110 \_1000=-0 \mathrm{~b} 1.1000 * 2^{\wedge} 2=-6$
$0 \mathrm{xe} 8=1 \_110 \_1000=-0 \mathrm{bb} 1.1000 * 2^{\wedge} 2=-6$
$0 \mathrm{xe} 9=1 \_110 \_1001=-0 \mathrm{~b} 1.1001 * 2^{\wedge} 2=-6.25$
0 xe9 $=1 \_110 \_1001=-0 b 1.1001 * 2^{\wedge} 2=-6.25$
0 xea $=1 \_110 \_1010=-0 b 1.1010 * 2^{\wedge} 2=-6.5$
0 xea $=1 \_110 \_1010=-0 b 1.1010 * 2^{\wedge} 2=-6.5$
0 xeb $=1 \_110 \_1011=-0 b 1.1011 * 2^{\wedge} 2=-6.75$
$\left\{\begin{array}{l}0 \times \mathrm{xeb}=1 \_110 \_1011=-0 \mathrm{~b} 1.1011 * 2^{\wedge} 2=-6.75 \\ 0 \times \mathrm{xec}=1 \_110 \_1100=-0 b 1.1100 * 2^{\wedge} 2=-7\end{array}\right.$
0 xec $=1 \_110 \_1100=-0 \mathrm{~b} 1.1100 * 2 \wedge 2=-7$
0 xed $=1 \_110 \_1101=-0 \mathrm{~b} 1.1101 * 2 \wedge 2=-7.25$
0 xee $=11101110=-0 \mathrm{~b} 1.1110 * 2 \wedge 2=-7.5$
oxae $=10^{-1101}=-0 b 1.1101 * 2^{\wedge}-2=-0$.
0 xed $=1 \_110 \_1101=-0 b 1.1101 * 2^{\wedge} 2=-7.25$
0 xee $=1 \_110 \_1110=-0 b 1.1110 * 2^{\wedge} 2=-7.5$
0 xee $=1 \_110-1110=-0 b 1.1110 * 2^{\wedge} 2=-7.5$
0 xef $=1 \_110 \_1111=-0 b 1.1111 * 2^{\wedge} 2=-7.75$
$0 \times f 0=1 \_111 \_0000=-0 b 1.0000 * 2 \wedge 3=-8$
$0 \times f 1=1 \_111 \_0001=-0 b 1.0001 * 2 \wedge 3=-8.5$
$0 \times f 1=1 \_111 \_0001=-0 b 1.0001 * 2 \wedge 3=-8.5$
$0 \times f 2=1 \_111-0010=-0 b 1.0010 * 2^{\wedge} 3=-9$
$0 \times f 3=1 \_111 \_0011=-0 b 1.0011 * 2 \wedge 3=-9.5$
$\left\{\begin{array}{l}0 \times f 2=1 \_111-0010=-0 b 1.0010 * 2^{\wedge} 3=-9 \\ 0 \times f 3=1 \_111 \_0011=-0 b 1.0011 * 2^{\wedge} 3=-9.5\end{array}\right.$
$0 \times f 3=1 \_111 \_0011=-0 b 1.0011 * 2 \wedge 3=-9.5$
$0 \times f 4=1 \_111 \_0100=-0 b 1.0100 * 2 \wedge 3=-10$
$\left\{\begin{array}{l}0 \times f 4=1 \_111 \_0100=-0 \mathrm{~b} 1.0100 * 2 \wedge 3=-10 \\ 0 \times f 5=1 \_111 \_0101=-0 \mathrm{~b} 1.0101 * 2 \wedge 3=-10.5 \\ 0 \times f 6=11110=-0 b 1.0110 * 2 \wedge 3=-11\end{array}\right.$
$0 \times f 6=1 \_111 \_0110=-0$ b1.0110*2^3 $=-11$
$0 \times f 6=1 \_111 \_0110=-0 b 1.0110 * 2^{\wedge} 3=-11$
$0 \times f 7=1 \_111-0111=-0 b 1.0111 * 2^{\wedge} 3=-11.5$
$0 \times f 7=1 \_111 \_0111=-0 b 1.0111 * 2 \wedge 3=-11$.
$0 \times f 8=1 \_111 \_1000=-0 b 1.1000 * 2 \wedge 3=-12$
$\left\{\begin{array}{l}0 \times f 8=1 \_111-1000=-0 b 1 \cdot 1000 * 2^{\wedge} 3=-12 \\ 0 \times f 9=1-111 \_1001=-0 b 1 \cdot 1001 * 2^{\wedge} 3=-12.5 \\ 0 x f a=11111010=-0 b 1.1010 * 2^{\wedge} 3=-13\end{array}\right.$
$0 \times 1 \times 1{ }^{2}$
$0 \times f a=1 \_111 \_1010=-0 b 1 \cdot 1010 * 2 \wedge 3=-13$
$0 \times f b=1 \_111 \_1011=-0 b 1 \cdot 1011 * 2^{\wedge} 3=-13.5$
$0 \times f b=1 \_111 \_1011=-0 \mathrm{~b} 1.1011 * 2 \wedge 3=-13$.
$0 \times f \mathrm{fc}=1 \_111 \_1100=-0 \mathrm{~b} 1.1100 * 2 \wedge 3=-14$
$0 \times f \mathrm{fc}=1 \_111 \_1100=-0 \mathrm{~b} 1.1100 * 2^{\wedge} 3=-14$
$0 \times f \mathrm{fd}=1-111-1101=-0 \mathrm{~b} 1.1101 * 2^{\wedge} 3=-14.5$
$0 \times \mathrm{xfe}=1_{-}{ }^{111 \_} \mathrm{l}^{1110}=-0 \mathrm{~b} 1.1110 * 2^{\wedge} 3=-15$
$0 \times f e=1 \_111 \_1110=-0 b 1$.
$0 \times f f=1 \_{ }^{111 \_1111}=-\operatorname{Inf}$

