Multi-objective optimization of water distribution networks via NSGA-II and Pseudo-Weights

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Abstract—Managing water distribution networks via pumps scheduling programs is a multi-objective optimization problem with dynamic and various site-specific challenges. Metaheuristics-based approaches, with respect to mathematical solvers, offer data-driven strategies for manageable and adaptive control. Some evolutionary approaches are suitable for multi-criteria decision making and decentralized coordination on programmable logic controllers. This paper focuses on the development of a testbed and an early assessment of an approach based on NSGA-II and Pseudo-Weights. The experimental studies are based on a physically developed case study, and on a scalable case study with realistic water demand and source patterns. The testbed has been publicly released.

Keywords—water distribution network, genetic algorithm, multi-objective optimization, multi-criteria decision making

I. INTRODUCTION AND BACKGROUND

The optimal management of Water Distribution Networks (WDNs) often faces various site-specific challenges: network topology and complexity, number of electrical pumps, heterogeneous water sources, availability of service reservoirs, local electricity tariffs for peak/off-peak periods, pumps maintenance cost, local hourly water demand, seasonal weather conditions, medium-term socio-economic context such as growth of population and urbanization, and so on [1].

The task of determining the operating time of each pump, in order to meet the predicted water demand, and according to other management criteria, is known as Pump Scheduling (PS) [2]. Two common criteria are to reduce the pumping cost and maintenance, and to guarantee a cyclic sources exploitation. Usually, the scheduling horizon is one day, after which the same or a revised schedule is applied. To manage the PS task complexity, a WDN is partitioned into subnetworks [2]. The PS program provides a real-time control of sources, pumps, and tanks of the local distribution system, according to a decision-making process supported by information technology [3][4].

In the literature, different approaches have been proposed for optimal PS, such as linear/nonlinear programming, dynamic programming, metaheuristic algorithms. It is well-known that metaheuristics are computationally slower than mathematical solvers, but are relatively easier to implement, and are capable of handling both real and discrete types of decision variables in multimodal search spaces [5]. For this reason, various approaches have been experimented to the PS, such as Simulated Annealing, Hill Climb, Ant Colony Optimization, Shuffled Frog Leaping, and Genetic Algorithms (GAs). Among them, GAs have been extensively considered [5][7][8][9][10].

A significant design aspect is the scheme of representation of PS, affecting the size and complexity of the decision space: it can be an implicit scheme (e.g., expressed in terms of tank level-controlled triggers) or an explicit scheme (e.g., expressed in terms of time-controlled triggers).

Although some researches model the PS as a multi-objective optimization problem [5][7], most of them find one particular Pareto-optimal solution at a time. Thus, for multiple solutions, the GA has to be applied multiple times. In order to support a more flexible and adaptive decision making, this research focuses on the ability of some GAs to find multiple Pareto-optimal solutions in one single simulation run [5]. In essence, since GAs work with a population of solutions, it can be extended to maintain diverse sets of solutions. In Nondominated Sorting GA (NSGA)[5], there are representative solutions (called “non-dominated”) that are superior or equal to the others (called “dominated”), with respect to all objectives. In NSGA, the selection operator works differently than in conventional GA: the fitness assignment, based on dummy values, allows multiple optimal points to co-exist in the population.

The choice of one solution over the others requires a decision-making process. One typical decision-making is to scalarize the vector of objectives into one objective, via a weight vector. However, the obtained solution largely depends on the weights, and this sensitivity makes the determination of such parameters expensive. A method to reduce the parametric sensitivity of decision-making is to move from the space of solutions to another space, simpler and more manageable from the human decisor. In this paper, the pseudo-weight method is used, in which a candidate solution is represented by a calculated weight for each objective. In the normalized pseudo-weight
space, the best solution can be identified by assigning a target pseudo-weight vector expressing the relative importance among the objectives.

The paper is structured as follows: Section II formally describes the methodology. Section III illustrates the case studies. Section IV draws the conclusions. The main contributions of this paper are the following: (i) to propose a multi-objective optimization for water distribution networks based on NSGA-II and Pseudo-Weights; (ii) to show how different decision-making strategies can be easily compared; (iii) to develop and publicly release a testbed; (iv) to outline future developments of this research.

II. METHODOLOGY

Fig. 1 illustrates a reference scenario of water distribution. Let us consider \( N \) tanks, with related pumps \( p_i, i = 1, \ldots, N \). Each pump with a binary (on/off) command to supply the main tank with a constant flow \( f_i \). A pump behavior is specified via an hourly scheduling program in a daily horizon, imparted via a relay, \( p_i(t) \in \{0,1\}, t = 0, \ldots, 23 \). Each tank is supplied by an external source \( s_i(t) \). The total daily flow of the external sources is assumed to be sufficient to cover the total daily water demand at the main tank.

Let \( v_i(t) \) be the current volume of the \( i \)-th tank, measured via a sensor. Let \( v_0(t) \) be the main tank volume. The main tank is equipped with \( M \) independent output valves having constant flow, to supply the water demand \( d_j(t), j = 1, \ldots, M \). On the figure top, a Programmable Logic Controller (PLC) solves the PS problem, by taking the expected daily water demand \( \{d_j(t)\} \) and the tank volumes \( \{v_i(t)\} \) as inputs, and providing the PS solution as an output.

With the explicit scheme, the solution is specified as a sequence of 24 binary commands per pump, \( p_i(t) \). With the implicit scheme, the solution is a pair of thresholds volumes \( (v_{i}^n, v_{i}^{off}) \); initially the pump is turned off; when the level is under \( v_{i}^{off} \) / upper \( v_{i}^n \), then the pump is switched off / on, respectively.

The optimal PS is represented as a multi-objective optimization problem with three objective functions to minimize: (1) daily pumping energy cost, (2) daily number of pump switches, (3) daily volume surplus/deficit of the main tank. Table I summarizes the motivation/description of each objective, whereas Equations (1-3) define them formally.

\[
\begin{align*}
F_{PC} &= \sum_{i=1}^{N} \sum_{t=0}^{23} f_i \cdot p_i(t) \quad (1) \\
F_{SW} &= \sum_{i=1}^{N} \sum_{t=0}^{22} |p_i(t+1) - p_i(t)| \\
F_{SV} &= \sum_{t=0}^{23} \left( \sum_{i=1}^{N} f_i \cdot p_i(t) - \sum_{j=1}^{M} d_j(t) \right) \quad (3)
\end{align*}
\]

Three types of constraints are also imposed on the problem: (4) daily water availability, (5) lower tank volume, (6) upper tank volume. Table II summarizes the motivation/description of each constraint, whereas Equations (4-6) define them formally.

\[
\begin{align*}
\text{Daily water availability} & \quad \text{The total daily water supplied by external sources is greater than or equal to the total daily water demand.} \\
\text{Lower tank volume} & \quad \text{The tank volume cannot be lower than a predefined threshold, under which the pump is switched off.} \\
\text{Upper tank volume} & \quad \text{The tank volume cannot be higher than a predefined threshold, over which the water surplus is lost (water overflow).}
\end{align*}
\]

TABLE I. DEFINITION OF EACH OBJECTIVE TO OPTIMIZE

<table>
<thead>
<tr>
<th>Objective</th>
<th>Motivation/description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total daily pumping cost ( F_{PC} )</td>
<td>The pumping energy cost is directly proportional to the pump water flow (l/hour).</td>
</tr>
<tr>
<td>Total daily number of pump switches ( F_{SW} )</td>
<td>The number of pump switches is a measure of mechanical wear.</td>
</tr>
<tr>
<td>Daily volume variation of the main tank ( F_{SV} )</td>
<td>It is the absolute difference between the initial and final main tank volume. It measures the acyclicity of the process.</td>
</tr>
</tbody>
</table>

TABLE II. DESCRIPTION OF EACH CONSTRAINT

<table>
<thead>
<tr>
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</tbody>
</table>

To minimize the objective functions (1-3) under the constraints (4-6), the constrained NSGA-II [11] is used. Specifically, NSGA-II is an evolutionary algorithm for multi-objective problems, based on the notion of dominancy between solutions. Solution \( x \) dominates \( y \) if none of objectives in \( x \) is worse than in \( y \) and at least one objective in \( x \) is better than in \( y \) [11]. At each generation, the population of PS solutions is divided into the feasible and infeasible sub-populations,
according to the total constraints’ violation, and then the feasible population is ranked based on the notion of dominancy.

\[
\sum_{i=1}^{N} s_i(t) \geq \sum_{j=1}^{M} d_j(t) \quad (4)
\]

\[
p_i(t) = 0, \forall i \neq 0 \land v_i(t) \leq v_j \quad (5)
\]

\[
v_i(t+1) = \begin{cases} 
\min\{\bar{v}_i; v_i(t) - p_i(t) + s_i(t)\}, & i \neq 0 \\
\min\{\bar{v}_i; v_i(t) - \sum_{j=0}^{M} d_j(t) + \sum_{i=0}^{N} f_i \cdot p_i(t)\}, & i = 0
\end{cases} \quad (6)
\]

The Pareto fronts of \( l \) levels are formed, the infeasible chromosomes are stored in front \( l+1 \). The crowding distance between chromosomes is also considered to preserve diversity. The parent selection is based on a combined criterion: total constraint violation, non-dominination rank and crowding distance. After obtaining a set of non-dominated solutions, a single solution has to be chosen for implementation.

The decision-making approach used is based on pseudo-weights [12]. For each \( o \)-th objective function, a pseudo-weight of a solution is calculated as follows:

\[
w_o = \frac{(\bar{F}_o - F_o)/(\bar{F}_o - F_o)}{\sum_{h=1}^{N}(\bar{F}_h - F_h)/(\bar{F}_h - F_h)} \quad (7)
\]

where \( \bar{F}_o \) and \( F_o \) are the maximum and minimum values of the \( o \)-th objective function, respectively. In (7) the sum of all elements \( w_o \) of the vector is forced to one. Thus, the pseudo-weight vector represents a relative importance of each objective function for the solution. This means that solutions that are closer to the minimum objective value have a higher weight value for that objective. To accomplish different strategies, the decisor establishes different target pseudo-weight vectors. In the reference scenario, the following four different strategies and related targets have been considered: (a) balanced: \( (1/3, 1/3, 1/3) \); cost-saving: \( (.9, .05, .05) \), switch-saving: \( (.05, .9, .05) \), volumes-cyclicity: \( (.05, .05, .9) \). For each strategy, the best solution is found in the space of pseudo-weights, as the solution with the closest target pseudo-weight vector.

**III. CASE STUDIES**

In order to assess the effectiveness of the proposed approach, a simulation test bed has been developed for the modeling and execution of pilot case studies. The testbed is based on a recent multi-objective optimization framework supporting a variety of approaches [13]. A hydraulic simulation model has been developed in order to support the features illustrated in Fig. 1. The overall testbed has been publicly released as a GitHub repository [14]. To extend the features of the hydraulic simulator, as a future task, the testbed could be integrated with the WNTR framework, which contains the EpanetSimulator and the WNTRSImulator [15].

To understand the potential of the proposed approach, this Section shows an experiment on an interpretable pilot case study of the reference scenario, as well as another experiment on a scalable case study.

**A. Interpretable case study**

This first case study is based on a comparative analysis of implicit and explicit schemes across four different strategies. The case study is intentionally small to allow an easy interpretation of the scheduling results. It uses \( N=2 \) pumps and \( M=2 \) valves for demand. It has also been physically developed in a hydraulic lab as a prototype, using a Raspberry Pi© programmable controller, for the purpose of integration and lifecycle testing.

Specifically, the following hyperparameters have been set in the optimization framework: population size: 100, number of generations: 1000, crossover rate 0.9, selection: binary tournament, and mutation rate = 1/ chromosome length (48 or 4 genes, in case of explicit or implicit scheme, respectively). The following parameters have been set in the hydraulic simulator, according to the physical prototype (volumes are in \( l \), flows in \( l/h \)): \( \bar{V}_0 = 30, \bar{V}_1 = \bar{V}_2 = 14, v_0 = 10, v_1 = v_2 = 4, v_0(0) = 30, v_1(0) = v_2(0) = 4, f_1 = f_2 = 3 \). Fig. 2 shows the water demand. For the sake of simplicity/interpretability, \( d_1=s_1 \) and \( d_2=s_2 \).

Fig. 3 shows the optimal PS and simulation results with the explicit scheme and strategies (a) balanced, (b) cost-saving, (c) switch-saving, (d) volumes-cyclicity. Fig. 4 shows the results generated with the implicit scheme. As expected, Fig. 3a and particularly Fig. 3d show a better volumes-cyclicity with respect to Figures 3b-c, which is consistent with the corresponding strategies. The volumes-cyclicity is better achieved with the implicit scheme: in Figures 4a-d, \( F_{PC} \) is less than or equal to the corresponding Figures 3a-d. In contrast, the cost-saving is better with the explicit scheme: in Figures 3a-d, \( F_{PC} \) is less than or equal to the corresponding Figures 4a-d. The switch-saving is generally better with the implicit scheme, except if cost-saving is the preferred strategy: note in Fig. 4b that pump \( p_1 \) is characterized by frequent switches. Such switches are caused by the very close switching thresholds, \( v_1^{off} \approx v_1^{on} \), which results from the cost-saving strategy. In a balanced strategy, the implicit scheme is more effective.

Overall, with respect to the explicit scheme, the implicit scheme always achieves minimum (optimum) values of \( F_{PC} \), as well as of \( F_{SW} \) except for the cost-saving strategy. On the other hand, the \( F_{PC} \) value achieved via the implicit scheme is equal or higher to the corresponding value achieved via the explicit one.

![Fig. 2. Water demand, equal to the external sources \( s_1, s_2 \).](image)
Fig. 3. Optimal PS and simulation results, with explicit scheme and strategies (a) balanced, (b) cost-saving, (c) switch-saving, (d) volumes-cyclicity.

Hence, the implicit scheme tends to find better solutions from the point of view of mechanic wear and process cyclicity, at a cost that in some cases is higher. In this pilot case study, the implicit pump scheduling scheme can be appreciated for its effectiveness with the balanced, switch-saving, and volumes-cyclicity strategies, whereas the explicit scheduling can be better exploited to manage the cost-saving strategies.

B. Scalable case study

In order to evaluate the effectiveness of the proposed approach when varying the problem size, in this case study the considered problem complexity differs by one order of magnitude with respect to the previous one. Specifically, \( N = 20 \) pumps/sources and \( M = 20 \) valves for demand have been used. Half of the water production (i.e., 10 sources) is based on natural sources, whereas the other half is based on water desalinization technology. The natural sources are characterized by a daily constant supply. The average flow is \( s = 0.8 \), with 10% variation among sources. The artificial water production is based on a combined water desalination and electricity generation system, a sustainable technology in which a humidification-dehumidification (HDH) process is integrated with photovoltaic-thermal modules [16].

Fig. 4. Optimal PS and simulation results, with implicit scheme and strategies (a) balanced, (b) cost-saving, (c) switch-saving, (d) volumes-cyclicity.

Fig. 5. Hourly profiles of water flow for HDH-based sources \( s_i \) (adapted from [16]).

Fig. 5 shows the hourly profiles of water flow for some representative months of the year. In the scenario, the production in July has been considered, with 10% variation among sources.
The 20 water demand patterns are based on a mid-size city, and intended for residential (5 valves), industrial (5 valves) and commercial/institutional (10 valves) nodes [17]. Fig. 6 shows each type of pattern. A 10% variation among demands of the same type has been considered.

In this scenario, the implicit representation scheme has been used, with each pump controlled by a lower and an upper bound. As a consequence, each chromosome is made by 2N = 40 genes. The following hyperparameters have been set in the optimization framework: population size: 100, number of generations: 200, crossover rate 0.9, selection: binary tournament, and polynomial mutation with rate = 1/40 (chromosome length). The following initial state parameters have been set in the hydraulic simulator (volumes are in l, flows in l/h): \( V_0 = 200 \), \( V_i = 50 \), \( V_o = 20 \), \( V_i = 5 \), \( V_o(0) = 100 \), \( v_i(0) = 10 \), \( f_i = 1 \).

Table III summarizes the PS determined via different strategies. For the sake of readability, the switching bounds have been rounded to the nearest integer. In Table III the best value possible, by keeping all tanks full. This single-objective strategy has been introduced to show that a multi-objective strategy in general is more effective.

Table III: PS for different strategies, with implicit scheme

<table>
<thead>
<tr>
<th>Strategy</th>
<th>Prc</th>
<th>Fsw</th>
<th>FAV</th>
<th>lower/upper switching bounds determined ( v_{i,0}^{on-off} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>cost-saving</td>
<td>260</td>
<td>51</td>
<td>59</td>
<td>10/42 7/42 6/44 10/7 7/44 40/44 14/11 7/41 7/47 44/14 35/27 43/44 27 8/33 48/18 49/26 9/19 7/44 11/45 8/47</td>
</tr>
<tr>
<td>volumes-cyclicity</td>
<td>290</td>
<td>55</td>
<td>29</td>
<td>10/1 11/45 39/40 12/1 13/2 39/26 7/20 14/3 8/10 14/3 15/42 11/7 6/38 11/5 49/46 48/10 9/19 31/43 13/45 7/46</td>
</tr>
</tbody>
</table>

Formally, the water-greedy strategy is characterized by a PS statically determined with \( v_{i,0}^{on} = v_{i,0}^{off} \): it means that the pump is switched on as soon as the level is below the maximum. In practice, the tank is almost always full.

As a result, the table shows what follows: (i) the volumes-cyclicity strategy tries to achieve the cyclicity via a high number of switches and pumping cost; (ii) the switch-saving strategy minimizes switches at the expense of cyclicity and of some pumping cost; (iii) the cost-saving strategy minimizes cost via high switches and high cyclicity; (iv) the balanced strategy achieves a good volumes cyclicity and good pumping cost. Not surprisingly, it is apparent from Table III that the water-greedy strategy is very expensive in terms of pumping and switching costs, as well as poorly volumes-cyclic. In contrast, the other strategies are very effective in achieving the expected optimization. It can be also observed a high variety of switching bounds provided by each strategy. This reveals the fact that the search space is inherently complex.

IV. CONCLUSIONS

In this paper, the development of a testbed that simulates water distribution networks, and enables the evaluation of in-node decision making, is presented. The purpose is to introduce a novel design perspective of multi-objective optimization systems for water distribution, offered by NSGA-II and Pseudo-Weights. An interpretable (i.e., small) case study and a scalable (large) case study have been discussed, to show the effectiveness of the proposed approach, by comparing different strategies.

Further research is necessary to compare different metaheuristics on different and large scenarios. To achieve significant results, future work will focus on further experimentation and investigation, as well as on further integration with advanced hydraulic simulator.

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