

## PROCESS MINING

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### Process Mining: introduction

2 of 68

✓ The focus of process mining is to discover, monitor and improve **real** processes (i.e., not assumed processes) by extracting knowledge from **event logs** readily available in today's information systems.

✓ Process mining techniques includes:

a) **automated process discovery** (extracting process models from an event log)

b) **conformance checking** (monitoring deviations by comparing model and log)

c) **model enhancement** (model extension and repairing)

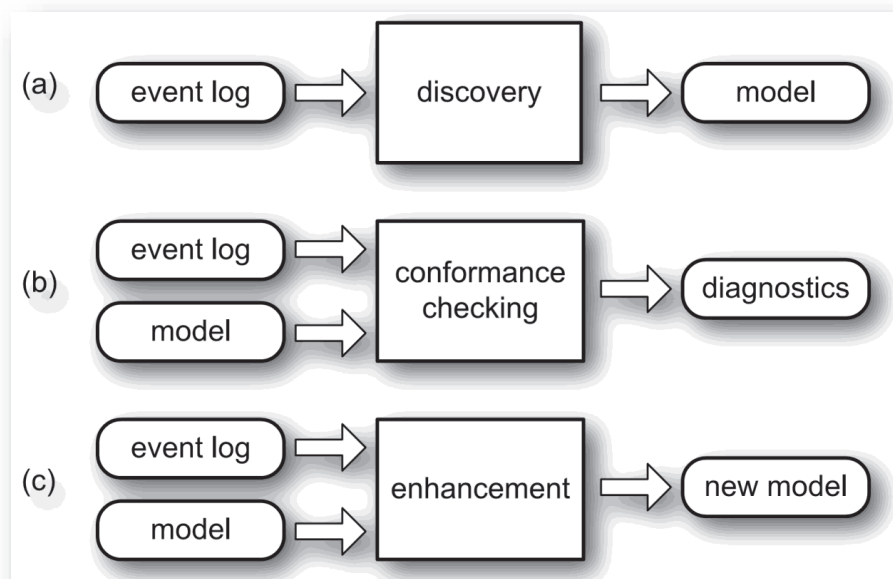


Figure : The three basic types of process mining explained in terms of input and output: (a) discovery, (b) conformance checking, and (c) enhancement.

✓ Drivers: growth of digital world + continuous process changes over time

✓ Process models are expressed via process notation: Petri net, causal nets, process trees, EPCs, BPMN, or UML activity diagrams.

✓ BPMN 2.0 is a de-facto standard for modeling.

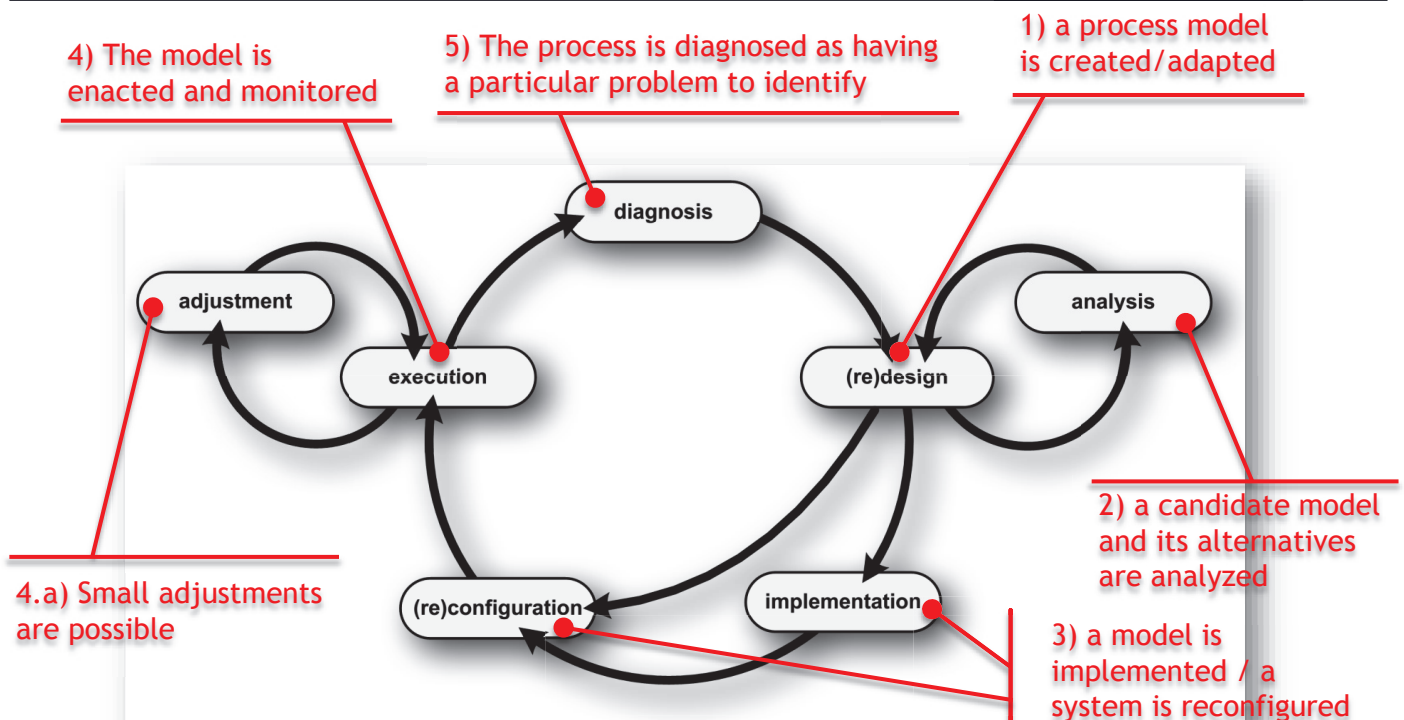
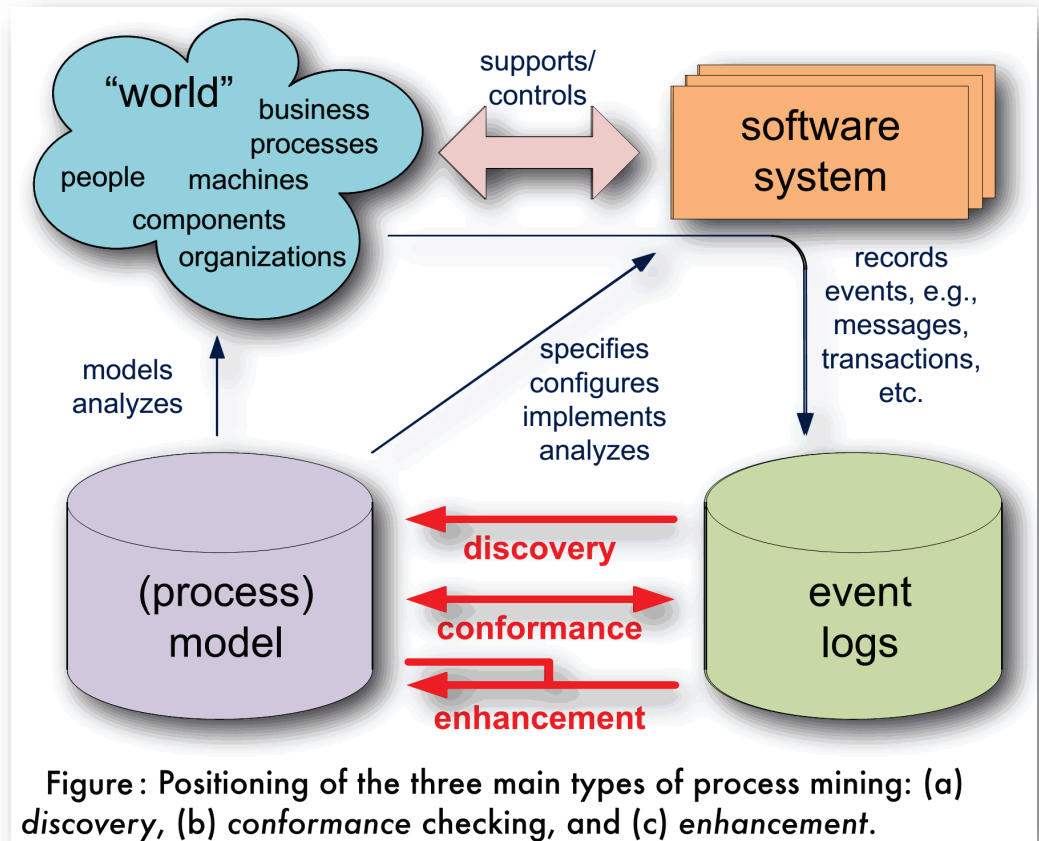
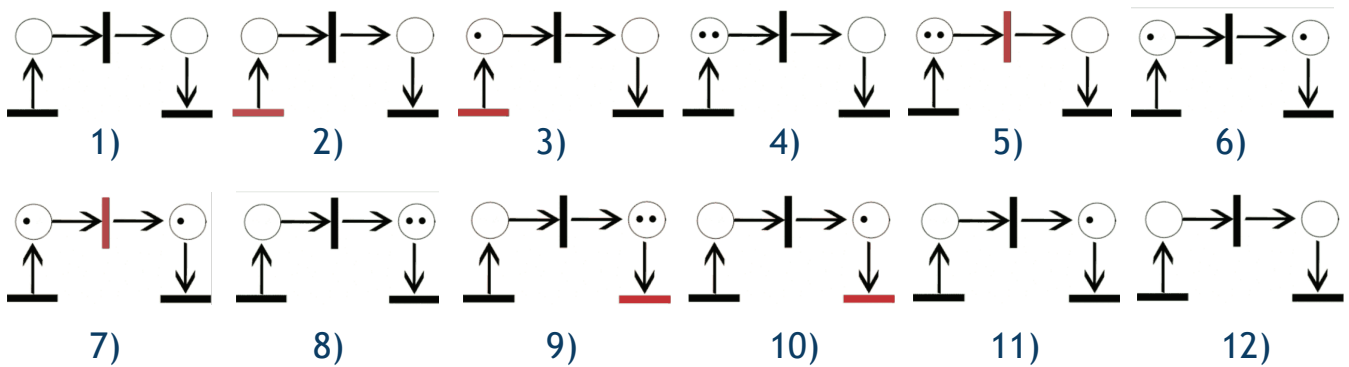


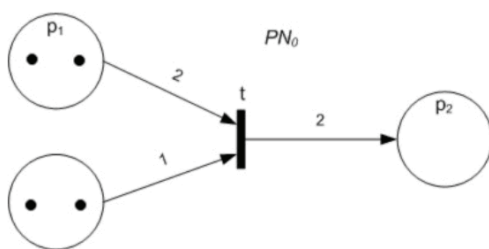
Figure: The BPM life-cycle identifying the various phases of a business process and its corresponding information system(s); process mining (potentially) plays a role in all phases (except for the implementation phase).

- **Petri net**, a mathematical modeling language for describing distributed systems. It is a bipartite graph in which nodes represents **transitions** and **places**, connected by arcs.

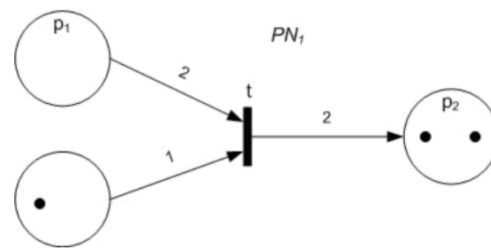


- a **transition** is an event that may occur, and is represented by a bar
- a **place** is a condition and is represented by a circle
- **arcs** run from a place to a transition (input place) or vice versa (output place), never between places or between transitions
- places may contain a discrete number of marks called **tokens**. A distribution of tokens over the places represents a configuration (marking) of the net
- a transition is fired if it is enabled, i.e., there are sufficient tokens in all of its input places. When the transition fires it consumes the required input tokens and created tokens in its output places. A firing is atomic (single non interruptible step).
- Unless otherwise specified, when multiple transitions are enabled at the same time, any one of them may fire (non determinism).

- In **pure petri nets** the behavior can be specified with **arc multiplicities**: a transition  $t$  is enabled at marking  $m$  if every input place  $p$  of  $t$  contains at least as many tokens as the multiplicity of the arc from  $p$  to  $t$  is.

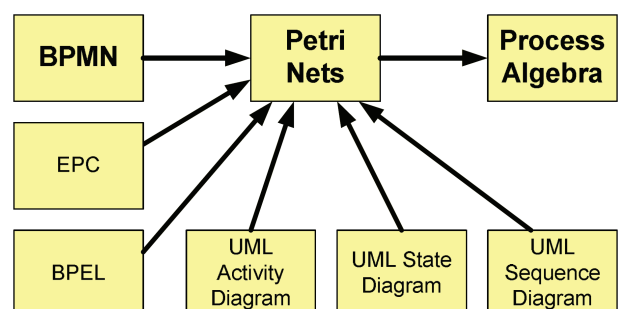


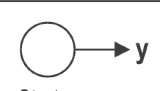
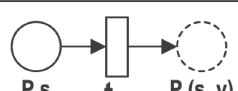

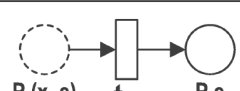
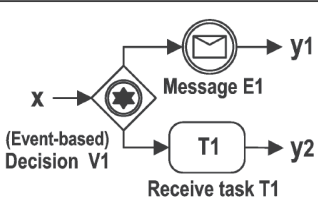
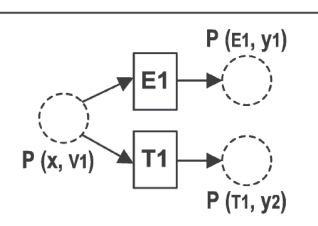

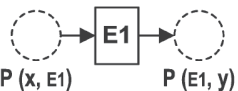
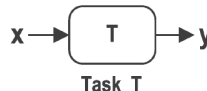
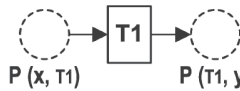
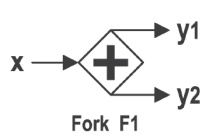
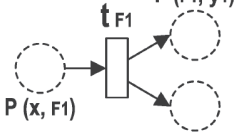
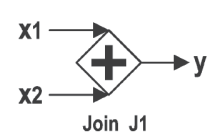
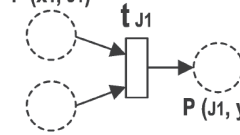
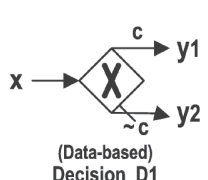
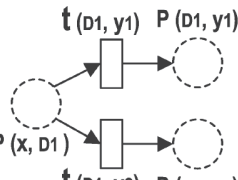
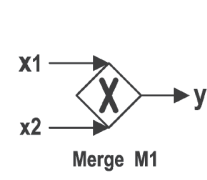
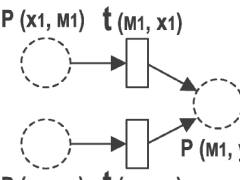
A Petri net with an enabled transition.



The Petri net that follows after the transition fires (Initial Petri net in the figure above).

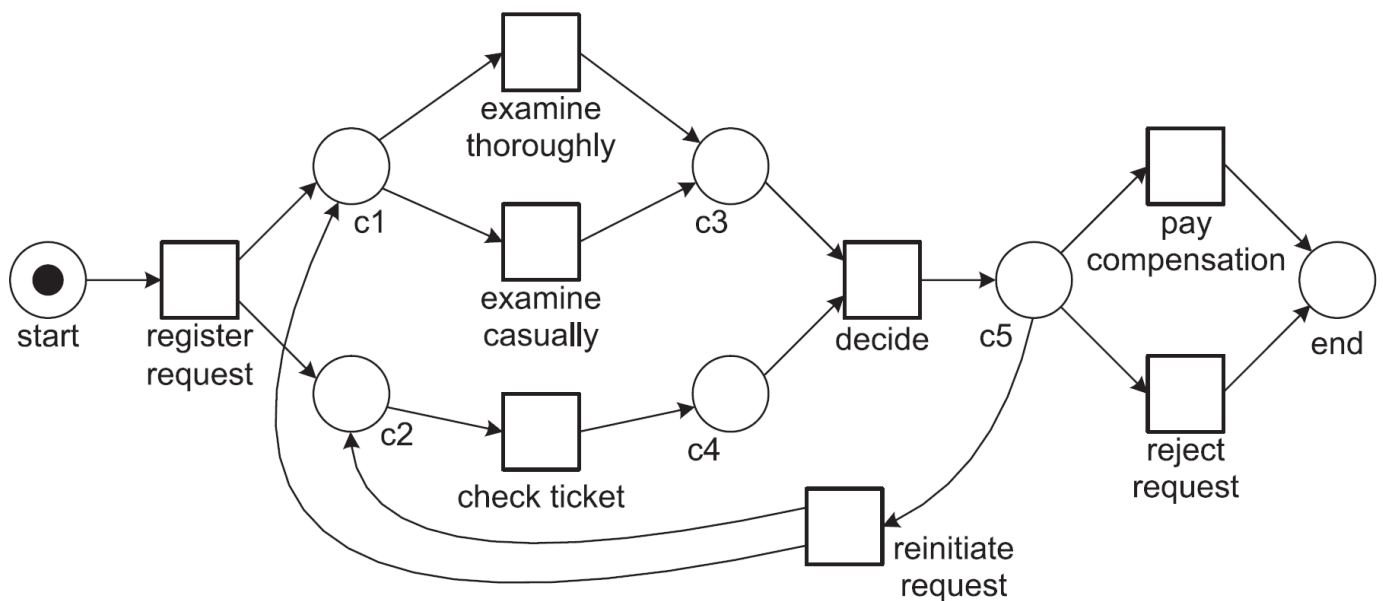
- Extended Petri exist, e.g, coloured petri nets are a backward compatible extension allowing the distinction between tokens with data values attached.
- **Model transformations** provide a wide range of techniques for model analysis on business processes used in industry. **Process algebra** is a family of formal approaches used in computer science to model concurrent systems. It provides algebraic laws to manipulate, analyze and permit formal reasoning about processes, and are at the core of process software engines.



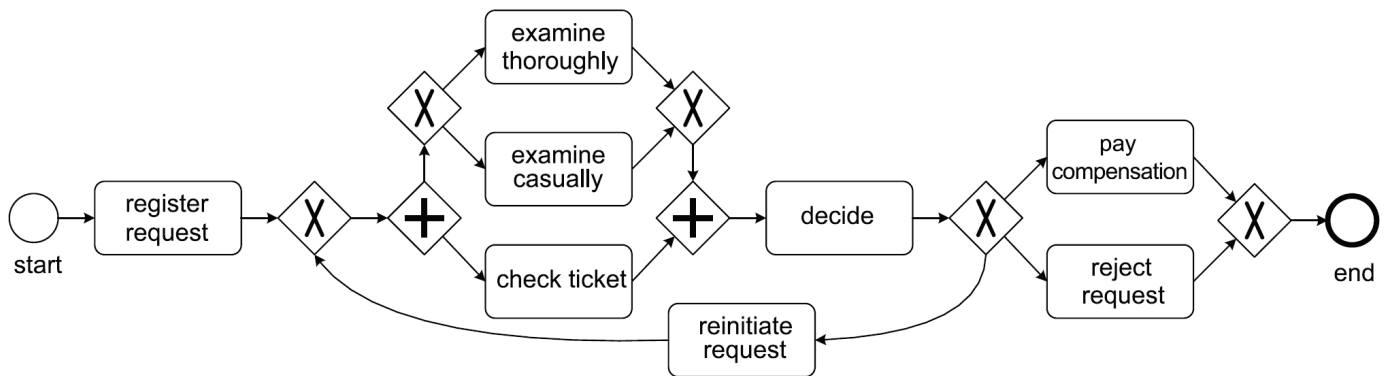
BPMN Object	Petri-net Module	BPMN Object	Petri-net Module	BPMN Object	Petri-net Module
 <p>Start s</p>	 <p><math>P_s</math> <math>t_s</math> <math>P(s, y)</math></p>	 <p>End e</p>	 <p><math>P(x, e)</math> <math>t_e</math> <math>P_e</math></p>	 <p>Message E1                  (Event-based) Decision V1                  Receive task T1</p>	 <p><math>P(x, V1)</math> <math>E1</math> <math>P(E1, y1)</math>  <math>T1</math> <math>P(T1, y2)</math></p>
 <p>Message E</p>	 <p><math>P(x, E1)</math> <math>E1</math> <math>P(E1, y)</math></p>	 <p>Task T</p>	 <p><math>P(x, T1)</math> <math>T1</math> <math>P(T1, y)</math></p>		
 <p>Fork F1</p>	 <p><math>P(x, F1)</math> <math>t_{F1}</math> <math>P(F1, y1)</math>  <math>P(F1, y2)</math></p>	 <p>Join J1</p>	 <p><math>P(x1, J1)</math> <math>t_{J1}</math> <math>P(J1, y)</math>  <math>P(x2, J1)</math></p>		
 <p>(Data-based) Decision D1</p>	 <p><math>P(x, D1)</math> <math>t_{(D1, y1)}</math> <math>P(D1, y1)</math>  <math>t_{(D1, y2)}</math> <math>P(D1, y2)</math></p>	 <p>Merge M1</p>	 <p><math>P(x1, M1)</math> <math>t_{(M1, x1)}</math> <math>P(M1, y)</math>  <math>P(x2, M1)</math> <math>t_{(M1, x2)}</math></p>		

[ Note ]:  
 x, x1 or x2 represents an input object, and y, y1 or y2 represents an output object.

Mapping task, events, and gateways onto Petri-net modules



A Petri net modeling the handling of compensation requests



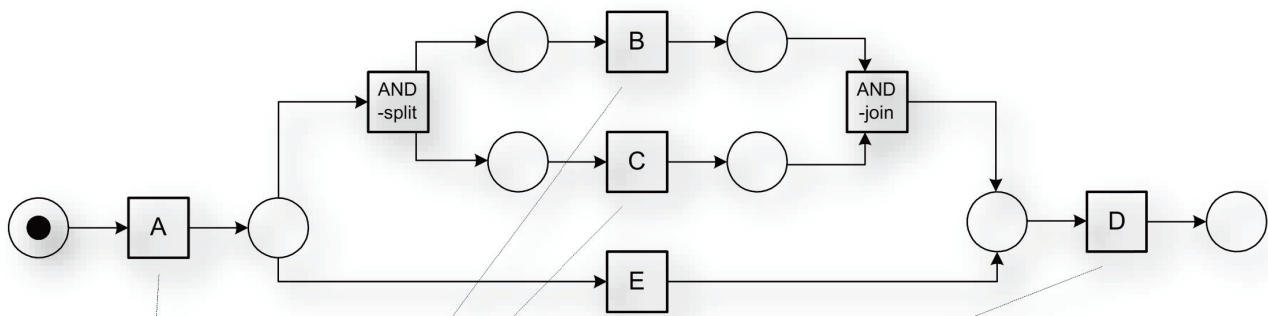
The same process modeled in terms of BPMN

PM is not limited to workflow, it covers different perspectives:

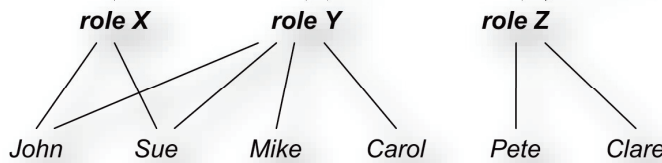
- a) **control-flow perspective:** focuses on the ordering of activities, with the purpose of finding a good characterization of all possible paths.
- b) **organizational perspective:** focuses on resources, the goal is to either structure the organization by classifying people in terms of roles and organizational units or to show the business network.
- c) **case perspective:** focuses on properties of cases: the case path in the process, the actors working on it, the values of the corresponding data objects.
- d) **time perspective** is concerned with discovering bottlenecks, measuring service levels, monitoring resources utilization, predicting the remaining processing time of running cases.

An event log

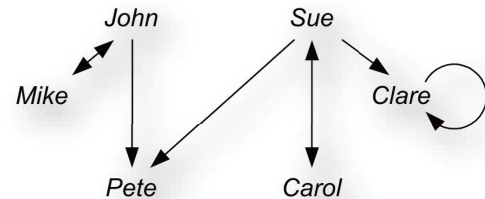
case id	activity id	originator	time stamp
case 1	activity A	John	9-3-2004:15.01
case 2	activity A	John	9-3-2004:15.12
case 3	activity A	Sue	9-3-2004:16.03
case 3	activity B	Carol	9-3-2004:16.07
...	...	...	...



(a) The control-flow structure expressed in terms of a Petri net.



(b) The organizational structure expressed in terms of an activity-role-performer diagram.



(c) A sociogram based on transfer of work.

**Fig.** Some mining results for the process perspective (a) and organizational (b and c) perspective based on the event log shown.

• Starting point for PM is a collection of events (events log), which may be stored in database tables, message logs, mail archives, transaction logs, and other data sources. More important than the storage is their quality.

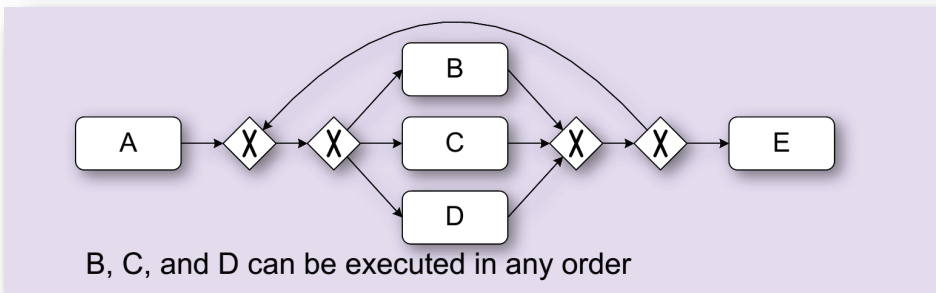
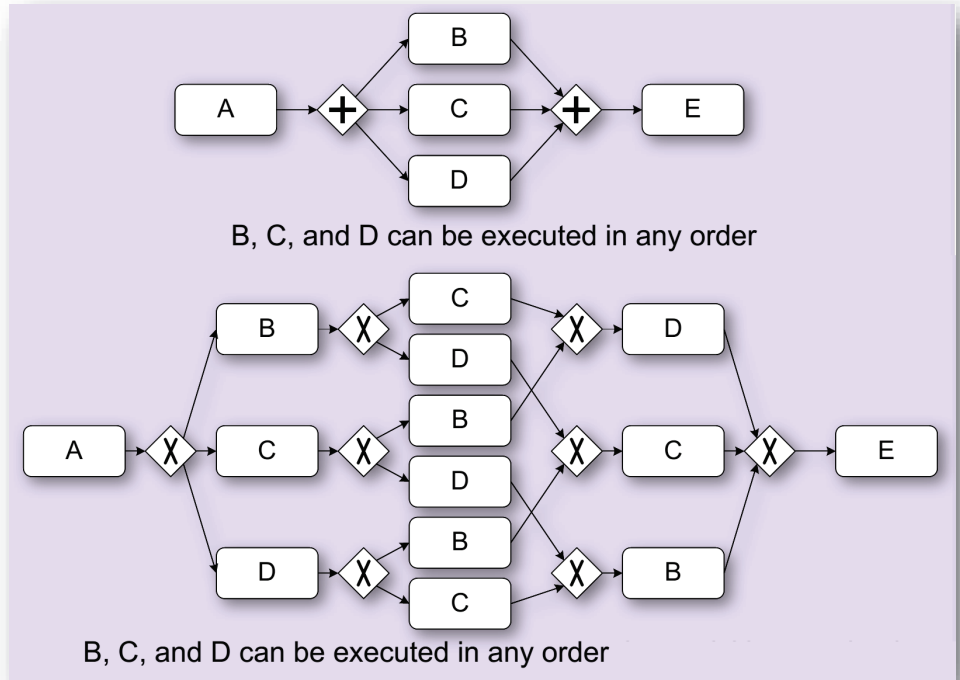
Level	Characterization	Examples
★★★★★	Highest level: the event log is of excellent quality (i.e., trustworthy and complete) and events are well-defined. Events are recorded in an automatic, systematic, reliable, and safe manner. Privacy and security considerations are addressed adequately. Moreover, the events recorded (and all of their attributes) have clear semantics. This implies the existence of one or more ontologies. Events and their attributes point to this ontology.	Semantically annotated logs of BPM systems.
★★★★	Events are recorded automatically and in a systematic and reliable manner, i.e., logs are trustworthy and complete. Unlike the systems operating at level ★★★★★, notions such as process instance (case) and activity are supported in an explicit manner.	Events logs of traditional BPM/workflow systems.
★★★	Events are recorded automatically, but no systematic approach is followed to record events. However, unlike logs at level ★★, there is some level of guarantee that the events recorded match reality (i.e., the event log is trustworthy but not necessarily complete). Consider, for example, the events recorded by an ERP system. Although events need to be extracted from a variety of tables, the information can be assumed to be correct (e.g., it is safe to assume that a payment recorded by the ERP actually exists and vice versa).	Tables in ERP systems, event logs of CRM systems, transaction logs of messaging systems, event logs of high-tech systems, etc.
★★	Events are recorded automatically, i.e., as a by-product of some information system. Coverage varies, i.e., no systematic approach is followed to decide which events are recorded. Moreover, it is possible to bypass the information system. Hence, events may be missing or not recorded properly.	Event logs of document and product management systems, error logs of embedded systems, worksheets of service engineers, etc.
★	Lowest level: event logs are of poor quality. Recorded events may not correspond to reality and events may be missing. Event logs for which events are recorded by hand typically have such characteristics.	Trails left in paper documents routed through the organization ("yellow notes"), paper-based medical records, etc.

Table: Maturity levels for event logs.

- Starting PM need to be driven by **questions**. Without concrete questions it is very difficult to extract meaningful events from tables of a database.
- As event logs contain only sample behavior, they should not be assumed to be complete. **Open world assumption**: the fact that something did not happen does not mean that it cannot happen.

• The **simplest** model that can explain the behavior seen in the log is the best model (**Occam's Razor principle**)

- Consider an event log  $L = \{$   
 $\langle A, B, C, D, E \rangle,$   
 $\langle A, B, D, C, E \rangle,$   
 $\langle A, C, B, D, E \rangle,$   
 $\langle A, C, D, B, E \rangle,$   
 $\langle A, D, B, C, E \rangle,$   
 $\langle A, D, C, B, E \rangle \}$



• But cases such as  $\langle A, B, B, B, E \rangle$  are possible according to the model but are not likely according to the event log.

- Noise and incompleteness make process discovery a challenging problem. There are four competing model quality dimensions:
  - fitness**: to allow for most of the behavior seen in the event log,
  - simplicity**: to allow for the most compact representation of the log
  - precision**: it does not allow for too much extra behavior w.r.t the log
  - generalization**: it does not restrict behavior to just the log

• A model that is not precise is "underfitting". A model that does not generalize is "overfitting".

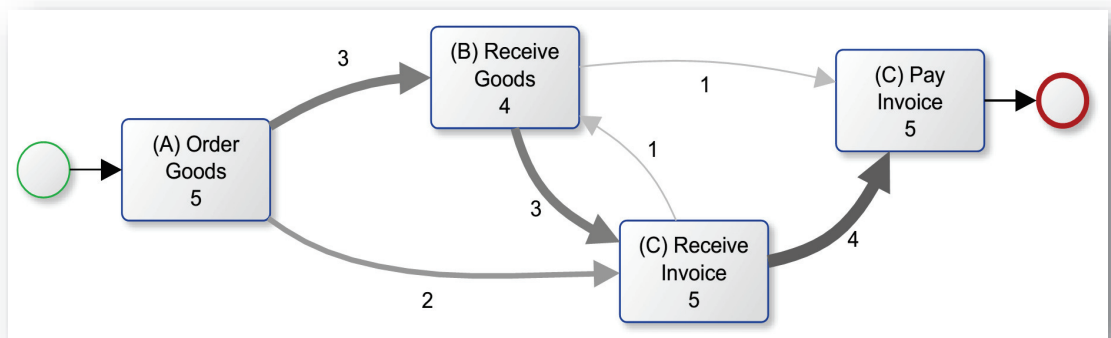
• Balancing fitness, simplicity, precision and generalization is challenging. This is the reason that most of the more powerful process discovery techniques provide various parameters.

• Three important categories of mining algorithms:

- i) **Deterministic** mining algorithm: it always delivers the same result for the same input. e.g. the alpha-algorithm (Van der Aalst et al. 2002).
- ii) **Heuristic** mining algorithm: it also uses deterministic algorithms but they incorporate frequencies of events and traces for reconstructing a process model, disregarding infrequent paths in order to manage complexity.
- iii) **Genetic** mining algorithm: it uses an evolutionary approach to find a satisfactory solution by iteratively selecting individuals and reproducing them by crossover and mutation over different generations.

E.g. **Heuristic Fuzzy Miner** algorithm (Günther and Van der Aalst 2007), which does not follow the BPMN notation but uses a **dependency graph**:

it does not contain gateways but shows only dependencies between activities.



Process Mining tools

• **ProM**: a major academic tool providing many different mining algorithms, analysis, conversion and export modules.

• **Disco**: intuitive and usable application. It provides integrated

functionality for filtering and loading of event logs. It is especially suited for novel users. Non-commercial license is for academic institutions.

• Most used formats: **CSV**(comma separated values), **MXML** (Mining eXtensible Markup Language) and its successor, **XES** (eXtensible Event Stream)

• No support for the extraction of event data from source systems: data has to be extracted with specialized data extraction software or by using export functionalities of the source systems.

Process Mining Tools

Product Name	Type <sup>6</sup>	Link
ARIS Process Performance Manager	C	<a href="http://www.softwareag.com">www.softwareag.com</a>
celonis business intelligence (SAP)	C	<a href="http://www.celonis.de">www.celonis.de</a>
Disco	C	<a href="http://www.fluxicom.com">www.fluxicom.com</a>
Genet/Petrify	O	<a href="http://www.lsi.upc.edu">www.lsi.upc.edu</a>
Interstage Business Process Manager	C	<a href="http://www.fujitsu.com">www.fujitsu.com</a>
QPR ProcessAnalyzer	C	<a href="http://www.gqr.com">www.gqr.com</a>
ProM	O	<a href="http://www.processmining.org">www.processmining.org</a>
ProcessGold	C	<a href="http://www.processgold.de">www.processgold.de</a>
Rbminer/Dbminer	O	<a href="http://www.lsi.upc.edu">www.lsi.upc.edu</a>
ReflectOne	C	<a href="http://www.pallas-athena.com">www.pallas-athena.com</a>
ServiceMosaic	O	<a href="http://soc.cse.unsw.edu.au">soc.cse.unsw.edu.au</a>

C = commercial, O = open source



- Event logs contain a set of events. A single event has a unique event ID, it refers to one individual case, it has a timestamp, and it shows which resources executed which task. It is a minimum requirement that the events refer to (i) one case, (ii) one task, and (iii) a point in time.

Case ID	Event ID	Timestamp	Activity	Resource
1	Ch-4680555556-1	2012-07-30 11:14	Check stock availability	SYS1
1	Re-5972222222-1	2012-07-30 14:20	Retrieve product from warehouse	Rick
1	Co-6319444444-1	2012-07-30 15:10	Confirm order	Chuck
1	Ge-6402777778-1	2012-07-30 15:22	Get shipping address	SYS2
1	Em-6555555556-1	2012-07-30 15:44	Emit invoice	SYS2
1	Re-4180555556-1	2012-08-04 10:02	Receive payment	SYS2
1	Sh-4659722222-1	2012-08-05 11:11	Ship product	Susi
1	Ar-3833333333-1	2012-08-06 09:12	Archive order	DMS
2	Ch-4055555556-2	2012-08-01 09:44	Check stock availability	SYS1
2	Ch-4208333333-2	2012-08-01 10:06	Check materials availability	SYS1
2	Re-4666666667-2	2012-08-01 11:12	Request raw materials	Ringo
2	Ob-3263888889-2	2012-08-03 07:50	Obtain raw materials	Olaf
2	Ma-6131944444-2	2012-08-04 14:43	Manufacture product	SYS1
2	Co-6187615741-2	2012-08-04 14:51	Confirm order	Conny
2	Em-6388888889-2	2012-08-04 15:20	Emit invoice	SYS2
2	Ge-6439814815-2	2012-08-04 15:27	Get shipping address	SYS2
2	Sh-7277777778-2	2012-08-04 17:28	Ship product	Sara
2	Re-3611111111-2	2012-08-07 08:40	Receive payment	SYS2
2	Ar-3680555556-2	2012-08-07 08:50	Archive order	DMS
3	Ch-4208333333-3	2012-08-02 10:06	Check stock availability	SYS1
3	Ch-4243055556-3	2012-08-02 10:11	Check materials availability	SYS1

Process Discovery: the  $\alpha$ -algorithm

- It is a basic deterministic mining algorithm. Assumptions:
  - (1) the events in the log are chronologically ordered.
  - (2) each event refers to a single case.
  - (3) each event relates to a specific activity of the process.
  - (4) each activity of the process is included in the log.
  - (5) the log is **behaviorally complete** in the sense that if an activity *a* can be

directly followed by an activity *b*, then there is at least one case in the log where we observe *ab*.

Case ID	Event ID	Timestamp	Activity
1	Ch-468	2012-07-30 11:14	Check stock availability
1	Re-597	2012-07-30 14:20	Retrieve product from warehouse
1	Co-631	2012-07-30 15:10	Confirm order
1	Ge-640	2012-07-30 15:22	Get shipping address
1	Em-655	2012-07-30 15:44	Emit invoice
1	Re-418	2012-08-04 10:02	Receive payment
1	Sh-465	2012-08-05 11:11	Ship product
1	Ar-383	2012-08-06 09:12	Archive order
2	Ch-405	2012-08-01 09:44	Check stock availability
2	Ch-420	2012-08-01 10:06	Check materials availability
2	Re-466	2012-08-01 11:12	Request raw materials
2	Ob-326	2012-08-03 07:50	Obtain raw materials
2	Ma-613	2012-08-04 14:43	Manufacture product
2	Co-618	2012-08-04 14:51	Confirm order
2	Em-638	2012-08-04 15:20	Emit invoice
2	Ge-643	2012-08-04 15:27	Get shipping address
2	Sh-727	2012-08-04 17:28	Ship product
2	Re-361	2012-08-07 08:40	Receive payment
2	Ar-368	2012-08-07 08:50	Archive order

Letter	Activities
a	Check stock availability
b	Retrieve product from warehouse
c	Check materials availability
d	Request raw materials
e	Obtain raw materials
f	Manufacture product
g	Confirm order
h	Get shipping address
i	Ship product
j	Emit invoice
k	Receive payment
l	Archive order

**Workflow Log**  
 a,b,g,h,j,k,i,l  
 a,c,d,e,f,g,j,h,i,k,l  
 ...

- The starting point is to build the workflow log



- Order relations are easily derived by using the footprint matrix of the log:

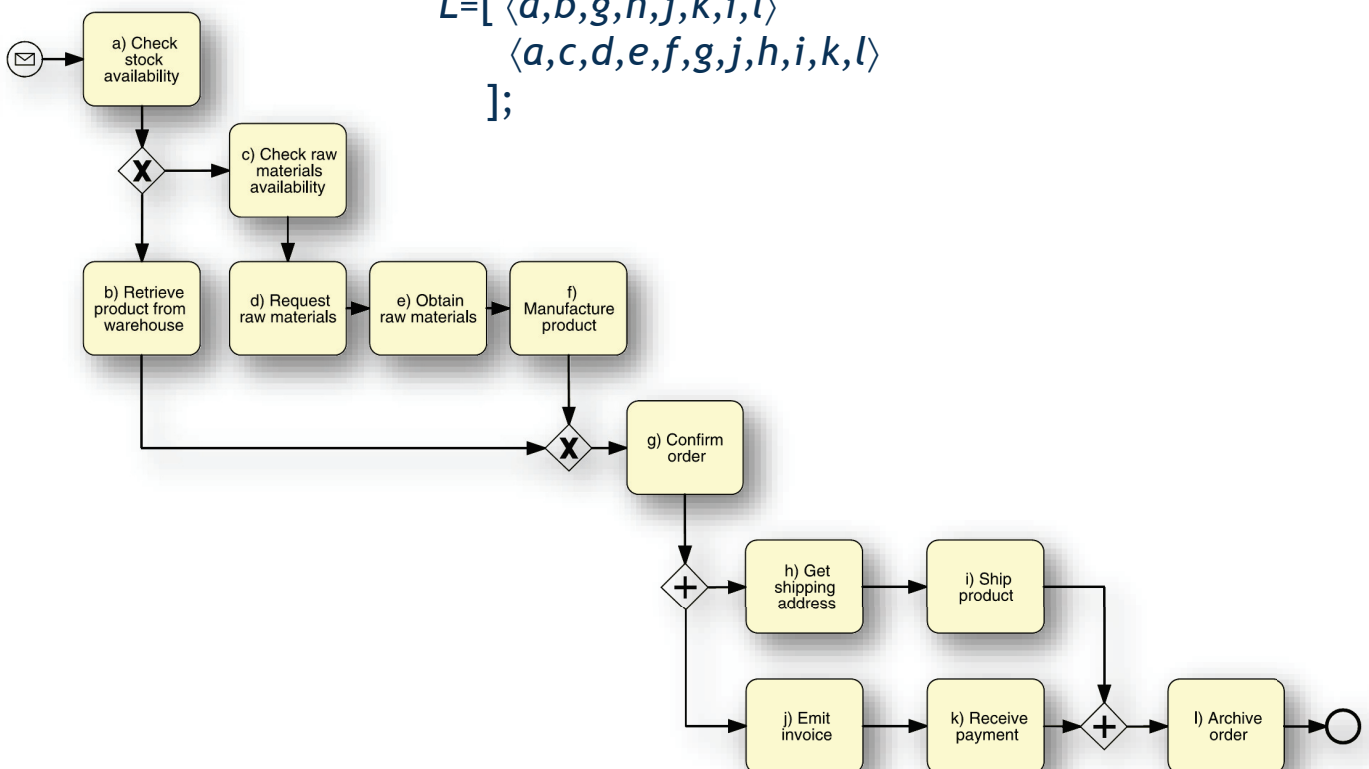
• Fig. Footprint represented as a matrix of the workflow log

$L = [ \langle a, b, g, h, j, k, i, l \rangle \langle a, c, d, e, f, g, j, h, i, k, l \rangle ]$ ,

	a	b	c	d	e	f	g	h	i	j	k	l
a	#	→	→	#	#	#	#	#	#	#	#	#
b	←	#	#	#	#	#	→	#	#	#	#	#
c	←	#	#	→	#	#	#	#	#	#	#	#
d	#	#	←	#	→	#	#	#	#	#	#	#
e	#	#	#	←	#	→	#	#	#	#	#	#
f	#	#	#	#	←	#	→	#	#	#	#	#
g	#	←	#	#	#	←	#	→	#	→	#	#
h	#	#	#	#	#	#	←	#	→		#	#
i	#	#	#	#	#	#	#	←	#	#		→
j	#	#	#	#	#	#	←		#	#	→	#
k	#	#	#	#	#	#	#	#		←	#	→
l	#	#	#	#	#	#	#	#	←	#	←	#

- Process model constructed by the  $\alpha$ -algorithm from workflow log

$L = [ \langle a, b, g, h, j, k, i, l \rangle \langle a, c, d, e, f, g, j, h, i, k, l \rangle ]$ ;

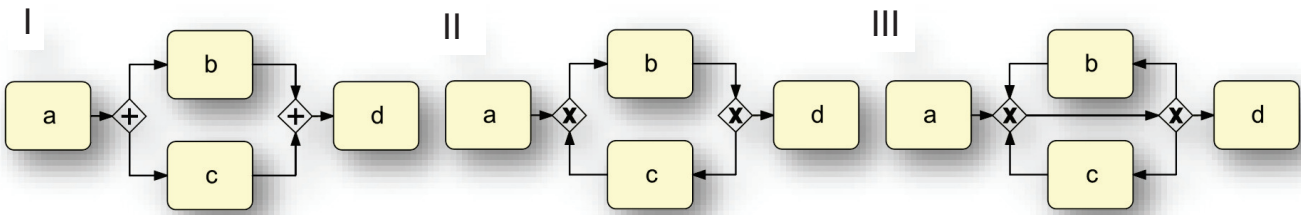


- *Limitations of the  $\alpha$ -algorithm*: it is not able to distinguish *short loops* from true parallelism:

I: *abcd, acbd*

II: *abd, <sup>b</sup>abcd, abc<sup>b</sup>d*

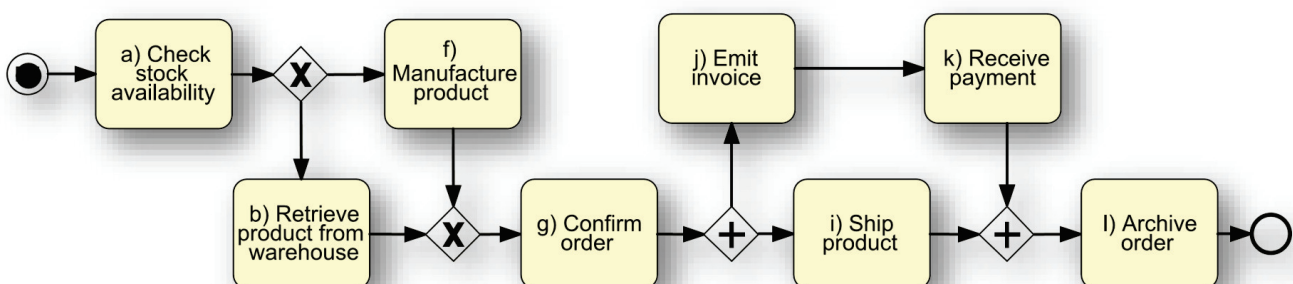
III: *ad, abd, <sup>b</sup>abcd, ac<sup>b</sup>d*



**Fig.** Examples of two short loops, which are problematic for the  $\alpha$ -algorithm

- All three models above can produce the workflow logs that yield  $b||c$ , because both  $bc$  and  $cb$  can be observed.
- To distinguish (I) and (II), in the  $\alpha$ +algorithm extension  $b||c$  is only included if there is no sequence  $bc b$  in the logs. Preprocessing can be also used to collapse repetitions (like  $aa$  and  $bb$ ) to a single execution.
- Further problems for the  $\alpha$ -algorithm are *incompleteness* and *noise*. E.g. to determine potential parallelism in 10 concurrent tasks, the number of required different cases to observe is  $10! = 3,268,800$ . Moreover, event logs often include cases with missing head, tail, intermediate episode, logging errors with events being swapped or recorded twice.

- ✓ Conformance checking is concerned with the question whether or not the execution of a process (i.e., event logs) follows constraints.
- ✓ We focus on constraints expressed as a *normative process model*. If a particular constraint does not hold, we speak of a *violation*.
- ✓ The idea is to *replay* each trace of the log recording at each step whether an activity is allowed to be executed according to the model.
- ✓ For example replay the case  $\langle a, b, g, i, j, k, l \rangle$  on the model shown in figure.



**Fig.** BPMN model with token on start event for replaying the case  $\langle a, b, g, i, j, k, l \rangle$

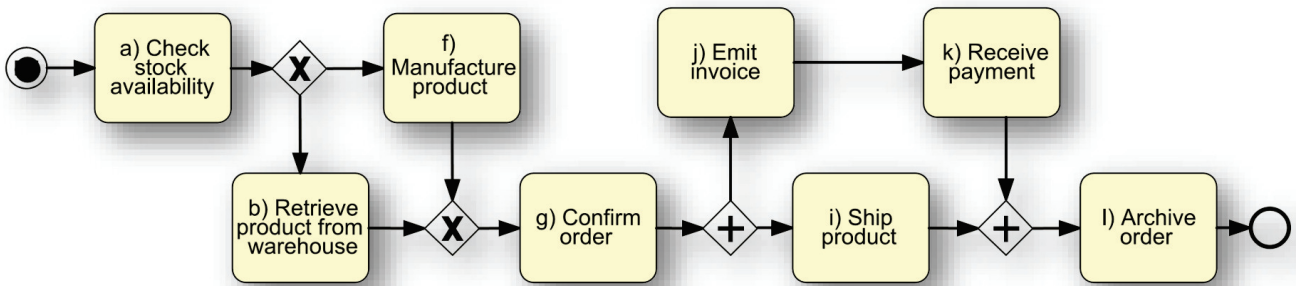
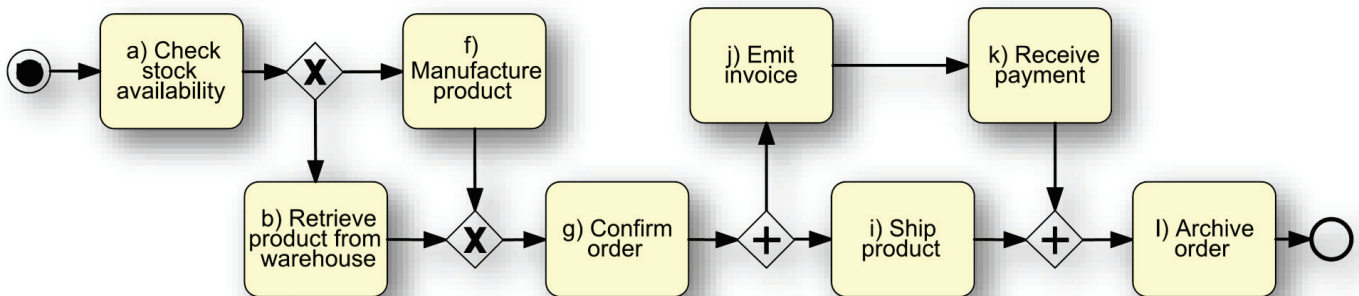


Fig. BPMN model with token on start event for replaying the case  $\langle a, b, g, i, j, k, l \rangle$

✓ In the initial state the process has a token on the start event, which leads to activity *a*. Then, the XOR-split is activated, which allows to either continue with *b* or with *f*. For the considered case, we can continue with *b*. Then, we can continue with *g*, after which the AND-split enables both *i* and *j*. These activities are concurrent. In order to replay the case, we first execute *i* and *j* afterwards. Once *i* and later *k* is completed, the AND-join is allowed to proceed. One token on each its input arcs is required for that. Since both of these tokens are consumed, a single token can be created to enable *l*, which can be finally executed. Thus, the case can be totally replayed on the model.



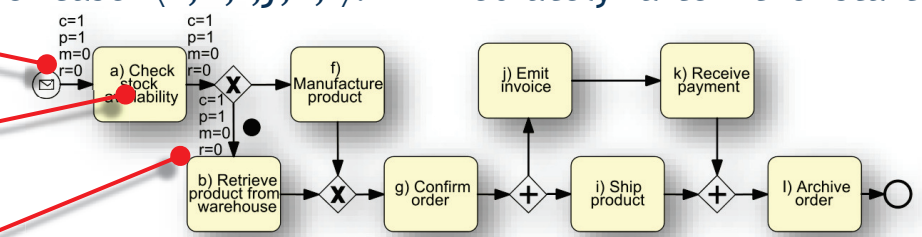
✓ Based on the concept of token replay, we can also assess the conformance of a trace to a process model.

✓ The idea is to compare at each step the number of tokens that are required for replaying an activity with the actually available tokens.

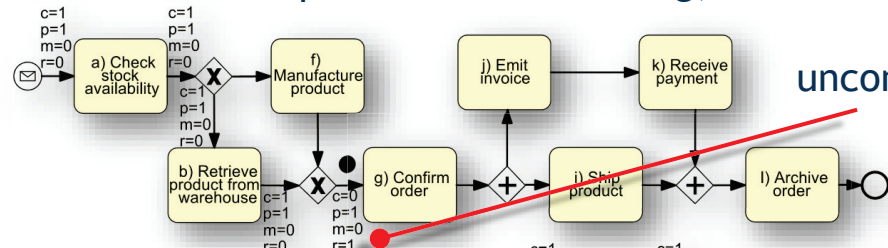
✓ At each step, we might observe situations of conformance and non-conformance. In case of conformance, we count the following four facts:

- *p*: # of output tokens correctly produced by a model element
- *c*: # of input tokens correctly consumed by a model element
- *m*: # of missing (unproduced) output tokens, e.g. because something did not occur
- *r*: # of input tokens remaining unconsumed, e.g. because something did not occur although the model expected it to happen

✓ Example. Consider the case  $\langle a, b, i, j, k, l \rangle$ . Immediately after the start event, one token is correctly produced and consumed. The same situation after replaying  $a$ .

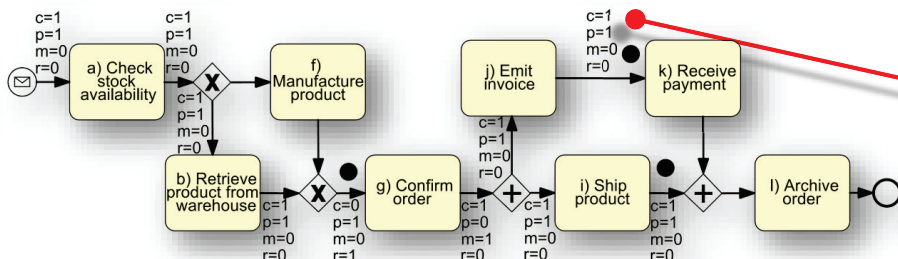
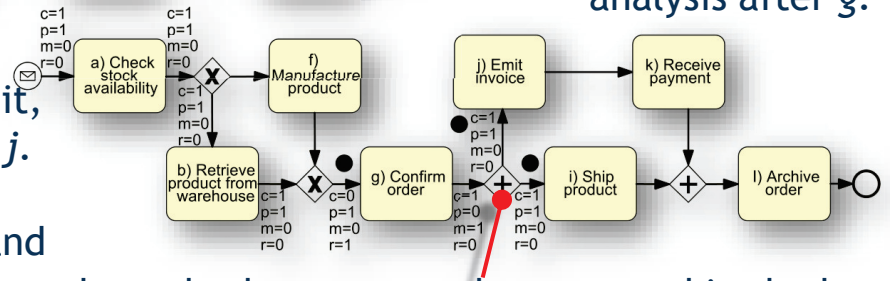


✓ Let us continue with  $b$  to check the considered case. After replaying  $b$ , there is a token produced to execute  $g$ , but it is not consumed by the case.



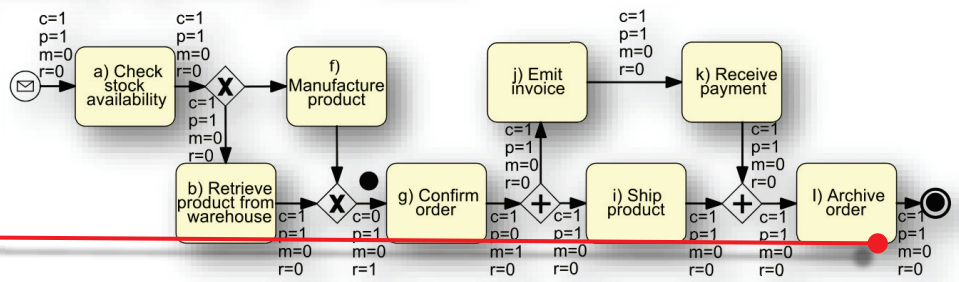
Thus, one token remains unconsumed before  $g$ , since  $g$  is not in the log for replay. Let us continue with the analysis after  $g$ .

After  $g$  there is a missing token for firing the AND-split, which would activate  $i$  and  $j$ . The AND-split can correctly consume the input token, and correctly produce the output tokens: both are correctly consumed in the log



✓ The token delivered by  $j$  can also be replayed by  $k$  in the case  $\langle a, b, i, j, k, l \rangle$ .

✓ The AND-join can synchronize  $k$  and  $i$ , and finally  $l$  can be also replayed in the log.



✓ We calculate the *fitness* of the case by using the fractions *missing-to-consumed* and *remaining-to-produced*:

$$fitness = \frac{1}{2} \left( 1 - \frac{m}{c} \right) + \frac{1}{2} \left( 1 - \frac{r}{p} \right)$$

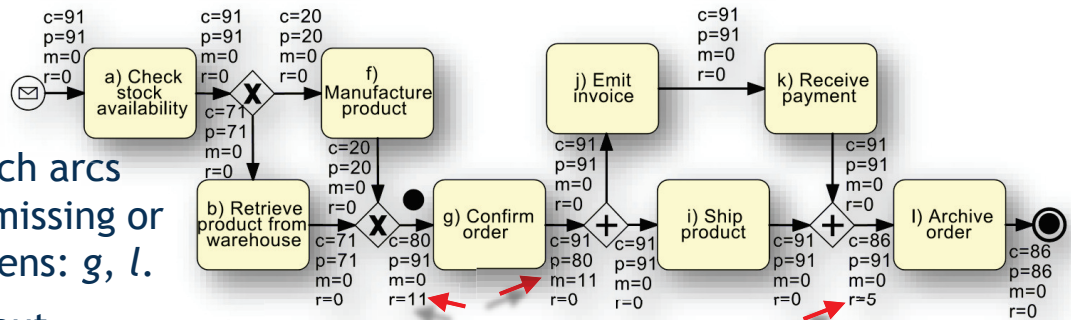
- $p$ : # of output tokens correctly produced
- $c$ : # of input tokens correctly consumed
- $m$ : # of missing (unproduced) output tokens
- $r$ : # of input tokens remaining unconsumed

$$p+m = c+r$$

✓ With  $m=1$  and  $r=1$ ,  $c=12$  and  $p=12$ ,  $fitness = (1-1/12)/2 + (1-1/12)/2 = 0.9166$

✓ With a set of cases: after replaying a case, continue counting  $c, p, m, r$  by replaying the next case in the process model. Once all cases have been replayed, get the resulting fitness with the same formula. Example in figure

$$p+m = c+r$$

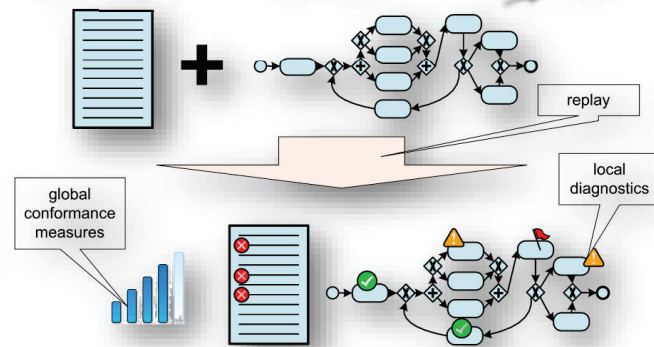


✓ Inspect which arcs encountered missing or remaining tokens:  $g, l$ .

✓ Given 91 input tokens, about 22% is handled via  $f$  and 78% via  $b$ .

✓ 12% omits  $g$  (11 tokens remaining/missing at the input/output of  $g$ )

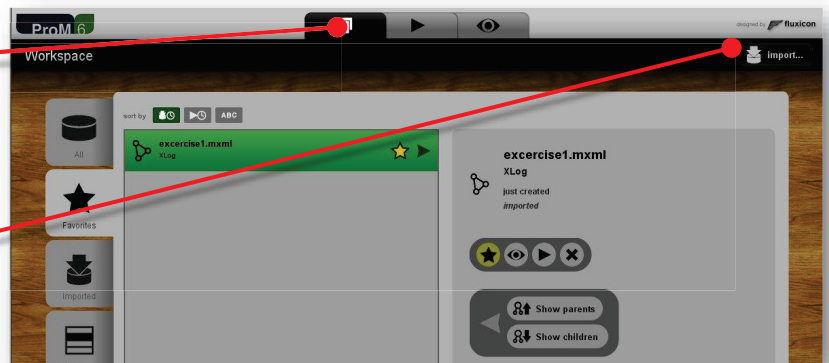
✓ 5.5% omits  $l$  (5 tokens remaining at the input of  $l$ )



Conclusion: conformance checking provides global conformance measures (like fitness) and local diagnostics

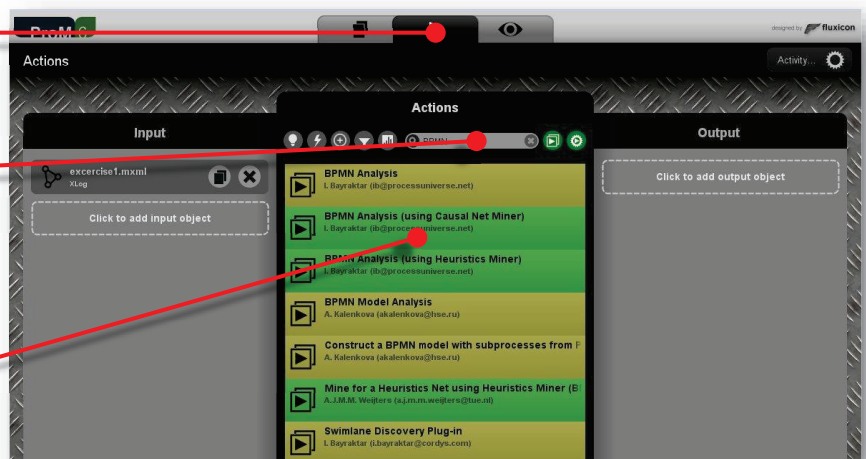
Process Mining tools: ProM 6.x

✓ *Workspace Tab* for input/output



✓ Click on import to load *exercise1.xes*

✓ *ActionTab* for executing algorithms



✓ Enter "BPMN" to select BPMN-based plugins

✓ Select "BPMN Analysis (using Causal Net Miner)" and press "Start"

### ✓ BPMN Analysis using Causal (C-) Net Miner

It is an advanced algorithm. How it works (in brief):

- A **C-net** is a representation of a process model as a graph, where nodes represent activities and arcs represent causal dependencies;
- **Cost-based fitness** is measured based on finding skipped/inserted activities giving minimal costs (highest possible fitness value), using **A\*** algorithm (heuristic variant of Dijkstra's algorithm) to find shortest paths between two nodes in a directed graph with arc costs;
- The cost function is provided with options to specify the relative costs of skipped / inserted activities
- A **projection** method is used to split the log into pieces: it selects groups of events tightly related in the log projecting the log on these events. Leave default values and click on "Continue".

**BPMN Analysis Settings**

**Projection Details**

Number of Most Frequent Path :

Number of Most Time Consuming Path :

Number of Least Frequent Path :

Number of Least Time Consuming Path :

### Introduction to Process Mining tools

- A wizard procedure to configure the replay process.

**Replay Log in Causal Net**

Map each node on the left side panel to a set of event class on the right side panel

E

B

A

C

D

**Replay Log in Causal Net**

**Introduction**

This wizard will guide you to configure this log replay. Configuring the replay consists of several tasks:

1. Mapping Flexible model's nodes to event class (if there is no such mapping yet), and
2. Select replay algorithm to be used.

The wizard will allow you to perform these tasks in the given order.

- Check the label match between node of the net and event classes. There can be additional nodes in the net, causing mismatch.

- Some algorithms are grounded on the theory of regions, which maps a model in the state based domain (automata) into the event-based domain (e.g Petri net). Leave default values and click "Next"

**Replay Log in Causal Net**

**Select Algorithm**

Select your replay algorithm.

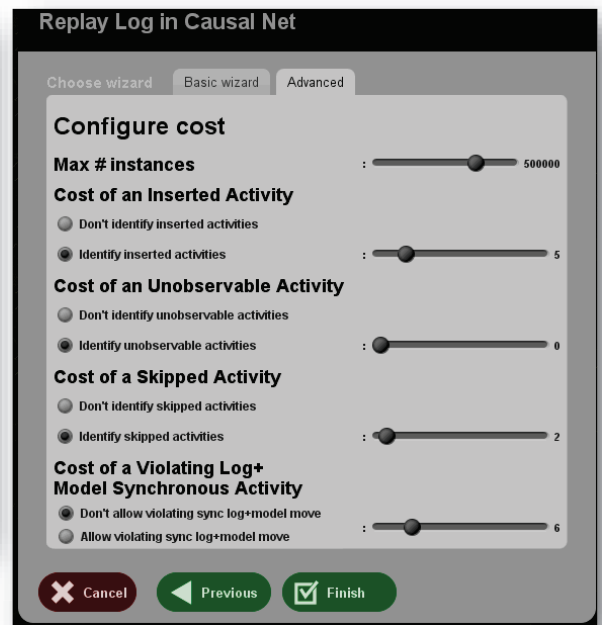
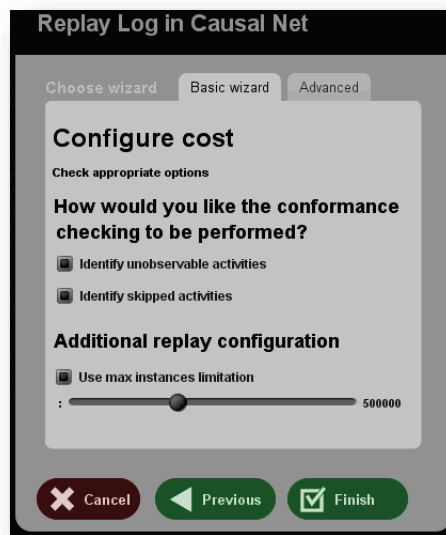
Cost-based A\* heuristic log replay

Cost-based A\* heuristic log replay

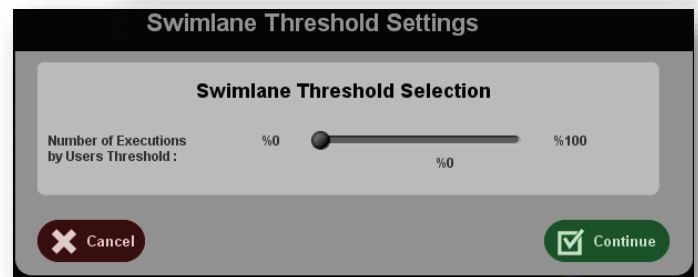
Cancellation-region-aware cost-based A\* heuristic log replay



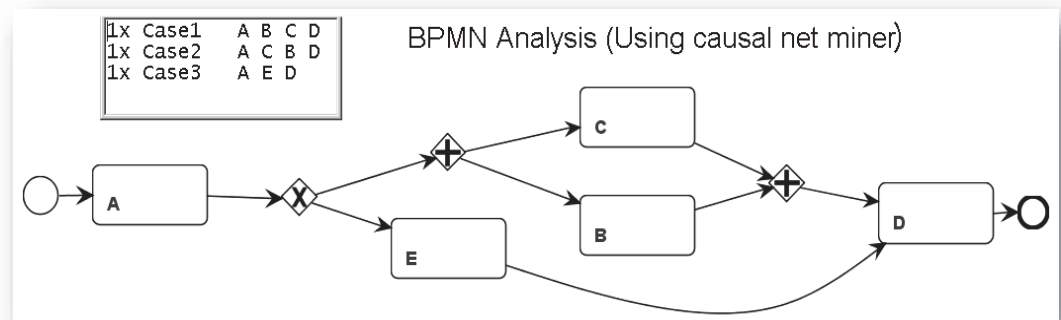
- The last part of the wizard relates to the cost configuration: leave the default values and press “Finish”.



- Finally, a threshold can be set to discover also swimlanes
- Leave the default values and press “Finish”/”Continue”.



- Exercise 1

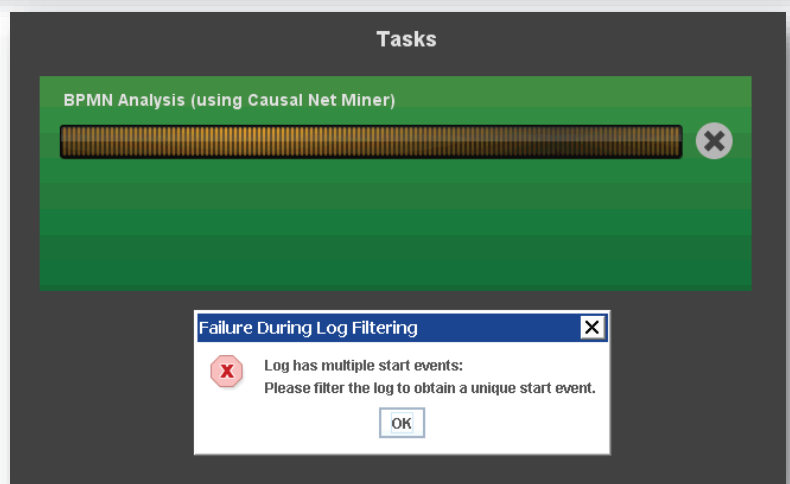


- Exercise 2

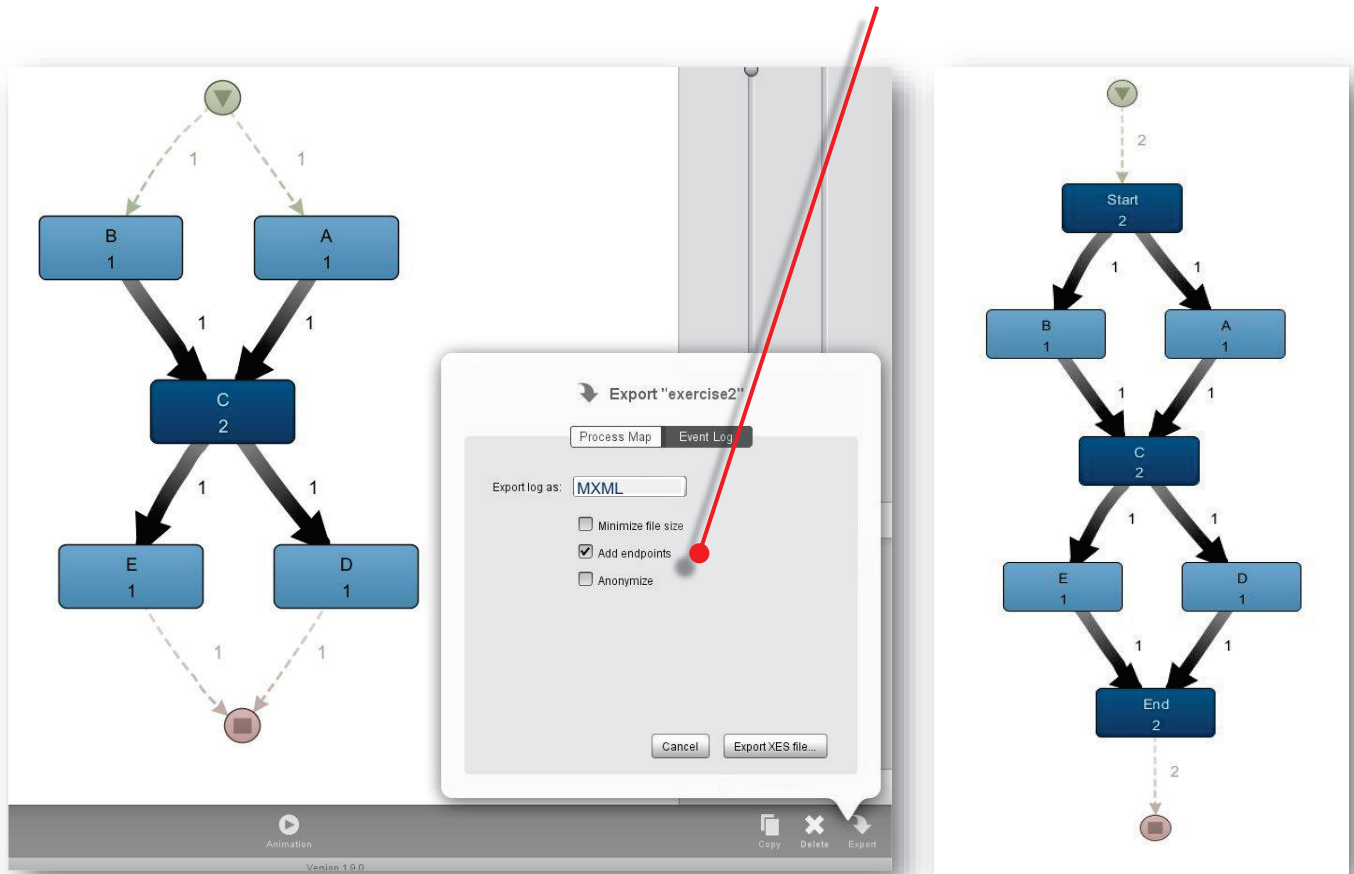
1x Case1	A C D
1x Case2	B C E

- The log cannot be processed, because it has multiple start events

- To add the Start/End events, you can use either DISCO or TEXTPAD

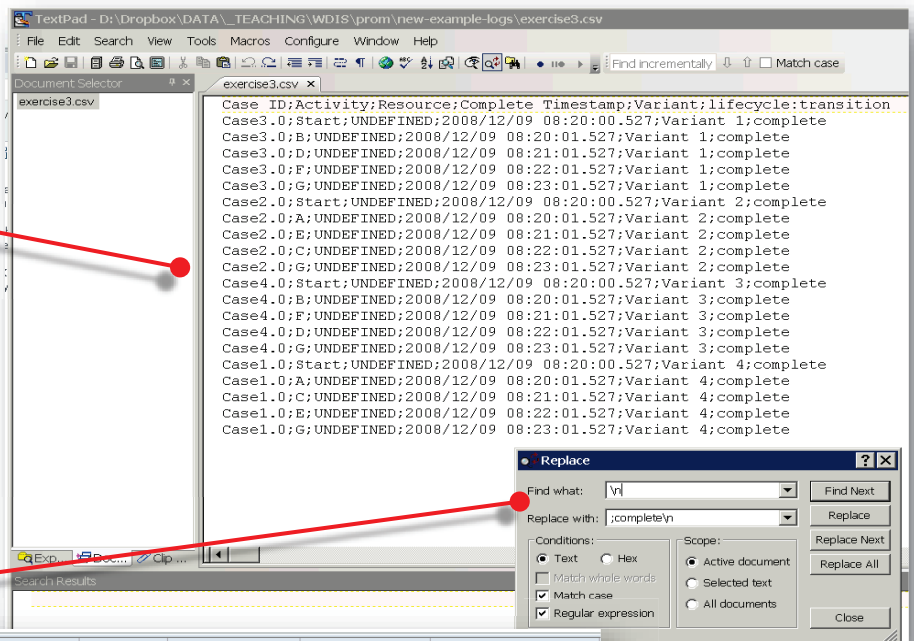


- With Disco, you can export the log by adding endpoints



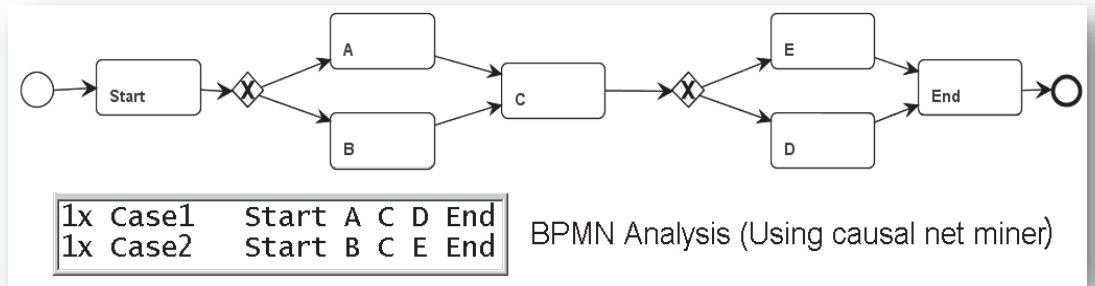
- To manually edit the log, convert it from MXML to CSV. Then edit it with Textpad or Excel and then use again Disco to convert it to MXML

- With Textpad regular expressions can be used

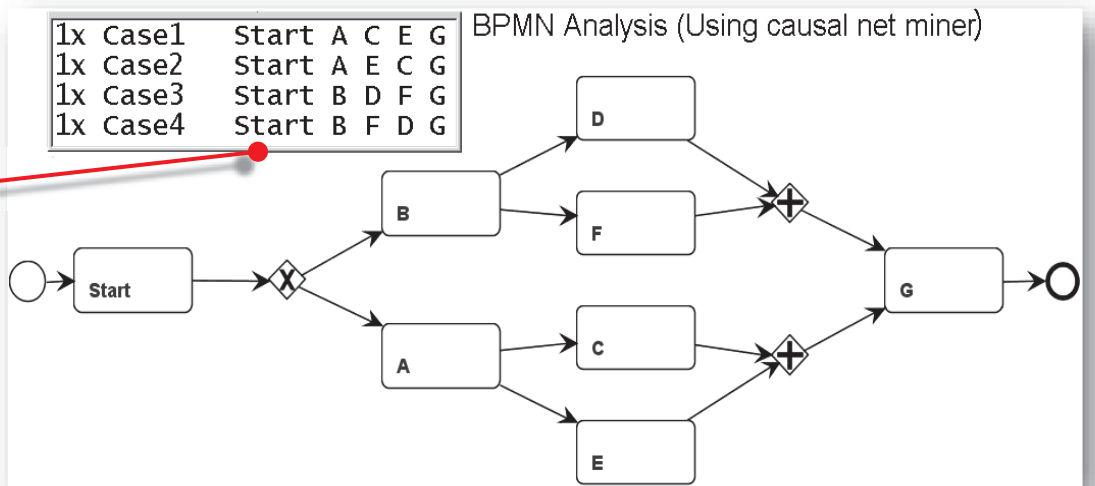


A	B	C	D	E	F	G	H
Case ID	Activity	Resource	Complete Timestamp	Variant	(case) creator	(case) variant	lifecycle:transition
Case2.0	Start	Start	2008/12/09 08:20:01.527	Variant 1	Fluxicon Disco	Variant 1	complete
Case2.0	B	UNDEFINED	2008/12/09 08:20:01.527	Variant 1	Fluxicon Disco	Variant 1	complete
Case2.0	C	UNDEFINED	2008/12/09 08:21:01.527	Variant 1	Fluxicon Disco	Variant 1	complete
Case2.0	E	UNDEFINED	2008/12/09 08:22:01.527	Variant 1	Fluxicon Disco	Variant 1	complete
Case2.0	End	End	2008/12/09 08:22:01.527	Variant 1	Fluxicon Disco	Variant 1	complete
Case1.0	Start	Start	2008/12/09 08:20:01.527	Variant 2	Fluxicon Disco	Variant 2	complete
Case1.0	A	UNDEFINED	2008/12/09 08:20:01.527	Variant 2	Fluxicon Disco	Variant 2	complete
Case1.0	C	UNDEFINED	2008/12/09 08:21:01.527	Variant 2	Fluxicon Disco	Variant 2	complete
Case1.0	D	UNDEFINED	2008/12/09 08:22:01.527	Variant 2	Fluxicon Disco	Variant 2	complete
Case1.0	End	End	2008/12/09 08:22:01.527	Variant 2	Fluxicon Disco	Variant 2	complete

• Exercise 2

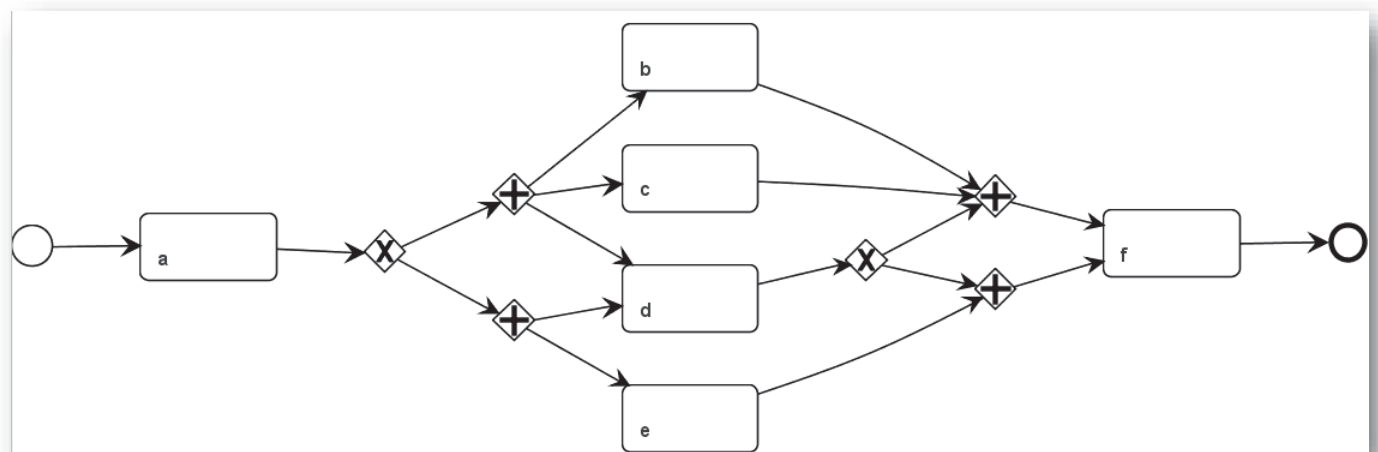


• Exercise 3  
(the Start event must be added)



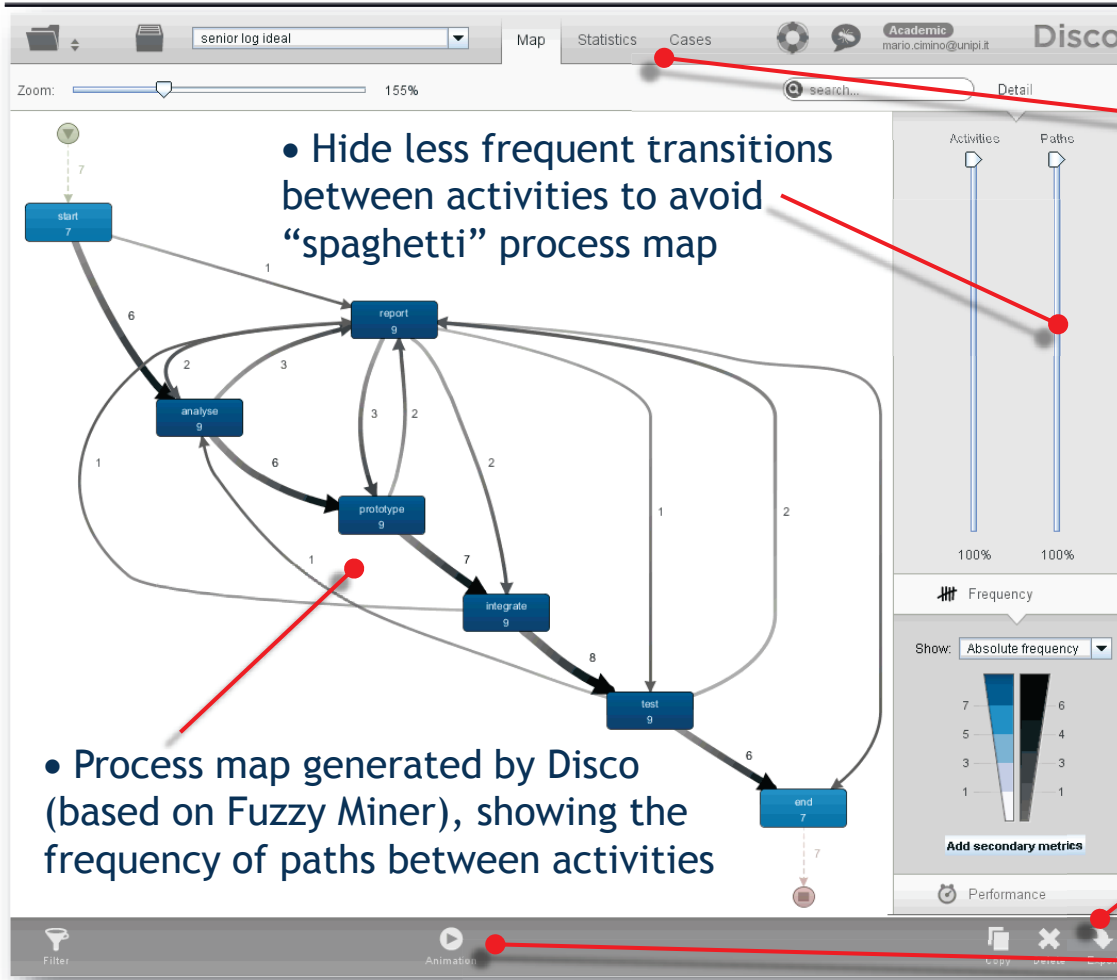
• Exercise 4

1x Case1	a	b	c	d	f
1x Case2	a	c	b	d	f
1x Case3	a	b	d	c	f
1x Case4	a	c	d	b	f
1x Case5	a	d	e	f	
1x Case6	a	e	d	f	



- SENIOR log (Software Engineering for Input/Output problems)
- It contains different cases of problem solving. Each case involves a worker improving the input/output (i/o) of a Java-based software application
- Synthetic log: cases without violations; the base pattern, iterated one or many times is  $(a \rightarrow p \rightarrow i \rightarrow t) \parallel r$

Case ID	Timestamp	Activity
4	05/02/2015 00.00	start
4	05/02/2015 01.00	analyse
4	05/02/2015 02.00	prototype
4	05/02/2015 03.00	integrate
4	05/02/2015 04.00	test
4	05/02/2015 05.00	report
4	05/02/2015 06.00	end
5	05/02/2015 00.00	start
5	05/02/2015 01.00	analyse
5	05/02/2015 02.00	prototype
5	05/02/2015 03.00	integrate
5	05/02/2015 04.00	test
5	05/02/2015 05.00	report
5	05/02/2015 07.00	analyse
5	05/02/2015 08.00	report
5	05/02/2015 09.00	prototype
5	05/02/2015 10.00	integrate
5	05/02/2015 11.00	test
5	05/02/2015 12.00	end
6	05/02/2015 00.00	start
6	05/02/2015 01.00	analyse
6	05/02/2015 02.00	report
6	05/02/2015 03.00	prototype
6	05/02/2015 04.00	integrate
6	05/02/2015 05.00	test
6	05/02/2015 06.00	analyse
6	05/02/2015 07.00	prototype
6	05/02/2015 08.00	report
6	05/02/2015 09.00	integrate
6	05/02/2015 10.00	test
6	05/02/2015 11.00	end



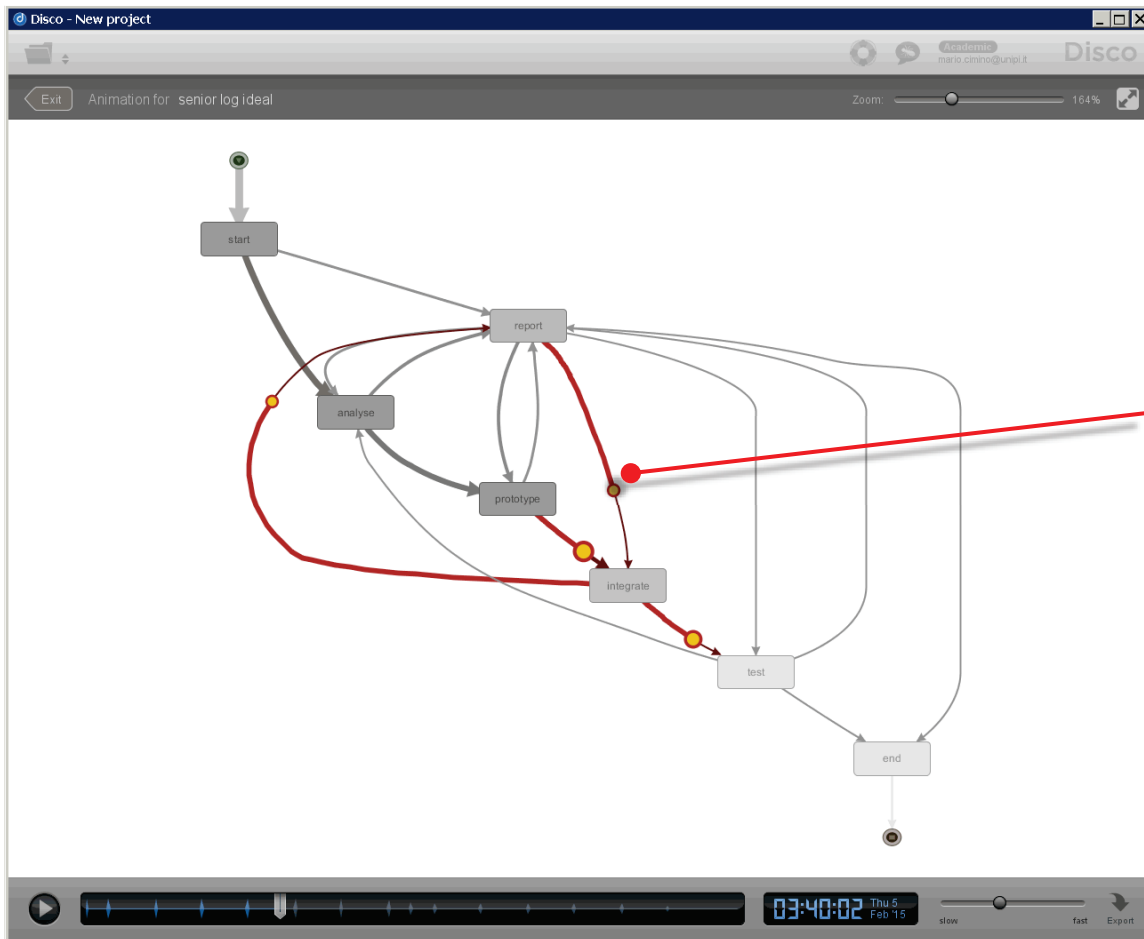
• Hide less frequent transitions between activities to avoid "spaghetti" process map

• See statistics and Cases

• Export data in a number of formats

• Animation

• Process map generated by Disco (based on Fuzzy Miner), showing the frequency of paths between activities

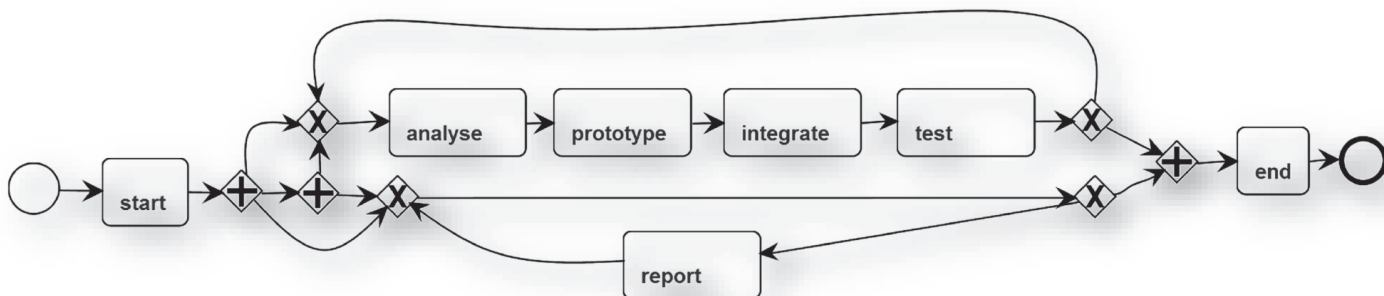


• Tokens flows animation

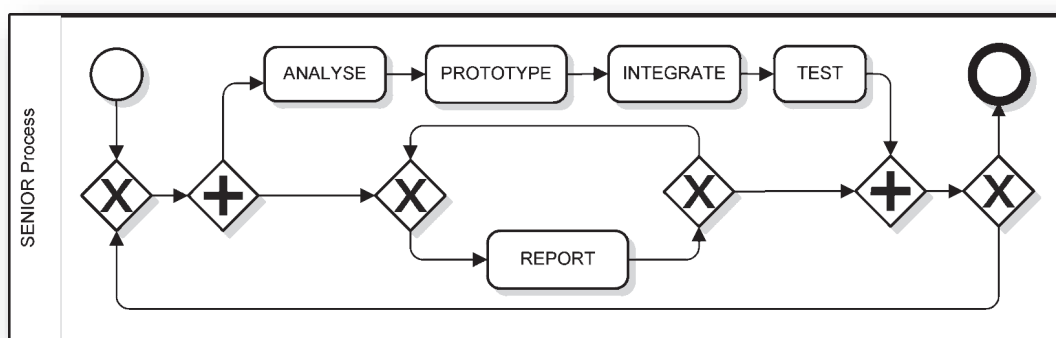
- In ProM, apply “BPMN Miner”
- Select “Inductive Miner” and use default parameters

The screenshot shows the ProM software interface. On the left, the 'Select Miner' dialog is open, showing a list of mining algorithms. The 'Inductive Miner' is selected. On the right, the 'Actions' panel is visible, showing a list of actions. The 'BPMN Miner' action is highlighted. The interface includes a search bar, a playback control bar, and a 'Finish' button.

- Model generated by the inductive miner algorithm



- Since there is no violation in the event log, the generated model is very similar to the normative process:



- In brief: the **Inductive Miner** aims to discover block-structured process models fitting the behavior represented in event log. IM partitions the activities, select the most important process constructs, splits the log and recurses until a base case is encountered.

- A *process tree* is the hierarchical representation of a block-structured workflow net. The leaves of the tree are activities, representing transitions. The nodes of the tree, *operators*, describe how their children are combined: exclusive choice ( $\times$ ), sequential composition ( $\rightarrow$ ), parallel composition ( $\wedge$ ), and loop ( $\cup$ ).

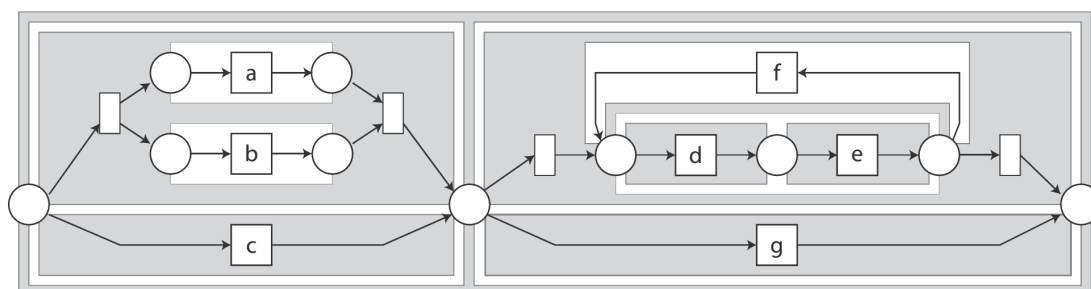
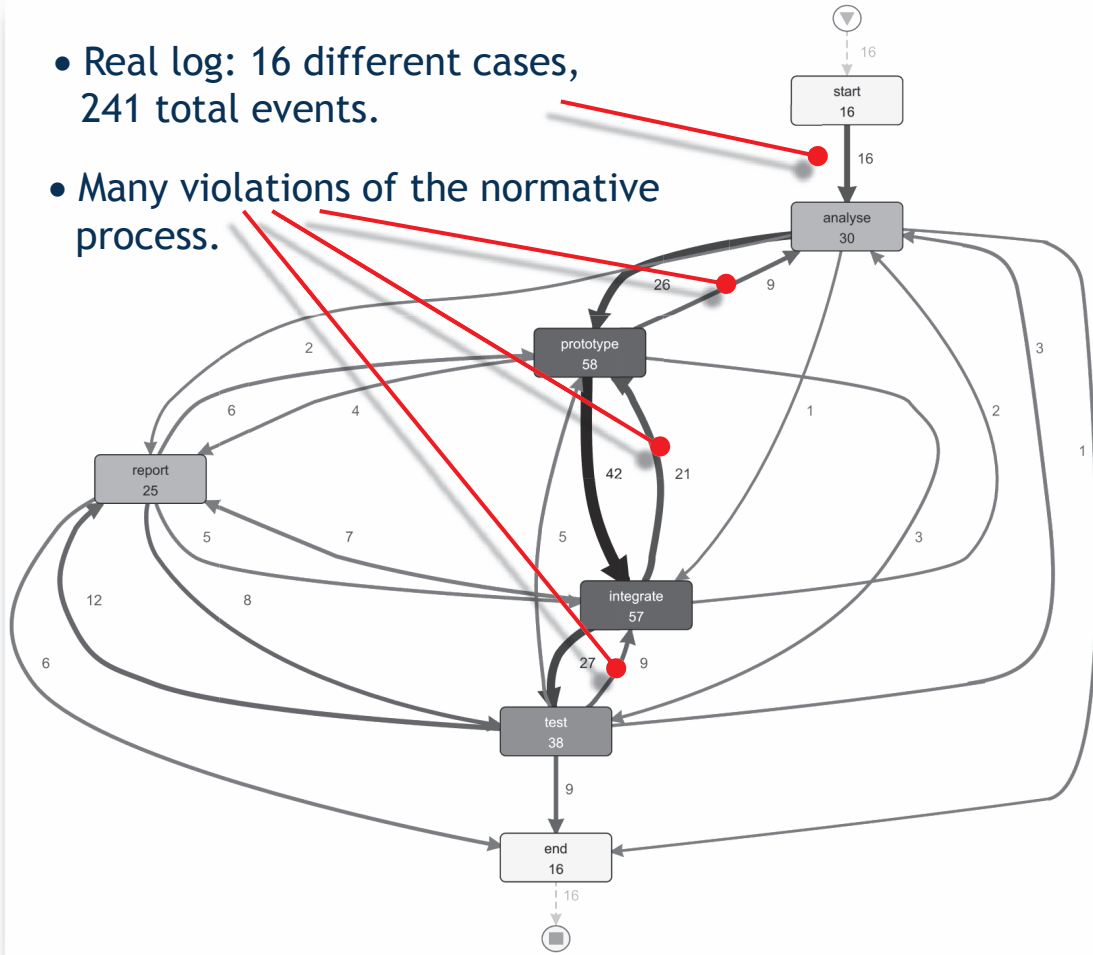
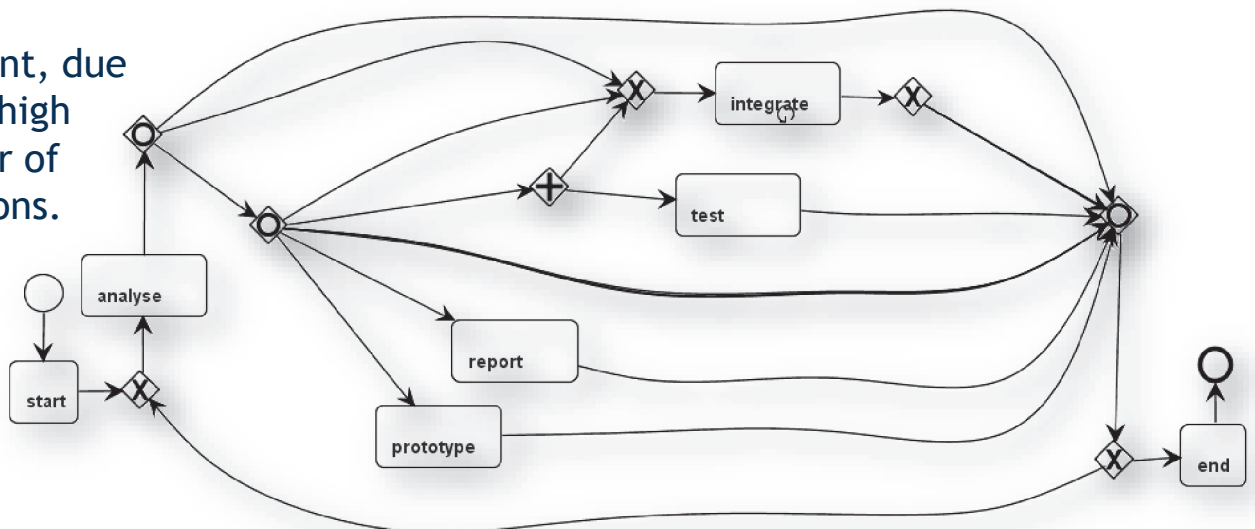
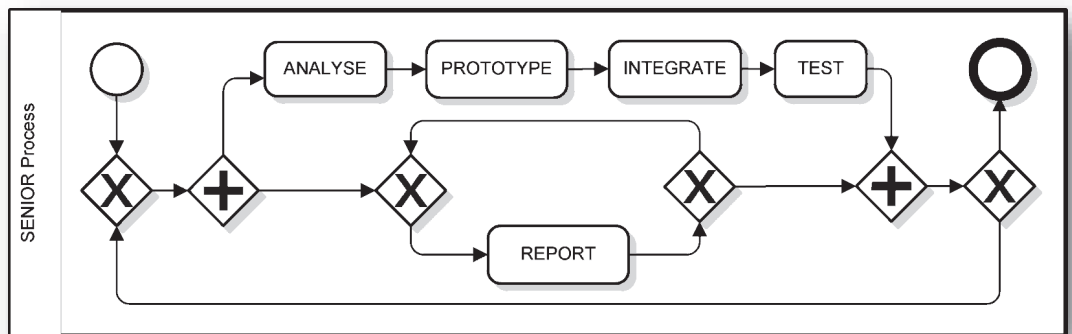


Figure: A block-structured workflow net  $M_E$ ; filled regions denote the block-structure; process tree  $\rightarrow(\times(\wedge(a, b), c), \times(\cup(\rightarrow(d, e), f), g))$  corresponds to this net.

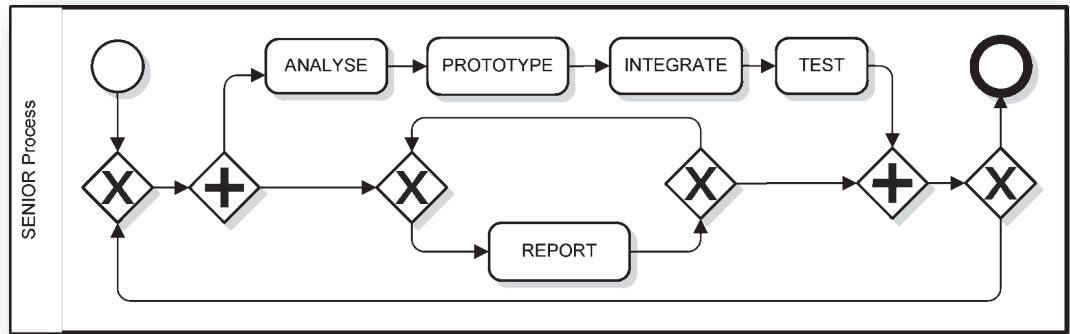
- Real log: 16 different cases, 241 total events.
- Many violations of the normative process.



- Normative process:
- The “spaghetti” model generated by the inductive miner algorithm is very different, due to the high number of violations.

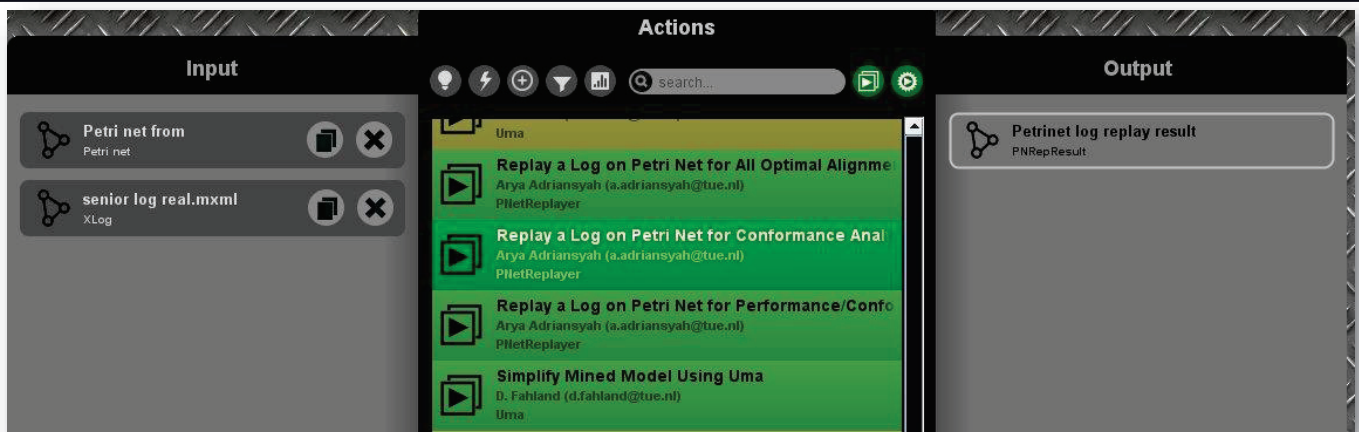


- Conformance checking: to check the real log against the normative process



- Steps on ProM:

- 1: Import both the normative model (senior bpmn.xml) and the real log (senior log real.mxml)
- 2: In the action tab, click on “Select BPMN Diagram”; the normative process model appears.
- 3: Select the BPMN Diagram in the workspace tab, and click the action button; then select “Convert BPMN Diagram to Petri net (control-flow)”;
- 4: In the workspace tab, select the Petri net, and click the action button; then click to add input object and select “senior log real.mxml”
- 5: In the action tab, select “Replay Log on Petri Net for Conformance Analysis”



- 6: Answer YES to the question “No final marking is found on this model. Do you want to create one?”; select “p\_end\_end” as a candidate final marking;

Click on “Add place”.





## 7: Select “Event Name” as a classifier

**Map Transitions to Event Class**  
First, select a classifier. Unmapped transitions will be mapped to a dummy event class.

Choose classifier: Event Name

Continue report?\_merge\_null: NONE

Transition	Event Class
report_split_null	NONE
start_merge_null	NONE
t_act_analyse	analyse
t_act_integrate	integrate
t_act_prototype	prototype
t_act_report	report
t_act_test	test
t_end_end	end
t_start_start	start

## 8: Select NONE for all transitions, except for those with “t\_act”, ”t\_end”, “t\_start” as a name prefix, whose mapping must be accurately checked

## 9: Select “YES, set them to invisible” in the dialog windows on the visibility of unmapped transitions

## 10: Wait the processing for about a half a mminute

**Replay in Petri net**

Choose algorithm: Basic wizard | Advanced

**Select Algorithm**  
Select your replay algorithm

What is the purpose of your replay?  
 Measuring fitness  
 Measuring behavioral appropriateness

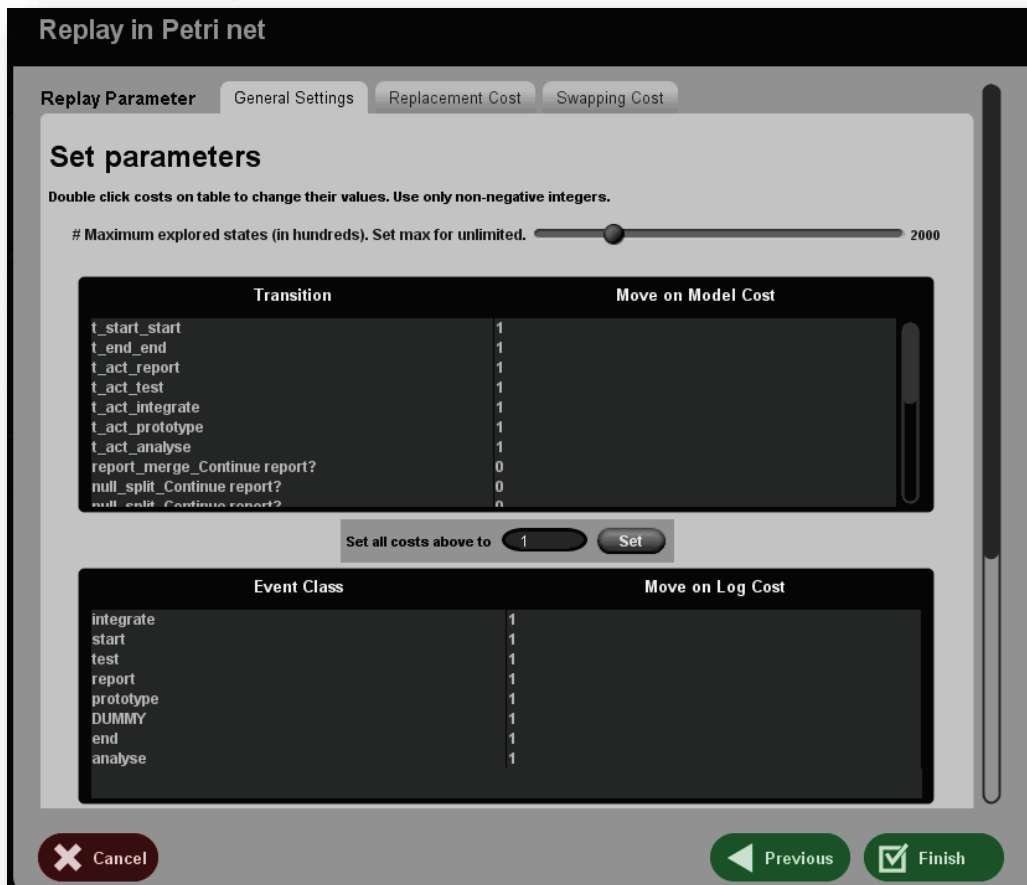
Would you penalize improper completion?  
 Yes  
 No

Suggested algorithm(s)  
 A\* Cost-based Fitness Express with ILP (swap+replacement aware), assuming at most 32767 tokens in each place.  
 A\* Cost-based Fitness Express with ILP, assuming at most 32767 tokens in each place.  
 A\* Cost-based Fitness Express, assuming at most 32767 tokens in each place.

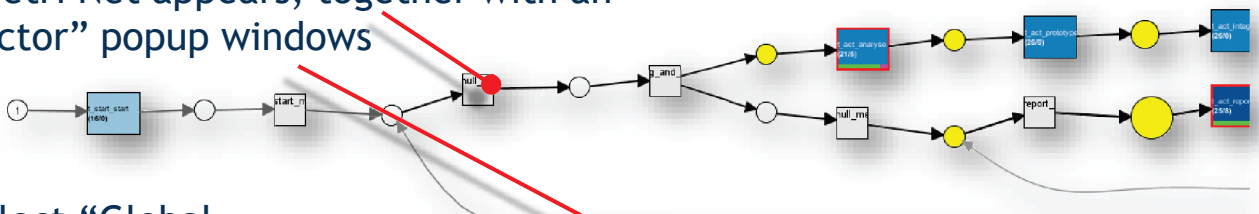
Buttons: Cancel, Previous, Next

## 11: Leave the default algorithm for measuring fitness

12: Leave the default parameters, and click on “Finish”. Wait some seconds



13: A Petri Net appears, together with an “Inspector” popup windows



14: Select “Global Statistics” to see a table with the most important average fitness properties.

- In particular, the average *Trace Fitness* is shown: 0.737457...

- The Trace-Fitness value represents the fitness value of the Petri Net with the log, and indicates how well the event log can be replayed in the discovered Petri Net.

**Inspector**

Info    Display    Filter    Export

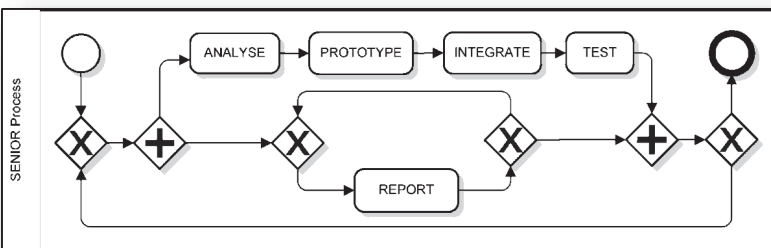
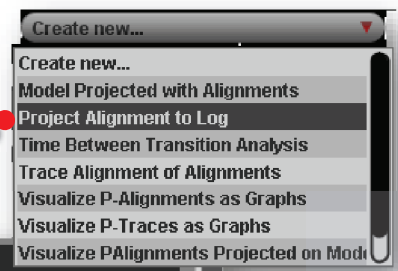
Legend  
View  
Elements Statistics  
Global Statistics (non-filtered traces)

Property	Value
Raw Fitness Cost	6.5625
Queued States	300.4375
Num. States	199.24999999999997
Calculation Time (ms)	37.875
Move-Log Fitness	0.678366384432561
Trace Fitness	0.7374574879682253
Trace Length	15.0
Move-Model Fitness	0.938484436456039

- A fitness value of 1 means that the log can be successfully replayed, whereas a value of 0 means that this is completely not the case.

15: Select *Create new* ⇒ *Project Alignment to log*

16: The individual trace fitness values can be inspected



← The normative process

**LEGEND**

- Synchronous move (move log+model)
- Unobservable move (move model only)
- Skipped event class (move model only)
- Inserted event class (move log only)
- Replaced violation (move log+model)
- Swapped violation (move log+model)

• Case 491381: Fitness=1

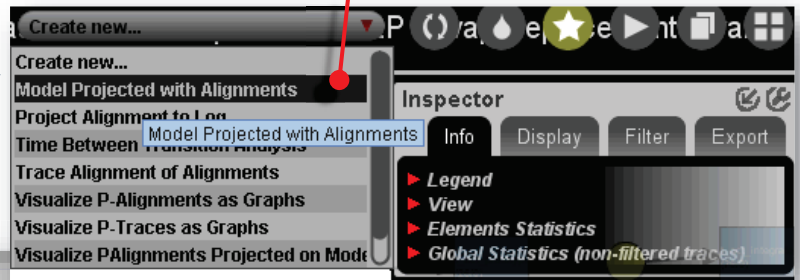
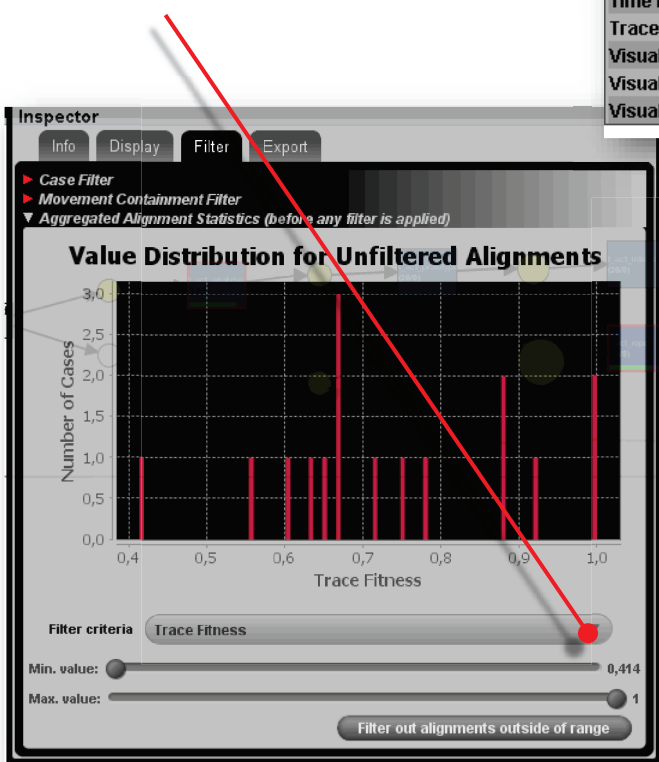
491381, 11/12/2014 22.11, start  
 491381, 11/12/2014 22.12, analyse  
 491381, 15/12/2014 17.05, prototype  
 491381, 06/01/2015 12.07, integrate  
 491381, 22/01/2015 11.22, test  
 491381, 24/01/2015 09.58, report  
 491381, 24/01/2015 16.47, end

• Case 477089: Fitness = 0.92 (report event skipped)

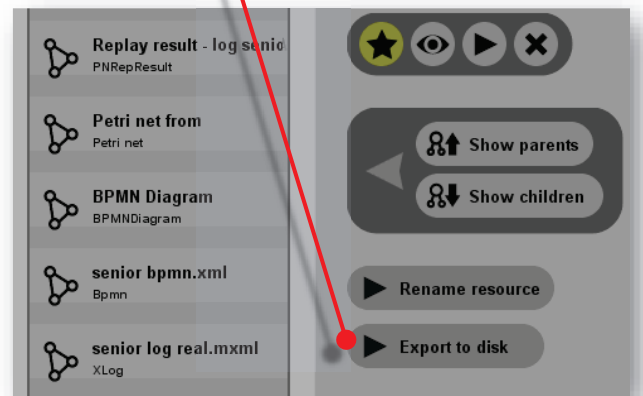
477089, 16/12/2014 21.59, start  
 477089, 16/12/2014 22.00, analyse  
 477089, 26/12/2014 14.49, prototype  
 477089, 08/01/2015 21.22, integrate  
 477089, 11/01/2015 15.34, test  
 477089, 11/01/2015 18.27, end



Select *Create new...> Model Projected with Alignments* to show the Inspector  
 Select *Filter tab > Aggregated Alignment Statistics > Trace Fitness*



1. Go to the workspace tab
2. Select the Replay result in the list
3. Click on “export to disk”
4. Select “Export result report as CSV(.csv)”



Separate cases into clusters according to fitness

<https://tinyurl.com/pdis-k-means>

<http://scistatcalc.blogspot.it/2014/01/k-means-clustering-calculator.html>

Choose File    Perform k-means clustering

Input	Output:-	Centroid values:-
1	# Sample value,	#Centroid index,
1	Centroid index	Centroid value
0.67	1,1	1,0.936
0.61	1,1	2,0.410
0.67	0.67,3	3,0.671
0.75	0.61,3	
0.41	0.67,3	
0.65	0.75,3	
0.71	0.41,2	
0.56	0.65,3	
0.64		
0.67		
0.88		
0.88		
0.78		
0.92		

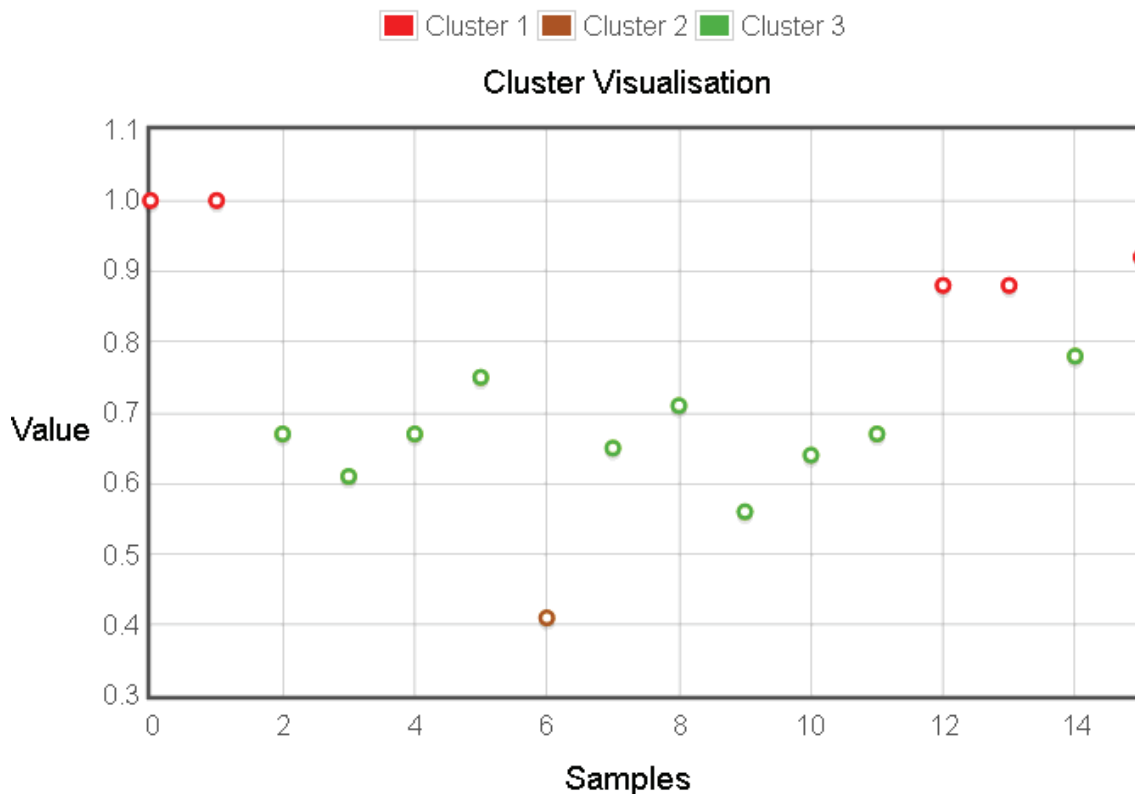
Enter number of clusters (k value):-

Enter number of iterations:-

Clear Input

Index	Case ID	Trace Fitness
1	491381	1
2	477447	1
3	493534	0,67
4	490259	0,61
5	492746	0,67
6	493724	0,75
7	483505	0,41
8	476904	0,65
9	479570	0,71
10	492998	0,56
11	490756	0,64
12	475754	0,67
13	485552	0,88
14	490875	0,88
15	456762	0,78
16	477089	0,92

Separate cases into clusters according to fitness



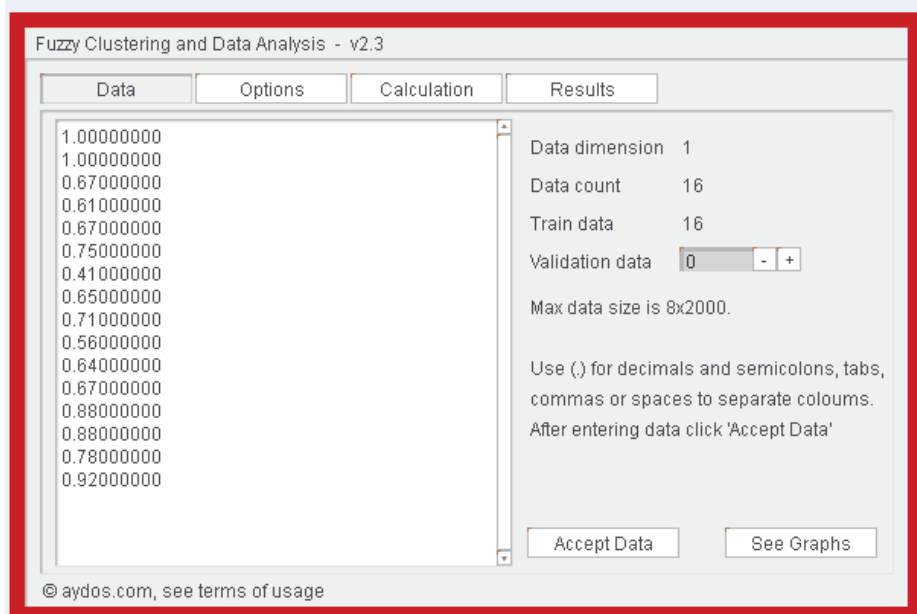
Separate cases into clusters according to fitness

<https://tinyurl.com/pdis-fcm>

<https://aydos.com/fcm/>

## Fuzzy Clustering

Fuzzy logic c-means clustering



Index	Case ID	Trace Fitness
1	491381	1
2	477447	1
3	493534	0,67
4	490259	0,61
5	492746	0,67
6	493724	0,75
7	483505	0,41
8	476904	0,65
9	479570	0,71
10	492998	0,56
11	490756	0,64
12	475754	0,67
13	485552	0,88
14	490875	0,88
15	456762	0,78
16	477089	0,92

Accept data > Options > Calculation > Results

Cluster centers:

0.93

0.67

0.44

Memberships

...

Fuzzy Clustering and Data Analysis - v2.3

Options

Calculation Options

Clusters: 3

Fuzziness coefficient: 2

Maximum iteration: 100

Epsilon: 0.01

Display Options

Decimal digit: 2

Separate colours with: tabs

Fuzzy Clustering and Data Analysis - v2.3

Calculation

Clustering Method: Fuzzy c-means (FCM)

Analysis Method: Fuzzy Least Square Estimation

Calculate Finished.

Fuzzy Clustering and Data Analysis - v2.3

Results

	Current	Previous	Results (ready to copy paste)
Data size	1x16	-	
Train data	16	-	RSME for train data : 0.000000000000
Validation data	0	-	RSQR for train data : 1.000000000000
Clusters	3	-	Clusters centers: 0.93 0.67 0.44
Fuzziness coefficient	2	-	
Normalization	No	-	
Exit iteration	22	-	
Clustering method	FCM	-	Memberships to each clusters: 0.95 0.04 0.01 0.95 0.04 0.01
Analysis method	FLSE	-	

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**Exercise:** Simplified map transitions to event classes

- Import the senior bpmn.xml file in Visual Paradigm and remove the pool
- Export the new BPMN as senior bpmn nopool.xml
- Convert the model to Petri Net via **“Convert BPMN to Petrinet”**  
the resulting Petri Net is more compact
- Carry out the **“Replay a Log on Petri Net for Conformance Analysis”**  
The map transitions to event classes is simplified.

Select mapping

List of Places

Continue report?  
END  
Next iteration?  
START  
p1  
p2  
p3  
p4  
p5

Add Place >>

<< Remove Place

Candidate Initial Marking

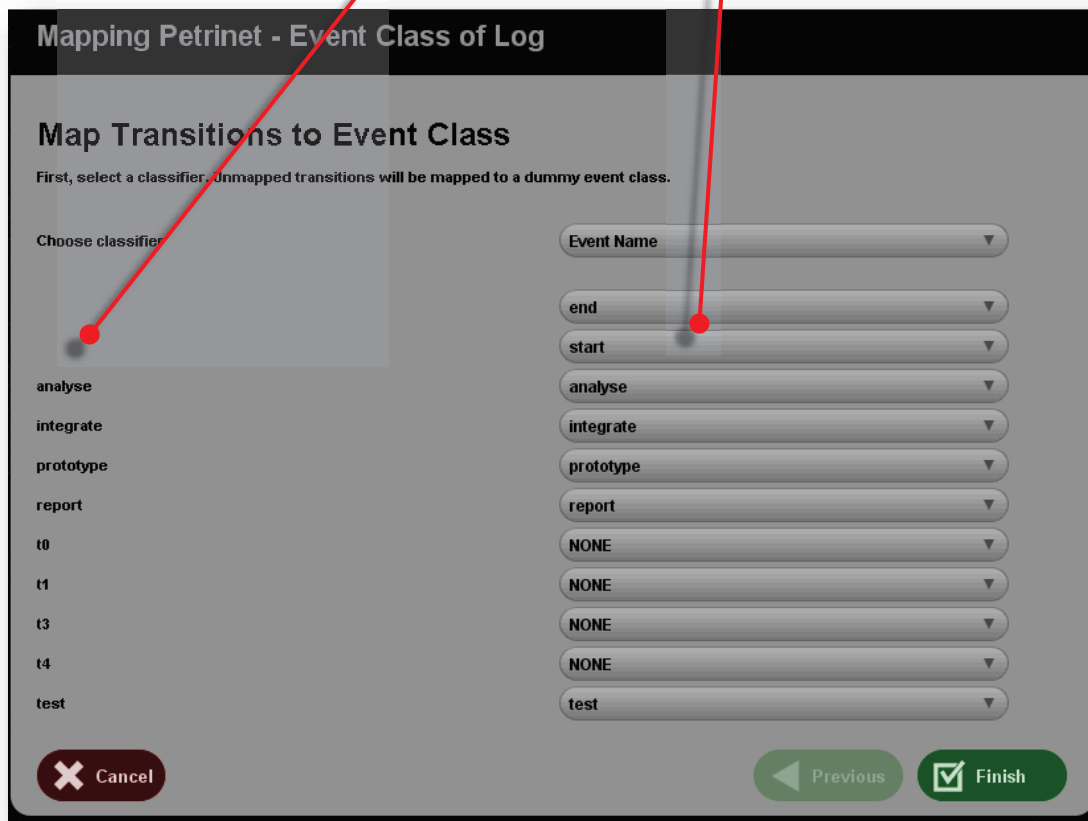
<Empty Marking>

No Initial Marking

No initial marking is found for this model. Do you want to create one?

Yes No

The transition name may not appear due to label errors in the BPMN



Inspect individual cases, compare the trace fitness w.r.t. the other Petri Net

Replay result - log senior log real.mxml on using A\* Cost-based Fitness Ex. Create new...

Case IDs	Trace Fitness
477447	1
491381	1
477089	0,91
485552	0,87
490875	0,87
456762	0,75
493724	0,73
479570	0,68
493534	0,65
492746	0,64
475754	0,63
476904	0,62
490756	0,6
490259	0,58
492998	0,52
483505	0,37

Inspector  
Info Display Filter Export

- ▶ Case Filter
- ▶ Movement Containment Filter
- ▼ Aggregated Alignment Statistics (before any filter is applied)

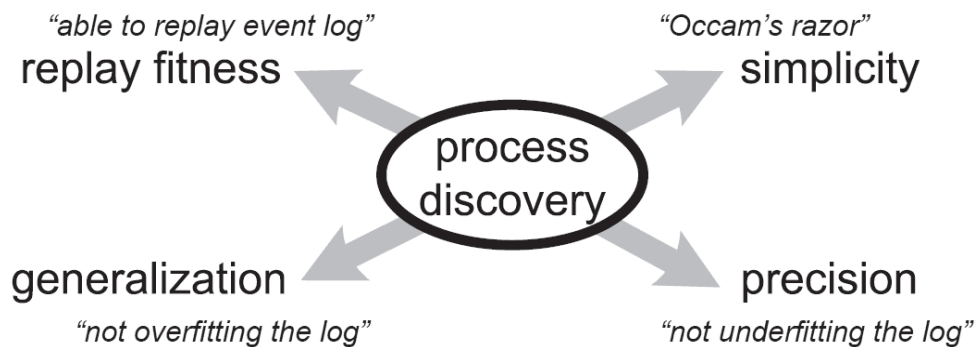
**Value Distribution for Unfiltered Alignments**

Filter criteria: Trace Fitness

Min. value: 0,37  
Max. value: 1

Filter out alignments outside of range

## The four quality dimensions for process discovery



The **Fitness** of a mined Model ( $M_m$ ) measures how much of the observed behavior in the log ( $L$ ) is captured by the process model. Good fitness (close to 1) allows the replay of (most of) the behavior seen in the event log

E.g. the fraction of event patterns represented by the model, the fraction of cases that can be replayed in the model)

$$f(L, M_m) = \frac{1}{2} \left( 1 - \frac{\sum_{i=1}^k n_i m_i}{\sum_{i=1}^k n_i c_i} \right) + \frac{1}{2} \left( 1 - \frac{\sum_{i=1}^k n_i r_i}{\sum_{i=1}^k n_i p_i} \right)$$

$k$	# of different traces.
$n_i$	# of traces of type $k$ in log $L$ .
$m_i$	# of missing tokens (artificially added) parsing $i$ .
$r_i$	# of remaining tokens parsing $i$ .
$c_i$	# of consumed tokens parsing $i$ .
$p_i$	# of produced tokens parsing $i$ .

## Introduction to Process Mining tools

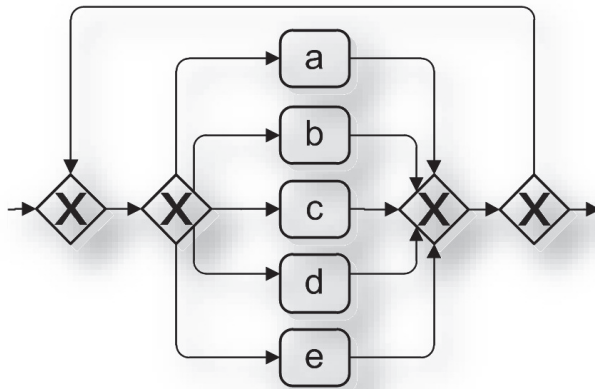
- **Simplicity** is measured by comparing the number of elements (i.e., **#gateways + #sequence flows + #activities**) of the model  $M$  with the number of activities (cardinality of) in the log.

In general it is measured by complexity metrics for process models such as model size or degree of structuredness.

- Fitness and simplicity are not enough to judge the quality of a discovered process model, as clearly shown in the following exercise.
- **Exercise:** Draw a model in BPMN with which you can replay any execution sequence that includes tasks  $a, b, c, d, e$ . Furthermore, discuss the fitness, simplicity, precision, and generalization of such a model for the trace  $\langle a, b, c, d, e \rangle$ .



## • Solution:



- Fitness: it is perfect to the execution sequence as it is able to replay the occurrence of *a* to *e*
- Simplicity: the model is not completely simple as it includes four gateways for characterizing the behavior of five activities.

- **Precision:** The discovered model should not allow for behavior very different from what was seen in the event log. The solution is not very precise because it does not introduce specific constraints on the behavior: any occurrence of *a* to *e* is allowed at any stage.

- A simplified formula for the precision of a mined model (*M*), assuming that  $\{enL\}$  is included in  $\{enM\}$ :

if the  $enM \gg enL$  then the *P* is low  
(too much extra behavior)

$$P(L, M) = \frac{1}{|\varepsilon|} \sum_{e \in \varepsilon} \frac{|en_L(e)|}{|en_M(e)|}$$

- $\varepsilon$  collection of *unique events* in a context of the log.
- $en_M(e)$  enabled activities in the model *M*.
- $en_L(e)$  observed activities actually executed in a similar context in *L*.

## Introduction to Process Mining tools

- **Generalization:** as opposed to precision, this criterion focus on avoiding overly precise models, since event logs are often far from complete.
- It refers to the ability of the model to abstract. The solution model does not constrain the behavior, and then there is hardly any general insight that we can learn from it.
- To calculate precision and generalization with ProM:  
after the Replay result generated by conformance checking, in the workspace select Replay Result, Petri net and the Log  
Then select “Measure Precision/Generalization” and continue with default settings

